Second NASA Formal Methods Workshop 1992

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Contents

Introduction 3
Workshop Agenda 5
A Brief Overview of NASA Langley's Research Program in Formal Methods 9
Welcome and Introduction by Chuck Meissner, Jr. (NASA Langley Research Center)
Why Formal Methods? by Ricky Butler (NASA Langley Research Center)
Tutorial: Design Specification Techniques by Ben DiVito (ViGYAN)
Tutorial: Code Verification Techniques by Michael Holloway (NASA Langley Research Center)
The FAA DFCS Handbook Formal Methods Chapter by John Rushby (SRI International)
Survey of State-of-Practice: Formal Methods in Industry by Dan Craigan (ORA Canada)
Formal Modelisation by Susan Gerhart (National Science Foundation)
Formal Methods Technology Insertion Into FTPP by Rick Harper (Charles Stark Draper Labs)
Formal Methods at IBM Federal Systems by David Hamilton (IBM Federal Systems)
Reliable Computing Platform by Ben DiVito (ViGYAN)
Clock Synchronization: Verification and Implementation by Paul Miner (NASA Langley Research Center)
NASA's Strategy for Technology Transfer by Sally Johnson (NASA Langley Research Center)

by Mark Bickford (Odyssey Re-	search Associates, Inc.)
Boeing's Work in Formal Method by Dave Fura (The Boeing Con	ls npany) 15
DO-178B and Formal Methods by George Finelli (NASA Lang	ley Research Center)
Introduction to the Boyer-Moore by Warren Hunt (Computation	Theorem Prover al Logic, Inc.) 1
Introduction to PVS by Natarajan Shankar (SRI Int	ternational) 1-
Logical Foundations of Computing	ng over the Floating Point Reals esearch Associates, Inc.)
by Richard Flatek (Ouyssey Ite	
	of California at Irvine)
Formal Safety Analysis by Nancy Leveson (University	of California at Irvine)
Formal Safety Analysis by Nancy Leveson (University The FM9001 by Warren Hunt (Computation	of California at Irvine) lal Logic, Inc.) lware iversity)
Formal Safety Analysis by Nancy Leveson (University The FM9001 by Warren Hunt (Computation Derivational Techniques for Hard by Steve Johnson (Indiana University)	of California at Irvine)

Introduction

This publication contains copies of the material presented at the Second NASA Langley Formal Methods Workshop held at the NASA Langley Research Center August 11–13, 1992. The purpose of the workshop was to bring together formal methods researchers and aerospace industry engineers to investigate new opportunities for applying formal methods to aerospace problems. The first part of the workshop was tutorial in nature. The second part of the workshop explored the potential of formal methods to solve current aerospace design and verification problems. The third part of the workshop involved on-line demonstrations of state-of-the-art formal verification tools. Finally, a detailed survey was filled in by the attendees; the results of the survey are compiled in this report.

The workshop was attended by aerospace industry engineers and managers, interested government representatives from FAA, NSA, NCSC, and DARPA, NASA Langley formal-methods contractors, university professors, and NASA personnel. A list of attendees is included in this publication.

Second NASA Langley Formal Methods Workshop H. J. E. Reid Conference Center

Tuesday, August 11, 1992

Topagait to	
7:30	Bus Leaves Radisson Hotel for Reid Conference Center
8:00 - 8:3) Late Registration
8:30 - 8:4	Welcome and Introduction Charles Meissner, Jr., Head, System Validation Methods Branch
8:45 - 9:	Why Formal Methods? Ricky Butler, NASA Langley Research Center
9:30 – 10:	Tutorial: Formal Methods Ben DiVito, VíGYAN Michael Holloway, NASA Langley Research Center
10:45 - 11:6	0 Break
11:00 - 11:	The FAA DFCS Handbook — Formal Methods Chapter John Rushby, SRI International
11:30 - 12:	Survey of State-of-Practice Formal Methods in Industry Dan Craigan, ORA Canada
12:30 - 1:	Lunch in NASA Cafeteria
1:30 - 2:	Formal Modellsation Susan Gerhart, National Science Foundation
2:00 - 2:	Formal Methods Technology Insertion Into FTPP Rick Harper, Charles Stark Draper Labs
2:30 - 3:	00 Break
3:00 - 3	Formal Methods at IBM Federal Systems David Hamilton, IBM Federal Systems
3:40 - 4	40 Reliable Computing Platform Ben DiVito, ViGYAN
4:40 - 5	OC Clock Synchronization Verification and Implementation Paul Miner, NASA Langley Research Center
5:00	Bus Leaves Reid Conference Center for Radisson Hotel
6:30 - 9	Workshop Dinner at the Radisson Hotel

Wednesday, August 12, 1992 Bus Leaves Radisson Hotel for Reid Conference Center 8:00 NASA's Strategy for Technology Transfer 8:30 8:45 Sally Johnson, NASA Langley Research Center Verification of FTPP Scoreboard and Spectool 8:45 - 9:15 Mark Bickford, Odyssey Research Associates, Inc. Boeing's Work in Formal Methods 9:15 - 9:45 Dave Fura, The Boeing Company DO-178B and Formal Methods 9:45 - 10:00 George Finelli, NASA Langley Research Center 10:00 - 10:30 **Break** introduction to the Boyer-Moore Theorem Prover 10:30 - 11:10 David Russinoff, Computational Logic, Inc. Introduction to PVS 11:10 - 11:50 Natarajan Shankar, SRI International Logical Foundations of Computing over the Floating Point Reals 11:50 - 12:30 Richard Platek, Odyssey Research Associates, Inc. 1:30 **Lunch in NASA Cafeteria** 12:30 nama pelika salakan kecama 1:30 -2:10 Formal Safety Analysis Nancy Leveson, University of California at Irvine The FM9001 2:10 - 2:45 Warren Hunt, Computational Logic, Inc. Break 2:45 -3:00 Panel: Degree of Mechanization in Formal Methods 3:00 -Paul Miner, NASA Langley Research Center, Moderator Nancy Leveson, University of California at Irvine Richard Platek, Odyssey Research Associates, Inc. John Rushby, SRI International **Exhibits of Formal Methods Tools and Techniques** 4:00 -6:00 Cash Bar Social 5:00 6:00 Bus Leaves Reid Conference Center for Radisson Hotel 6:00

Thursday, August 13, 1992

8:00	Bus Leaves Radisson Hotel for Reid Conference Center
8:30 - 9:00	Derivational Techniques for Hardware Steven Johnson, Indiana University
9:00 - 10:00	Panel: Issues In Hardware Verification Victor Carreno, NASA Langley Research Center, Moderator Mark Bickford, Odyssey Research Associates, Inc. Warren Hunt, Computational Logic, Inc. Steven Johnson, Indiana University Phillip Windley, University of Idaho
10:00 - 10:15	Break
10:15 - 11:15	Panel: Issues In Design/Code Verification Michael Holloway, NASA Langley Research Center, Moderator Ben DiVito, VíGYAN Damir Jamsek, Odyssey Research Associates, Inc. Miriam Leeser, Cornell University John Rushby, SRI International
11:15 - 11:45	Formal Methods Survey Completion
11:45 - 12:00	Closing Remarks Ricky Butler, NASA Langley Research Center
12:00	Bus Leaves Reid Conference Center for Radisson Hotel (for those not attending the technical review)

A Brief Overview of NASA Langley's Research Program in Formal Methods

System Validation Methods Branch NASA Langley Research Center Hampton, Virginia

September 21, 1992*

Abstract

This paper presents an overview of NASA Langley's research program in formal methods. The major goal of this work is to bring formal methods technology to a sufficiently mature level for use by the United States aerospace industry. Towards this goal, work is underway to design and formally verify a fault-tolerant computing platform suitable for advanced flight control applications. Also several direct technology transfer efforts have been initiated that apply formal methods to critical subsystems of real aerospace computer systems. The research team consists of six NASA civil servants and contractors from Boeing Military Aircraft Company, Computational Logic Inc., Odyssey Research Associates, SRI International, University of California at Davis, and Vigyan Inc.

Motivation

NASA Langley Research Center has been developing techniques for the design and validation of flight critical systems for over two decades. Although much progress has been made in developing methods which can accommodate physical failures, the design flaw remains a serious problem [2, 3, 4, 5, 6, 7, 8].

A recent report by the National Center For Advanced Technologies ¹ has identified "Provably Correct System Specification" and "Verification Formalism For Error-Free Specification" as key areas of research for future avionics software and ultrareliable electronics systems [9]. Aerospace engineers attending the NASA-LaRC Flight Critical Digital Systems Technology Workshop [10] listed techniques for the validation of concurrent and fault-tolerant computer systems high on the list of research priorities for NASA.

^{*}This is an updated version of the a paper entitled "NASA Langley's Research Program in Formal Methods" presented at COMPASS 91 [1].

¹A technical council funded by the Aerospace Industries Association of America (AIA) that represents the major U.S. aerospace companies engaged in the research, development and manufacture of aircraft, missiles and space systems and related propulsion, guidance, control and other equipment.

A further motivation for the use of formal methods is the practical limitations of lifetesting methods to quantify reliability in the ultrareliable domain. Unfortunately, the quantification of reliability in the presence of design faults has been found to be infeasible whether applied to hardware or software (standard or fault-tolerant) [11]. Therefore the use of nonstatistical method is necessary.

Formal Methods

Formal methods are the applied mathematics of computer systems engineering. There are many different types of formal methods with various degrees of rigor. The following is a useful (first-order) taxonomy of the degrees of rigor in formal methods:

Level-1: Formal specification of all or part of the system.

Level-2: Formal specification at two or more levels of abstraction and paper and pencil proofs that the detailed specification implies the more abstract specification.

Level-3: Formal proofs checked by a mechanical theorem prover.

Level 1 represents the use of mathematical logic or a specification language that has a formal semantics to specify the system. This can be done at several levels of abstraction. For example, one level might enumerate the required abstract properties of the system, while another level describes an implementation which is algorithmic in style. Level 2 formal methods goes beyond level 1 by developing pencil-and-paper proofs that the more concrete levels logically imply the more abstract-property oriented levels. Level 3 is the most rigorous application of formal methods. Here one uses a semi-automatic theorem prover to make sure that all of the proofs are valid. The Level 3 process of convincing a mechanical prover is really a process of developing an argument for an ultimate skeptic who must be shown every detail.

It is also important to realize that formal methods is not an all-or-nothing approach. The application of formal methods to the most critical portions of a system is a pragmatic and useful strategy. Although a complete formal verification of a large complex system is impractical at this time, a great increase in confidence in the system can be obtained by the use of formal methods at key locations in the system.

Research Team

The Langley formal methods program involves both in-house researchers and industrial/academic researchers working under contract to NASA Langley. Currently the in-house team consists of six civil servants and one in-house contractor (Vigyan Inc.). NASA Langley has awarded three contracts specifically devoted to formal methods (from the competitive NASA RFP 1-22-9130.0238). The selected contractors were SRI International, Computational Logic Inc., and Odyssey Research Associates. The three contracts are five-year, task assignment contracts with total spending authority at approximately \$2.5M per contract. Another task-assignment contract with Boeing Military Aircraft Company (BMAC) is being used to

explore formal methods as well. Through this contract BMAC is funding research at the University of California at Davis and California Polytechnic State University to assist them in the use of formal methods in aerospace applications.

NASA Langley's Research Strategy

The basic strategy of the research effort is to apply existing formal methods to challenging aerospace designs. This strategy leverages the huge investment of DARPA and National Security Agency in development of tools and concentrates on the problems specific to the aerospace problem domain. We have sought to build a strong inhouse research program as well as use contracts with the leading U.S. formal methods research teams (i.e. SRI, CLI, ORA) and aerospace industrial teams (BMAC, Draper Labs). In the short term we are seeking to apply formal methods to critical subsystems. In the medium term we are designing and verifying a reliable computing platform. Only in the long-term will we seek to make production-quality verification tools that are easily used by design engineers without overly specialized, detailed knowledge of formal methods.

The design of a digital flight control system involves two dissimilar activities:

- 1. design and implementation of control laws
- 2. design of the fault-tolerant computing platform which executes the control laws

Although these design activities are intimately connected, they require uniquely different skills. The first activity requires knowledge of feedback control theory and aerodynamics as well as numerical methods. The second activity requires knowledge of fault-tolerance theory and computer architecture. Although both activities are essential, we are concentrating at this time on the second activity. To facilitate the development and demonstration of tools and techniques to support the second activity, a reliable computing platform (RCP) is being developed. Also, several tasks are underway to facilitate the transfer of formal methods technology to aerospace industry.

The Reliable Computing Platform

The Reliable Computing Platform (RCP) dispatches the control-law application tasks and executes them on redundant processors. The reliable computing platform performs the necessary fault-tolerant functions and provides an interface to the network of sensors and actuators.

The RCP consists of both hardware and software components. A real-time operating system provides the applications software developer with a reliable mechanism for dispatching periodic tasks on a fault-tolerant computing base that appears to him as a single ultrareliable processor. Traditionally, an operating system has been implemented as an executive (or main program) that invokes subroutines implementing the application tasks. Communication between the tasks has been accomplished by use of shared memory. This strategy is effective for systems with nominal reliability requirements where a simplex processor can

be used. For ultra-reliable systems, the additional responsibility of providing fault tolerance makes this approach untenable.

For these reasons, the operating system and replicated computer architecture must be designed together so they mutually support the goals of the RCP. A multi-level hierarchical specification of the RCP is shown in figure 1.

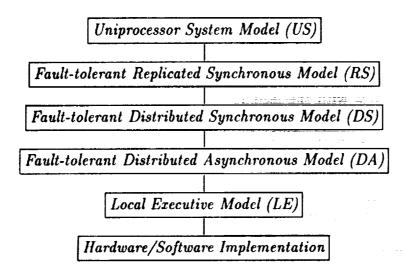


Figure 1: Hierarchical Specification of the Reliable Computing Platform (RCP)

The top level of the hierarchy describes the operating system as a function that sequentially invokes application tasks. This view of the operating system will be referred to as the uniprocessor specification (US), which is formalized as a state transition system and forms the basis of the specification for the RCP. Fault tolerance is achieved by voting results computed by the replicated processors operating on the same inputs. Interactive consistency checks on sensor inputs and voting of actuator outputs require synchronization of the replicated processors. The second level in the hierarchy (RS) describes the operating system as a synchronous system where each replicated processor executes the same application tasks. The existence of a global time base, an interactive consistency mechanism and a reliable voting mechanism are assumed at this level. Level 3 of the hierarchy breaks a frame into four sequential phases. This allows a more explicit modeling of interprocessor communication and the time phasing of computation, communication, and voting. At the fourth level, the assumptions of the synchronous model must be discharged. Rushby and von Henke [12] report on the formal verification of Lamport and Melliar-Smith's [13] interactive-convergence clock synchronization algorithm. This algorithm can serve as a foundation for the implementation of the replicated system by bounding the amount of asynchrony in the system so that it can duplicate the functionality of the DS model. Dedicated hardware implementations of the clock synchronization function are a long-term goal. The LE model is currently under development. This model describes the actions on each local processor delineating how each processor schedules tasks, votes results and rewrites its own local memory with voted values. Of primary importance in this specification is the utilization of a memory management

unit by the local executive in order to prevent the overwriting of incorrect memory locations while recovering from the effects of a transient fault. There will probably be another level of specification introduced before the final implementation in hardware and software is reached. The research activity will culminate in a detailed design and prototype implementation. Figure 2 depicts the generic hardware architecture assumed for implementing the replicated system. Single-source sensor inputs are distributed by special purpose hardware executing a Byzantine agreement algorithm. Replicated actuator outputs are all delivered in parallel to the actuators, where force-sum voting occurs. Interprocessor communication links allow replicated processors to exchange and vote on the results of task computations. As previously suggested, clock synchronization hardware may be added to the architecture as well.

The hardware architecture is a classic N-modular redundant (NMR) system with a small number N of processors. Single-source sensor inputs are distributed by special purpose hardware executing a Byzantine agreement algorithm. Replicated actuator outputs are all delivered in parallel to the actuators, where force-sum voting occurs. Interprocessor communication links allow replicated processors to exchange and vote on the results of task computations. This is illustrated in figure 2.

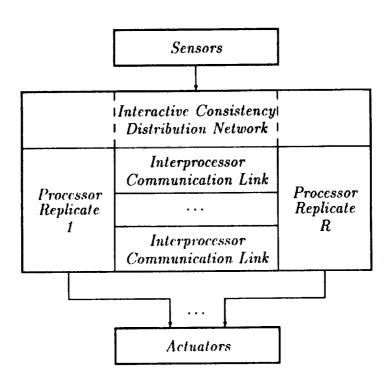


Figure 2: Generic hardware architecture.

The Division of Labor

The in-house team at NASA has been orchestrating the effort to apply formal methods to the RCP. The design problem has been decomposed into several separate activities, some of

which are being investigated by contractual teams and others by the in-house team. The efforts are roughly divided as follows:

in-house: system architecture, clock synchronization SRI: Clock synchronization, fault-tolerance

CLI: Byzantine Agreement Circuits, clock synchronization

ORA: Byzantine Agreement Circuits, applications

BMAC: Hardware Verification, formal requirements analysis

NASA In-house Work

The in-house team has concentrated on the system architecture for the RCP. The top two levels of the RCP were originally formally specified in standard mathematical notation and connected via mathematical (i.e. level 2 formal methods) proof[14, 15]. Under the assumption that a majority of processors are working in each frame, the proof establishes that the replicated system computes the same results as a single processor system not subject to failures. Sufficient conditions were developed that guarantee that the replicated system recovers from transient faults within a bounded amount of time. SRI subsequently generalized the models and constructed a mechanical proof in Ehdm [16]. Next, the NASA inhouse team developed the third and fourth level models. The top two levels and the two new models were then specified in Ehdm and all of the proofs were done mechanically using the Ehdm 5.2 prover [17, 18]

Inhouse work is underway to design and implement a fault-tolerant clock synchronization circuit capable of recovery from transient faults [19, 20]. The circuit is being implemented using programmable logic devices (PLDs) and FOXI fiber optic communications chips [21].

Contractual Efforts

SRI International

The redundancy management strategies of virtually all fault-tolerant systems depend upon some form of voting which in turn depends upon synchronization. Although in many systems the clock synchronization function has not been decoupled from the applications (e.g. the redundant versions of the applications synchronize by messages), research and experience have led us to believe that solving the synchronization problem independently from the applications design can provide significant simplification of the system [22, 23]. The operating system is built on top of this clock-synchronization foundation. Of course, the correctness of this foundation is essential. Thus, the clock synchronization algorithm and its implementation are prime candidates for formal methods. The verification strategy shown in figure 3 is being explored. The top-level in the hierarchy is an abstract property of the form:

$$\forall$$
 non-faulty $p, q: |C_p(t) - C_q(t)| < \delta$

where δ is the maximum clock skew guaranteed by the algorithm as long as a sufficient number of clocks (and the processors they are attached to) are working. The function $C_p(t)$

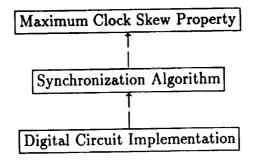


Figure 3: Hierarchical Verification of Clock Synchronization

gives the value of clock p at real time t. The middle level in the hierarchy is a mathematical definition of the synchronization algorithm. The bottom level is a detailed digital design of a circuit that implements the algorithm. The bottom level is sufficiently detailed to make translation into silicon straight forward.

The verification process involves two important steps: (1) verification that the algorithm satisfies the maximum skew property and (2) verification that the digital circuitry correctly implements the algorithm. The first step has already been completed by SRI International. The first such proof was accomplished during the design and verification of SIFT [13]. The proof was done by hand in the style of most journal proofs. More recently this proof step has been mechanically verified using the Ehdm theorem prover [12]. In addition, SRI has mechanically verified Schneider's clock synchronization paradigm [24] using Ehdm[25]. A further generalization was found at NASA Langley [20]². The design of a digital circuit to distribute clock values in support of fault-tolerant synchronization has been completed by SRI International and is currently being formally verified.³

SRI is currently writing a chapter for the FAA Digital Systems Validation Handbook Volume III on formal methods [26]. The handbook provides detailed information about digital system design and validation and is used by the FAA certifiers.

Computational Logic Inc.

Fault-tolerant systems, although internally redundant, must deal with single-source information from the external world. For example, a flight control system is built around the notion of feedback from physical sensors such as accelerometers, position sensors, pressure sensors, etc. Although these can be replicated (and they usually are), the replicates do not produce identical results. In order to use bit-by-bit majority voting all of the computational replicates must operate on identical input data. Thus, the sensor values (the complete redundant suite) must be distributed to each processor in a manner which guarantees that all working processors receive exactly the same value even in the presence of some faulty processors. This is the classic Byzantine Generals problem [27]. CLI is investigating the formal verifica-

²The bounded delay assumption was shown to follow from the other assumptions of the theory.

³Unlike the NASA inhouse circuit, the SRI intent is that the convergence algorithm be implemented in software.

tion of such algorithms and their implementation. They have formally verified the original Marshall, Shostak, and Lamport version of this algorithm using the Boyer Moore theorem prover [28]. They have also implemented this algorithm down to the register-transfer level and demonstrated that it implements the mathematical algorithm [29] and then subsequently verified the design down to a hardware description language (HDL) developed at CLI [30].

CLI has reproduced the SRI verification of the interactive convergence algorithm using the Boyer-Moore theorem prover [31]. CLI has also developed a formal model of asynchronous communication and demonstrated its utility by formally verifying a widely used protocol for asynchronous communication called the bi-phase mark protocol, also known as "Bi-Φ-M," "FM" or "single density" [32]. It is one of several protocols implemented by microcontrollers such as the Intel 82530 and is used in the Intel 82C501AD Ethernet Serial Interface.

Odyssey Research Associates

ORA has also been investigating the formal verification of Byzantine Generals algorithms. They have focused on the practical implementation of a Byzantine-resilient communications mechanism between Mini-Cayuga micro-processors [33, 34, 35]. The Mini-Cayuga is a small but formally verified microprocessor developed by ORA. It is a research prototype and has not been fabricated. The communications circuitry would serve as a foundation for a fault-tolerant architecture. It was designed assuming that the underlying processors were synchronized (say by a clock synchronization circuit). The issues involved with connecting the Byzantine communications circuit with a clock synchronization circuit and verifying the combination has not yet been explored.

Another task that has been started with ORA is to apply their Ada verification tools to aerospace applications. This effort consists of two subtasks. The first subtask is to verify some utility routines obtained from the NASA Goddard Space Flight Center and the NASA Lewis Research Center using their Ada Verification Tool named Penelope [36]. This subtask was accomplished in two steps: (1) a formal specification of the routines and (2) formal verification of the routines. Both steps uncovered errors in the routines [37]. The second subtask was to formally specify the mode-control panel logic of a Boeing-737 experimental aircraft system using Larch (the specification language used by Penelope) [38].

A joint project between ORA and Charles Stark Draper Laboratory (CSDL) has been initiated. The CSDL has been funded by NASA Langley to build fault-tolerant computer systems for over two decades. They have recently become interested in the use of formal methods to increase confidence in their designs. ORA has formally specified an important circuit (called the scoreboard) of the Fault-Tolerant Parallel Processor (FTPP) [39] in Caliban [40]. Work is currently underway to formally verify the circuit.

Boeing Military Aircraft Co.

The Boeing Company has been sponsored by NASA Langley to develop advanced validation and verification techniques for fly-by-wire systems. As part of the project, Boeing is exploring the use of formal methods. The goal of this work is two-fold: 1) technology transfer of formal methods to Boeing, and 2) assessment of formal methods technology maturity.

NASA Langley has been involved in a cooperative research partnership with Boeing to facilitate the acceptance and adoption of this high-risk, high-payoff technology by Boeing. The first step was to demonstrate that formal verification of "real" hardware devices is, in fact, feasible. The first Boeing tasks concentrated on applying the HOL hardware verification methodology to a set of hardware devices. With the assistance of a subcontract with U. C. Davis, Boeing verified a set of hardware devices, including a microprocessor[41], a floating-point coprocessor similar to the Intel 8087 but smaller[42, 43], a direct memory access (DMA) controller similar to the Intel 8237A but smaller[44], and a set of memory-management units[45, 46]. U. C. Davis also developed the generic-interpreter theory to aid in the formal specification and verification of hardware devices[47, 48, 49], and a horizontal-integration theory for composing verified devices into a system[50, 51, 52, 53].

After demonstrating the feasibility of verifying standard hardware devices, Boeing was ready to apply the methodology to a set of proprietary hardware devices being developed inhouse for use in a number of aeronautics and space applications. NASA sponsored a Boeing engineer to work with the Processor Interface Unit (PIU) design team to formally specify and verify the device. Although the NASA contract with Boeing will end in FY93, Boeing has already capitalized on the NASA program and has started their own IR&D effort to continue applying formal methods to the set of devices.

The cooperative research effort with Boeing has helped NASA Langley to assess the maturity of formal methods technology with respect to state-of-the-practice digital flight-control systems. First, Boeing was tasked to analyze the suitability of the VIPER chip for application to digital flight controls and to assess the design/verification methodology used on the VIPER[54]⁴. The generic-interpreter and horizontal-integration theories developed at U. C. Davis provide models to guide the specification and verification of hardware devices. Application of formal methods to the PIU has demonstrated that formal methods can be practically applied to the digital hardware devices being developed by Boeing today and has given NASA insight on how to make the process more cost effective.

Work is also progressing on a methodology for formal requirements analysis for aircraft systems[58, 59]. This work, being performed under a subcontract to California Polytechnic State University, includes development of a Wide-Spectrum Requirements Specification Language (WSRSL) and prototype tools to support the language. A set of requirements for an Advanced Subsonic Civil Transport (ASCT) developed by a Boeing engineer under previous NASA funding is being rewritten in WSRSL to demonstrate the use of the language and toolset. Since WSRSL is a formal language, the specification can be formally analyzed for syntactic correctness, completeness, and consistency. NASA Langley is currently evaluating WSRSL as a candidate requirements specification tool for the fly-by-light/power-by-wire project. Future plans include possible development of an automatic translator to Ehdm (SRI International's theorem prover) to facilitate verification of functional correctness as well.

⁴NASA Langley has just completed a 3 year Memorandum of Understanding (MOU) with the U.K. Royal Signals and Radar Establishment (RSRE) in formal methods. The MOU focused on the VIPER microprocessor and the verification methodology used in its development. Computational Logic Inc. and Langley inhouse researchers also performed assessments of the VIPER project[55, 56, 57].

NASA FM Repository

An anonymous FTP account has been set up at Langley to make the research results readily available. Formal specifications, research papers, and other useful information will be stored in machine-readable form. To access this repository, one must issue the following command: "ftp air16.larc.nasa.gov". One then supplies "anonymous" as the user name and his FTP address as the password.

Summary

Although the NASA program covers a wide-spectrum of theoretical and practical problem domains, it is strongly focused on the goal of designing a fault-tolerant reliable computing base which can support real-time control applications. Much progress has already been made in applying formal methods to critical subsystems such as clock synchronization, Byzantine agreement, voting, etc. The challenge ahead is to integrate all of these activities to accomplish a complete verification of the total RCP system and to continue the transfer of this technology to the aerospace industry.

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Welcome and Introduction

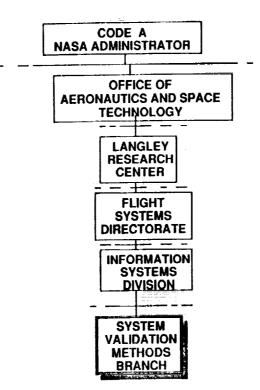
Charles Meissner, Jr.
Head, System Validation Methods Branch
NASA Langley Research Center

WELCOME AND INTRODUCTION

FORMAL METHODS WORKSHOP NASA LANGLEY RESEARCH CENTER AUGUST 11-13, 1992

Charles W. Meissner, Jr.
NASA Langley Research Center

NASA ORGANIZATION VERTICAL CUT TO SVMB



LANGLEY FAULT-TOLERANT DIGITAL SYSTEMS HISTORICAL PERSPECTIVE

CA. 1972

ARCS

F-T SYSTEM DESIGN

CARSRA

RELIABILITY ANALYSIS

SIFT

F-T COMPUTER

FTMP

F-T COMPUTER

CARE III

RELIABILITY

LIC SOFTWARE

S/W ERROR ANALYSIS

IAPSA

F-T DFCS DESIGN

SURE/ASSIST

RELIABILITY ANALYSIS

CA. 1992

AIPS

DISTRIBUTED F-T SYSTEM

ULTRARELIABLE DIGITAL AVIONICS

CONTROL SYSTEMS BECOMING THE PRACTICAL EQUIVALENT OF PRIMARY STRUCTURE

- U.S. FAR 1309-1 Requires P(fail)<10⁻⁹ for statistical compliance
- · Reliability can't be estimated to this level
- Experienced engineering and operational judgement used for compliance

FAULT-TOLERANT DIGITAL SYSTEMS ARE NECESSARY FOR PRACTICAL REALIZATION OF ADVANCED CONTROL

- Analog functionality insufficient for advanced control
- Analog too high in size, weight, power
- Digital system components not adequately reliable use redundancy to increase reliability

FORMAL METHODS FOR FLIGHT-CRITICAL SYSTEMS

- The only scientifically satisfactory approach to aspects of the digital validation process is through reasoning
- Formal methods may become important sooner than is commonly supposed in the aerospace community
- SVMB has put an emphasis on formal methods

Industry/FAA focus is essential feature of our formal methods work

Why Formal Methods?

Ricky Butler
System Validation Methods Branch
NASA Langley Research Center

Outline

Why Formal Methods?

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Ricky W. Butler NASA Langley Research Center

August 11, 1992

- formal requirements specification (phonebook example)

- hardware verification

code verificationdesign verification

Limitations of Formal Methods

Introduction to the Formal Specification and Verification

• The Digital Flight Control System Validation Problem

• What is Formal Methods?

A Small Sample of Aerospace Design Errors:

• F14 lost to uncontrollable spin, traced to tactical software. [SEN 9 5]

• F18: plane crashed due to missing exception condition, pilot OK. [SEN 6 2]

• AFTI-F16—Asynchronous operation, skew, and sensor noise led each channel to declare others failed in flight test 44. Flown home on a single channel. Other potentially disastrous bugs detected in flight tests 15 and 36.

• X29 bug detected by simulation after 162 "at-risk" flights. Analysis showed that the bug could have led to instability and consequent loss-of-aircraft.

• HiMAT crash landed without landing gear due to a design flaw. Traced to timing change in the software that had survived extensive testing.

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Why Formal Methods?

Validation of Ultra-Reliable Systems

Decomposes into two sub-problems:

- 1. Quantification of probability of system failure due to physical failure.
- 2. Establishing that Design Errors are not present.

(Note. Quantification of 2. is infeasible)

Life Testing

Basic Observation:

10-9 probability of failure estimate for a 1 hour mission

Requires

> 109 hours of testing

 $(10^9 \text{ hours} = 114,000 \text{ years})$

Three Basic Approaches to Overcoming the Design Error Problem

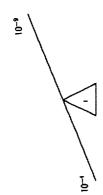
• Testing (Lots of it)

- Design Diversity (i.e. Software Fault-Tolerance: N-version programming, recovery blocks, etc.)
- Fault Avoidance:
- Formal Specification/Verification
- Automatic Program Synthesis
- Reusable Modules

Design Diversity

- 1. Separate Design/Implementation Teams
- 2. Same Specification
- 3. Multiple Versions
- 4. Non-exact Threshold Voters
- 5. Hope design flaws manifest errors independently or nearly

What Enables Ultra-Reliability Quantification For Physical Failure



- The only thing that enables quantification of ultra-reliability for hardware systems with respect to physical failure is the INDEPENDENCE ASSUMPTION.
- The independence assumption has been rejected at the 99% confidence level in several experiments for low reliability software.
- The independence assumption cannot be validated for high reliability software because of the exhorbitant test times remised.

Why is Software² so Hard to get Right?

- In software, there's nothing to go wrong but the design
- Our intuition and experience is with continuous systems but software is about discontinuous behavior
- Have to separately reason about or test millions of sequences of discrete state transitions
- And all the design complexity in modern systems is in the software (VLSI has the same characteristics as software)
- · Complexity exceeds our (unaided) intellectual grasp

Peverything said here applies to digital hardware astwell

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Design Diversity Problem

- If cannot assume independence must measure correlations.
- This is infeasible as well. It requires as much testing time as life-testing the system because the correlations must be in the ultra-reliable region in order for the system to be ultra-reliable.

OS:

- It is not possible to scientifically establish that design diversity achieves ultra-reliability.
- Design diversity creates an "illusion" of ultra-reliability.

within sealble amounts of testing time

Classical vs. Computer Systems

Classical Systems	Computer Systems
continuous state space	discrete state space
smooth transitions	abrupt transitions
finite testing	finite testing inadequate,
and interpolation OK	interpolation unsound
mathematical modeling	prototyping and testing
build to withstand additional stress build to specific assumptions	build to specific assumptions
predictable	surprising

What is Formal Methods?

Applied Mathematics and Engineering

- Established engineering disciplines use applied mathematics
- As a notation for describing systems
- As an analytical tool for calculating and predicting the behavior of systems
- Computers can provide speed and accuracy for the calculations

The Characteristics of Formal Methods

- Specification of system using languages based on mathematical
- Rigorous specification of desired properties as well as implementation details
- Mathematical proof that the implementation meets the desired abstract properties
- Use of semi-automatic theorem provers to ensure the correctness of the proofs

In principle, formal methods can accomplish the equivalent of exhaustive testing, if applied all the way from requirements to implementation

Applied Mathematics and Software Engineering (cont.)

- The applied mathematics of software is formal logic
- Formal Logic can provide
- A notation for describing software designs—formal specification
- A calculus for analyzing and predicting the behavior of systems—formal verification
- Computers can provide speed and accuracy for the calculations

Formal Logic

- Formal means "to do with form"
- Formal logic provides rules for constructing arguments that are sound because of their form, and independent of their mean-
- Example
- That animal is a cat
- All cats are sneaky
- Therefore that animal is sneaky

Formal Methods and Applied Mathematics

- Logic provides the foundation for all mathematics
- But traditional applications of mathematics have been to continuous systems, where highly developed bodies of theory (e.g., aerodynamics) remove practitioners from the elementary logical underpinnings
- But computer systems operate in a discrete domain, their operation is assentially a sequence of decisions, and each application is new
- Therefore have to develop a specific theory about each one, directly in logic

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Proof and Truth

- Logic provides rules of calculation that enable valid conclusions to be deduced from premises
- The calculation is called a proof
- If the premises are true statements about the world, then the soundness theorems of logic guarantee that the conclusion is also a true statement about the world
- Assumptions about the world made explicit, separated from rules of deduction

Formal Methods

Formal Specification: Use of notations derived from formal logic to describe

- assumptions about the world in which a system will operate
 - · requirements that the system is to achieve
- a design to accomplish those requirements

Formal Verification: Use of methods from formal logic to

- analyze specifications for certain forms of consistency, completeness
- prove that the design will satisfy the requirements, given the assumptions
 - prove that a more detailed design implements a more abstract one

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Draft Interim Defense Standard 00-55

Quote from the foreward to the Draft Standard:

The Steering Group "has determined that the current approach which is based on system testing and oversight of the design process will, in the long-term, become cumbersome and inefficient for the assurance of the safety of increasingly sophisticated software".

"The Steering Group therefore proposes the adoption of Formal Dasign Methods, based on rigorous mathematical principles, for the implementation of safety-critical computer software".

Levels of Formal Methods

Level 0: Static Code Analysis (No semantic analysis)

 $Level\ I:$ Specification using mathematical logic or language with a formal semantics (i.e. meaning expressible in logic)

Level 2: Formal Specification + Hand Proofs

Level 3: Formal Specification + Mechanical Proofs

Higher levels of rigor provide greater confidence but at greater cost.

European emphasis: Parta on Level 1, Abead in the transfer of this technology to inclinity.

U.S. emphasis: Fixths on Level 3 the to large National Security Agency finesatment. U.S. aleed in tools for fortual verification.

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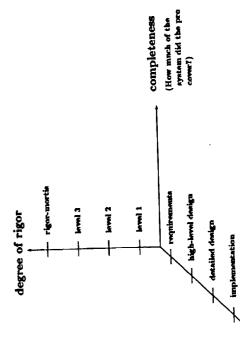
Mathematics of Formal Methods

The mathematics of Formal Methods include:

- predicate calculus (1st order logic)
- recursive function theory
- lambda calculus
- programming language semantics
- discrete mathematics—number theory, abstract algebra, etc.

Domain of Formal Methods

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Phase of life-cycle

The Maturity of An Engineering Discipline

A good measure of the maturity of an engineering discipline is the amount and sophistication of the mathematics routinely used in the design of system within its domain.

- much of hardware design (especially design above the gatelevel) is still ad-hoc.
- almost all software design is ad-hoc. Although there is a significant body of theoretical work, virtually none of it is used in the development of software today. (Exception: use of VDM and Z in Europe)

Formal Specification Example

Ada Procedure

type ARRAYN is stray(POSITIVE ranges O) of INTEGER; procedure SEARCH(A: in ARRAYN; N,X: in INTEGER; Y: ors INTEGER);

English Specification

The procedure searches an array "A" of length "N" for a value "X". If it finds the element, then "Y" is equal to the "index" of the array element that is equal to "X" on exist from the return. If there is no element of the array equal to "X" then the return.

Formal Specification

pre-condition: N > 0post-condition:

 $\{X=A[Y] \land \{1 \leq Y \leq N\} \lor \{(Y=0) \land \{Vk: \{1 \leq k \leq N\} \supset A[k] \neq X\}\}$

With some syntactic belp:

per-condition: N > 0post-condition; IF $(N \in \{1 \le k \le N\} \supset A[k] \neq X\}$ THEN (Y = 0)ELSB X = A[Y] AND $\{1 \le Y \le N\}$

Introduction to the Formal Specification and Verification

Example of Code Verification

function Lookup(var A:array[1..N] of integer; x: integer): 1..N; var i,m, n:1..N; label 11; {1 < N} \wedge arrend(A) \wedge (A[1] \leq x \wedge A[N])} begin m:11; n:= N; {1 < N} \wedge arrend(A) \wedge (A[n] \leq x \wedge A[N])} while m+1 \wedge are noted(A) \wedge (A[m] \leq x \wedge A[n])} while m+1 \wedge and noted(A) \wedge (A[m] \leq x \wedge A[n])} if x < A[i] then m:i is else m:i if x < A[i] then m:i is else m:i if A[i] < x then m:i is else m:i for a and a and a and a are noted(A) \wedge (A[m] \leq x \wedge A[n])} if $A[m] \neq x$ then A[m] = x the

11: end

 $\{(A[Lookup]=x) \lor \{\neg\exists k.(\{1 \leq k \leq N) \land (A[k]=x)\}\}\}$

a der

 $\mathit{Aortcod}(A) = \forall i, j. \{(1 \leq i < j \leq N) \supset (A[i] < A[j])\}$

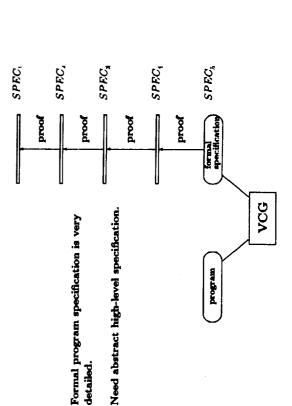
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Verification Conditions

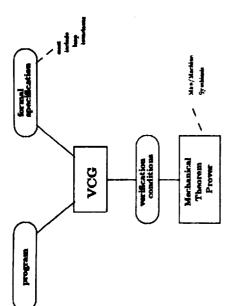
- 1. $\{(1 < N) \land sorted(A) \land (A[1] \le s < A[N])\}$
- $\supset \{(z < N) \land \mathit{norted}(A) \land (A|z] \leq a < A[N]\}\}$
- 2. $\{A[Lockup] = z\} \supset \{A[Lockup] = z\}$
- $3\cdot \left\{(m+1=n) \land \operatorname{aortod}(A) \land (A[m] \le n < A[n]) \land (A[m]=n)\right\} \supset \left\{A[m]=n\right\}$
- 4. (Failure) > (Pailure)
- 5. {(m+1=n) A sorted(A) A (A[m] < n < A[n]) A (A[m] ≠ n)}
- $O\left\{ \neg \exists k. \{(1 \le k \le N) \land (A[k] = \pi)\} \right\}$
- 6. $\{(m < n) \land norted(A) \land (A[m] \le x < A[n]) \land (m+1 < n)\}$
 - $\wedge \{A | \{m+n\} \operatorname{div} z \} \geq \varepsilon) \wedge \{\varepsilon \geq A | \{m+n\} \operatorname{div} z \} \}$
 - $\bigcup \{A_1^{[m+n]} \operatorname{div} z] = z\}$
- 7. $\{(m < n) \land \textit{norted}(A) \land (A[m] \le x < A[n]) \land (m+1 < n)$
 - $\wedge (A[(m+n)\operatorname{div} z] < \varepsilon) \wedge (\varepsilon \geq A[(m+n)\operatorname{div} z])\}$
- $\supset \left\{ \left(\left\{ (m+n) \operatorname{div} z \right\} + z = n \right\} \wedge \operatorname{aorted} \{A \} \wedge \left(A \left\{ (m+n) \operatorname{div} z \right\} \leq x < A [n] \right\} \right\}$
- 8. $\{(m < n) \land sorted(A) \land (A[m] \le x < A[n]) \land (m+1 < n) \land (A[(m+n) \text{ div 2}] < x) \land (x < A[(m+n) \text{ div 2}]) \}$
- $\frac{1}{2} \left(\frac{1}{2} m + n \right) \left(\frac{1}{2} n + n$

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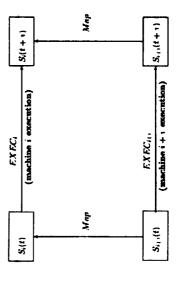
Formal Verification—Hierarchical Approach



Formal Verification (Level 3 Formal Methods)

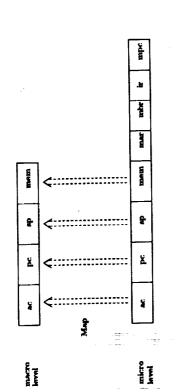


Hierarchical Verification



PROVE: $EXEC(Map(S_{i+1}(t))) = Map(EXEC_{i+1}(S_{i+1}(t)))$

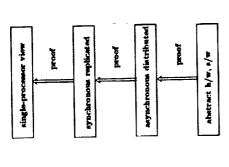
Hardware Example of a Mapping



MICROPROCESSOR instruction-level proof major state machine proof

PAULT-TOLERANT 0.S.

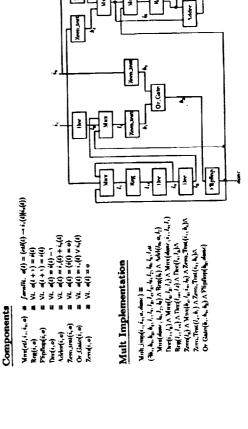
Examples of Proof Hierarchies



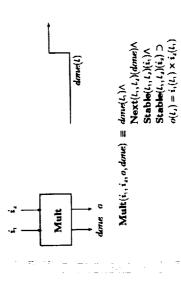
proud

gato-lowi model

Formal Specification of Hardware Implementation



Formal Specification of Hardware (Predicate Style)



 $\begin{aligned} \operatorname{Stable}(\iota_1,\iota_2)(f) &\equiv \forall i. \ \ \iota_i \leq l < \iota_i \supset f(t) = f(\iota_i) \\ \operatorname{Next}(\iota_i,\iota_i)(f) &\equiv \iota_i < \iota_i \wedge f(\iota_i) \wedge (\forall i. \ \ \iota_i < l < \iota_i \supset f(t)) \end{aligned}$

Where

ented the spatistic error production to the character demonstratement

Hardware Verification

MATHEMATICALLY PROVE:

 $\mathbf{Mulk_imp(\hat{s}_1,\hat{s}_2,o,done)}\supset\mathbf{Mulk(\hat{s}_1,\hat{s}_2,o,done)}$

i.e. PROVE

Formal Requirements Specification

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- How do we represent the phone book mathematically?
- 1. a set of ordered pairs of names and number. Adding and deleting entries via set addition and deletion
- 2. function whose domain is all possible names and range is all phone numbers. Adding and deleting entries via modification of function values.
- 3. function whose domain is only names currently in phone book and range is phone numbers. Adding and deleting entries via modification of the function domain and values. (Z style)

Let's start with approach 2.

In traditional mathematical notation, we would write:

Let N = set of names

 $P = \mathbf{set}$ of phone numbers

book: $N \longrightarrow P$

Phone Book Example

Requirements for an electronic phone book

- Phone book shall store the phone numbers of a city
- There shall be easy way to retrieve a phone number given a name
- It shall be possible to add and delete entries from the phone book

Specifying the Book

 $book: N \longrightarrow P$

How do we indicate that we do not have a phone number for all possible names, only for names of real people?

We decide to use a special number, that could never really occur in real life, e.g. 000-0000. We don't have to specify the implemented value of this special number we can just give it a name: $n_0 \in N$.

Now can define an empty phone book. In traditional notation, we would write:

 $emptybook: N \longrightarrow P$

 $emptybook(nm) \equiv n_0$

Accessing an Entry

Let N =set of names

 $P = \mathbf{set}$ of phone numbers

 $book: N \longrightarrow P$

 $n_0 \in N$

 $B = \text{set of functions}: N \longrightarrow P$

FindPhone: $B \times N \longrightarrow P$

FindPhone(bk, name) = bk(name)

Note that FindPhone is a higher-order function since its first argument is a function.

Complete Spec

Let $N = \mathbf{set}$ of names

 $P = \mathbf{set}$ of phone numbers book: N --- P

 $r_{\omega} \in \mathcal{N}$

 $B = \text{set of functions}: N \longrightarrow P$

FindPhone: B × N - P

FindPlune(bk, name) = bk(name)

AddPlume: $B \times N \times P \longrightarrow B$

 $AddPhone(bk,name,num)(x) = \begin{cases} bk(x) & \text{if } x \neq name \end{cases}$

DelPlume: $B \times N \longrightarrow B$

 $DelPhone(bk,name)(x) = \begin{cases} bk(x) & \text{if } x \neq name \\ r_0 & \text{if } x = name \end{cases}$

Can test spec with some putative theorems:

LEMMA (pulative !): Find Phone (Add Phone bk, name, num), name) = num LEMMA (putative 2): $bk(name) = n_0 \supset$

Del Plume (Add Plume (bk, name, num), name) = bk

THE PROPERTY CONTROL OF THE PR

Specifying Adding/Deleting an Entry

Let N = set of names

 $P = \mathbf{set}$ of phone numbers

book: $N \longrightarrow P$

7. E N

 $B = \operatorname{set} \operatorname{of functions}: N \longrightarrow P$

AddPlume: $B \times N \times P \longrightarrow B$

bk(x) if $x \neq name$ num if x = nameAdd Phane(bk, name, num) $(x) = \left\{ \right.$

Del Phone: $B \times N \longrightarrow B$

bk(x) if $x \neq name$ Del Phone(bk, name) $(x) = \left\{ \right.$

Some Realizations

- Our specification does not rule out the possibility of someone having a "no" phone number
 - We have not allowed multiple phone numbers per name
- not the user should be warned if a deletion is requested on · Our specification does not say anything about whether or a name not in the city

HOW DO WE REMEDY THESE DEFICIENCIES?

Deficiency 1

Our specification does not rule out the possibility of someone having a " n_a " phone number:

A SOLUTION:

Let
$$N = \operatorname{set}$$
 of names $V = \{\operatorname{valid}, \operatorname{invalid}\}$ $P = \operatorname{set}$ of phone numbers $P = \operatorname{set}$ of pairs: (P, V) book: $N \longrightarrow P$

$$B = \mathbf{set}$$
 of functions: $N \longrightarrow \mathcal{P}$

Find Phone :
$$B \times N \longrightarrow \mathcal{P}$$

Find Phone(bk, name) = bk(name)
Add Phone : $B \times N \times \mathcal{P} \longrightarrow B$

$$AddPhone(bk, name, num)(x) = \begin{cases} bk(x) & \text{if } x \neq name \\ (num, volid) & \text{if } x = name \end{cases}$$

Del Phone :
$$B \times N \longrightarrow B$$

$$Del Phone (bk, name)(x) = \begin{cases} bk(x) & \text{if } x \neq name \\ (n_0, \text{invalid}) & \text{if } x = name \end{cases}$$

Deficiency 2 (cont.)

Let N= set of names P= set of phone numbers $bank: N\longrightarrow 2^{p}$ P= set of functions: $N\longrightarrow 2^{p}$ $emplybank(name) \equiv \phi$ $FindPhome: <math>R\times N\longrightarrow P$

FindPhone(bk, name) = bk(name)AddPhone: $B \times N \times P \longrightarrow B$

$$AddPhone(bk,name,num)(x) = \begin{cases} bk(x) & \text{if } x \neq name \\ bk(name) \cup \{num\} & \text{if } x = name \end{cases}$$

Del Phone:
$$B \times N \longrightarrow B$$

Del Phone(bk, name) $(x) = \begin{cases} bk(x) & \text{if } x \neq name \\ \phi & \text{if } x = name \end{cases}$

Deficiency 2

We have not allowed multiple phone numbers per name: (THE REQUIRE-MENTS DID NOT SPECIFY WHETHER THIS IS NEEDED OR NOT)

SOLUTION:

Let $N = \operatorname{set}$ of names $P = \operatorname{set} \text{ of phone numbers}$ $\operatorname{book}: N \longrightarrow 2^{p}$ $P = \operatorname{set} \text{ of functions}: N \longrightarrow 2^{p}$

book: P

 $\phi \equiv (name) \equiv \phi$

The empty set ϕ can be used to represent the lack of a phone number for a name. This technique overcomes deficiency 1 as well.

NOTE: 2" is the set of subsets of P.

Deficiency 2 (cont. again)

Del Plume :
$$B \times N \longrightarrow B$$

Del Plume (bk, name) $(x) = \begin{cases} bk(x) & \text{if } x \neq \text{name} \end{cases}$

We notice that the function DelPhune deletes all of the phone numbers associated with a name. Should the system be able to just remove one phone number associated with the name? (REQUIREMENTS DID NOT COVER THIS SITUATION EITHER.) If so, we must define an additional function.

Del PlaneNum :
$$B \times N \times \mathcal{P} \longrightarrow B$$
 if $x \neq name$ $Del PlaneNum(bk, name, num) = \begin{cases} bk(x) & \text{if } x \neq name \end{cases}$

Some Observations

- · Our specification is abstract. The functions are defined over infinite domains.
- As one translates the requirements into mathematics, many things that are usually left out of English specifications are explicitly enumerated.
- The formal process exposes ambiguities and deficiencies in the requirements. Must chose between

book: N --- P

book: $N \longrightarrow 2^p$

 Putative theorem proving and scrutiny reveals deficiencies in the formal specification.

PVS Spec of Phonebook Example

phonebook: TREDRY BEGIN

name: TYPE

ph_number: TYPE name0: name

null_number: ph_number book: TYPE = [name -> ph_number]

nm: VAR name emptybook(nm): ph_number = null_number bk: VAR book

FindPhone(bk, nm): ph_number = bk(nm)

num: VAR ph_number AddPhone(bk, nm, num): book = bk WITH [nm := num]

DelPhone(bk, nm): book = bk WITH (nm := null_number]

END phonebook

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Z Approach

phone' w phone U { name? 1-> number?} phone: IAME --(-> PHOME known = don phone movn: P MAME number?: PHONE name? of known name?: WAVE. -PhoneDB:

Revised Requirements

Original Requirements

- · phone book shall store the phone numbers of a city
- There shall be easy way to retrieve a phone number given a name
- It shall be possible to add and delete entries from the phone book

Revised Requirements

- · For each name in the city, a set of phone numbers shall be stored
 - . There shall be easy way to retrieve the phone numbers given a name (SHOULD WE LIMIT THE NUMBER?)
 - It shall be possible to add a new name and phone number.
- It shall be possible to add new phone numbers to an existing name.
 - It shall be possible to delete a name
- It shall be possible to delete one of several phone numbers associated

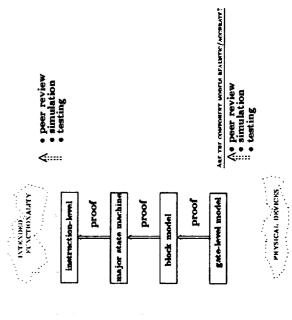
with a name.

- the user shall be warned if a deletion is requested on a name not in the
- the user should be warned if a deletion of a non-existent phone number is requested

Some More Observations

- There are many different ways to formally specify
- No matter what representation you chose you are making some decisions that bias the implementation
- The goal is to minimize this bias and yet be complete
- The process of formalizing the requirements can reveal problems and deficiencies and lead to a better English requirements document as well

Illustration of Limitations



Limitations of Formal Methods

Myth

A formally verified system will be perfect.

3

Reality

Formal verification finds bugs other methods can't reach.

(But other methods (e.g. testing) find bugs outside of the scope of formal verification)

The bottom line

Any validation is only as good as the model.

Simulators use operational models.

Formal verification can also use axiomatic models

1 4 4

What Makes a Technique a "Formal Method?"

FORMAL METHOD = LOGIC + CS language concepts

Important Attributes:

- logic based (e.g. \forall , \exists , \supset stuff)
- CS language concepts (e.g. data types, module-structure, generics)
- should be able to express what is done without saying how it is done (i.e. non-procedural)
- formal semantics
- · feasible to build useful tools which support analysis

Expressibility Vs. Proving Efficiency

There is a trade-off between the expressiveness of the specification language and the difficulty of building a theorem prover.

- propositional calculus (truth table is a decision procedure)
 - predicate calculus (semi-decidable via resolution)
- recursive function theory (undecidable)
- higher order logic (undecidable)



· no theorem prover available

Tutorial Design Specification Techniques

 $\underset{\mathrm{ViGYAN}}{\mathrm{Ben~DiVito}}$

Tutorial on Design Specification Techniques

Ben L. Di Vito

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August 11, 1992

Formal Specification Concepts

Requirements specification or high level design for many classes of (sub)systems can be represented using state machine models:

- We introduce an abstract representation of system state
- -It may require building up a suitable collection of type definitions
- Additional types, constants, and functions are introduced as needed to support subsequent formalization
 - We specify a set of upralivas or system services that can be invoked by users of the system across an appropriate interface
 - Operations may have input and output parameters
- Operations may cause the system state to be updated
- -Operations may have pre-conditions that must be satisfied for legitimate invocation
- Operations have post-conditions that express the net effect of executing or performing the operation

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• Formal specification concepts

- Statement of example problem
- Definition of system state
- · State invariant
- Operation specifications
- Maintaining the invariant
- Specification properties
- Hierarchical specification and verification

Specification Concepts (Cont'd)

- We may attach an invariant to the system state to formalize our notions of well-definedness
 - Operations should be shown to maintain the invariant after every invo-
- Desired properties may be expressed as predicates involving the system state and operations, and proved as putuive theorems that follow from the formalization
 - The formal specification may be used as one layer of a hierarchical specification and verification structure

Statement of Example Problem

We wish to specify an automated airline seat assignment system that meets the following requirements:

- The system shall execute seat assignment transactions for any scheduled airline flight on behalf of passengers or their agents.
- The system shall establish and maintain a centralized database of seat assiruments.
- 3. The system shall support a fleet having different aircraft types.
- 4. Seats shall be assigned to individual passengers in order of arrival.
- Passengers shall be allowed to specify preferences for seat type (e.g., window or aisle).
- 6. Seats shall be filled in front-to-back, left-to-right order.
- 7. Rows and seats shall be designated using a numeric index (one-based).
- 8. The system shall provide the following operations or transactions:
- Make a new seat assignment
- · Cancel an existing seat assignment

Definition of System State

For each flight f in the system database, we record a set of seat assignments

- Each seat assignment is a triple (r, s, p) for row r, seat s, and passenger p
 The system state is a mapping from flight identifier into that flight's
- · Initially, each flight has no assignments

current set of seat assignments

seat_assignment: TYPE = RECORD row: row, seat; seat, pass: passenger EMD

flight_assignments: TYPE = set[seat_assignment]

assn_state: TYPE = function[flight -> flight_assignments]

initial_state: function[flight -> flight_assignments] =
 (LAMBDA flt: emptyset[seat_assignment])

Basic Type Declarations

FHDM type declarations of our basic data items:

nrows: nat (* Max number of rows *)

neests: nat (* Max number of seats per row *)

n: VAR nat

row: TYPE FROM mat VITE (LAMEDA n: 1 <= n AED n <= mrows)

seat: TYPE FROM nat WITH (LAMBDA n: 1 <= n AND n <= neests)

flight: TYPE (* Flight identifier/descriptor *)

plane: TYPE (* Aircraft type *)

preference: TYPE (* Seat preference *)

passenger: TYPE (* Passenger identifier *)

Aircraft Seat Layout

We assume a simple two-dimensional representation for airplane seating

Accommodates a maximum number of rows and seats per row

 Requires us to indicate whether a (row, seat) pair exists for a given aircraft type

Support Functions

We assume several uninterpreted functions to answer questions about our sircraft

```
seat_exists: function[plane, row, seat -> bool]
meets_pref: function[plane, row, seat, preference -> bool]
aircraft: function[flight -> plane]
```

We need to express the condition that there are no available seats up to the point (r,s) in the aircraft meeting the passenger's preference

Specifying Operations

Our method of formally specifying operations is based on a relational tech-

- We use a relation to express the post-condition under which a state transition is allowable
- The predicate relates the value of system state kefore the operation is invoked to the value of system state after invocation
 - The condition only constrains allowable behavior; it does not prescribe it

If S_i and S_i are the state values before and after executing the operation, then the relations representing post-conditions have the form:

operation spec $(P_1, \ldots, P_n, S_i, S_i)$

where P_1, \ldots, P_n denote the parameters at the operation interface (additional conventions are needed for return values, exceptions, etc.)

A rest of the section of the section

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State Invariant

The system state is subject to two types of anomalies:

- 1. Assigning nonexistent seats to passengers
- 2. Assigning multiple seats to a single passenger

```
Prevention of (1) can be formalized as follows:

\( \text{ } a_{\text{o}} f l : a \) \( \text{ } a_{\text{o}} f l \) \) \( \text{ } a_{\text{o}} f l \) \) \( \text{ } a_{\text{o}} f l \) \( \text{ } a_{\text{o}} f l \) \) \( \text{ } a_{\text{o}} f l \) \) \( \text{IMPLIES} \)

\( \text{ } (\text{LARBDA as: (FURALL a, flt: member(a, as(flt)) IMPLIES} \)

\( \text{ } (\text{LARBDA as: (FURALL a, flt: member(a, as(flt)) a.row, a.seat)} \) \)

Prevention of (2) can be formalized as follows:

\( \text{ } \text{ } a_{\text{o}} f l \) \( \text{ } \text{ } a_{\text{o}} f l \) \( \text{ } \text{ } a_{\text{o}} f l \)

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Seat Assignment Operations

(LAMBDA as: existence(as) AND uniqueness(as).)

The first operation is cared assa(fll., pass), which cancels the seat assignment for passenger pass on flight fll:

The specification is split into two cases:

- 1. All seat assignment sets for flights other than /u are unchanged.
- 3. For flight $f\mu$, all assignments on behalf of passenger p_{nss} are removed (there should be at most one).

Seat Assignment Operations (Cont'd)

ment, if possible, for passenger pass on flight fit, returning a boolean value The second operation is make zern (flt, pass, pref), which makes a seat assignindicating whether a seat was available:

```
(LET a := (REC row := r, seat := s, pass := pass) IN
                                                                                                                                                                                                                                                                                                                            S2 = S1 VITH [(flt) := add(a, S1(flt))])
                                           assm_state, assm_state, bool -> bool] =
                                                                                                                                                                                                                                                                                                                                                                                                                        AMD MOT pref_filled(S1, flt, r, s, pref)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                AMD pref_filled(S2, flt, r, s, pref)))
                                                                                                                                                                                                                                                                                                                                                                             AMD seat_exists(aircraft(flt), r, s)
make_assn: function[flight, passenger, preference,
                                                                                                                       IF pref_filled(S1, flt, mrows, nseats, pref)
                                                                               (LAMBDA flt, pass, pref, S1, S2, avail:
                                                                                                                                                                  THE avail - false AND S2 - S1
                                                                                                                                                                                                       ELSE avail = true AND
                                                                                                                                                                                                                                                     (EXISTS r,s:
```

The specification is again split into two cases:

- 1. If no seats are available meeting the passenger's preference, no assignment is made and the state remains unchanged.
- 2. Otherwise, an assignment is made by adding a triple for the first seat satisfying the stated preference to the assignment set for flight /11.

Proof that First Operation Maintains Invariant

We sketch below a proof that the cancelasm operation maintains the state invariant assaimaniant.

1. We begin with the original conjecture:

assn_invariant($S1) \land \mathsf{cancel_assn}(fll,pans,S1,S2) \supset \mathsf{assn_invariant}(S2)$

2. Next, we expand the invariant predicate and split into two cases. First, we prove the existence case.

existence(S1) \land cancel assn(fU, pass, S1, S2) \supset existence(S2)

3. Expanding the predicates yields:

```
THEN (Y a: a \in S_2(fu) IFF (a \in S_1(fu) \land a, pass \neq pass))
(\forall \ a, f \mathcal{U} : a \in S1(f \mathcal{U}) \supset \text{seat.exists}(\text{aircraft}(f \mathcal{U}), a.row, a.seat)) \land \\
                                                                                                                                                                                                                                                                                                                           (\forall \ a, f \mathcal{U} : a \in S2(f \mathcal{U}) \supset \mathsf{seat.exists}(\mathsf{aircraft}(f \mathcal{U}), \mathsf{a.row}, \mathsf{a.seat}))
                                                                                                                                                                                       ELSE\ S_2(f) = S_1(f)
                                                             (\forall f: IF f = flt)
                                                                                                                                                                                                                                                                       \cap
```

Maintaining the Invariant

To establish that the state invariant is preserved by every operation, we must prove theorems of the form:

 $I(S_i) \land op_{-spec}(...) \supset I(S_i)$

where S_i and S_i are the before and after values of system state, and I represents the state invariant.

For our example, the required theorems can be expressed as follows:

cancel_assn_inv: LEMMA assn_invariant(S1) AED cancel_assn(flt,pass,S1, IMPLIES asem_invariant(S2)

```
AMD make_assn(flt,pass,pref,S1,S2,avail)
                                                                             IMPLIES asen_invariant(S2)
make_assn_inv: LEMMA assn_invariant(S1)
```

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Proof (Cont'd)

4. Consider two cases. If $f \neq f l l$, then $S_2(f) = S_1(f)$ and hence $a \in S_2(f l l)$ is equivalent to $a \in S_1(fl)$ from which the conclusion follows. Otherwise, we obtain:

```
(\forall \ a, f u: (a \in S1(f u) \land a.pass \neq prant) \supset seat.exists(sincraft(f u), a.row, a.seat))
(\forall \ a, f \mathcal{U}: a \in S1(f\mathcal{U}) \supset \mathsf{seat.exists}(\mathsf{aircraft}(f\mathcal{U}), a.\mathsf{row}, a.\mathsf{seat}))
                                                                                                                    Λ
```

5. After rewriting to the form:

```
(a \in S1(JU) \supset \text{seat.exists}(\text{aircraft}(JU), a.row, a.seat))
(a \in S_1(JU) \land a.pass \neq pans) \land
```

seat_exists(aircraft(fu), a.row, a.seat)

we see that the conclusion follows.

uniqueness(S1) \land cancel assn(fu, pans, S1, S2) \supset uniqueness(S2) 6. Returning to the uniqueness case, we must establish:

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Proof (Cont'd)

7. This produces:

```
(\forall a,b,fll:a\in S\iota(fll)\land b\in S\iota(fll)\land a.pass=b.pass\supset a=b)\land (\forall f:IFf=fll) (\forall f:IFf=fll) THEN\ (\forall a:a\in S\iota(fll)\ IFF\ (a\in S\iota(fll)\land a.pass\neq paxs)) EISE\ S\iota(f))
```

 $(\forall a,b,f u: a \in S_2(f u) \land b \in S_2(f u) \land a.pass = b.pass \supset a = b)$

8. Again, consider two cases. If $f \neq fll$, then $S_2(f) = S_1(f)$ and hence $a \in S_2(fll)$ is equivalent to $a \in S_1(fll)$ and $b \in S_2(fll)$ is equivalent to $b \in S_1(fll)$ from which the conclusion follows. Otherwise, we obtain:

9. Simplifying as before will establish that a=b.

1.1

Hierarchical Specification and Verification

- · We have specified only one layer of design in a hierarchy
- A next step might be to refine the specification into a more detailed, lower level description, e.g., in terms of more concrete data structures and operations
- It would then be possible to prove that the lower level specification correctly implements the upper level one
- Such an activity would constitute a design proof
- This can be carried out across several layers of a design hierarchy
- The process may stop at some point because further refinement of the formalism is no long cost-effective, but the high level specifications and proofs are still valuable

System Properties

Usually there are several types of system properties that are of interest to formalize and prove:

- Properties about critical system operation derived from high level requirements
- 2. Putative theorems used to confirm our understanding of the specified sys-

An example of (2) is the property that if the system is in state S_i , and we make a seat assignment and then immediately cancel it, we should return to the same system state:

make_cancel: LEWMA make_assn(flt,pass,pref,S1,S2,avail)
AND cancel_assn(flt,pass,S2,S3)
IMPLIES S1 = S3

Summary

5

A simple design problem was postulated and formally specified using $\mathsf{E}\mathsf{H}\mathsf{D}\mathsf{M}$

- System state and supporting types formalized
- State invariant formalized
- Operations specified
- · Operations shown to maintain state invariant
- Hierarchical specification techniques outlined

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Tutorial Code Verification Techniques

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Tutorial on Code Verification Techniques

C. Michael Holloway NASA Langley Research Center 11 August 1992

Formal Code Verification

Formal methods allow us to address the code correctness problem analytically instead of empirically:

- Software systems are treated as as mathematical objects, which allows reasoning about them
- Specifications are expressed precisely in an unambiguous notation
- Proofs are constructed to demonstrate that specifications are met for all values of input domain

Proof method replaces test cases by a static analysis – theoretically

achieves the effect of exhaustive testing.

• Proofs are not limited to functional correctness: any system property (for example, safety or security) that can be specified can also

Outline

- Some benefits of formal code verification
- The general method for verifying code
- A specific example verification
- How the process is mechanized

Method of Proof

- 1. Introduce assertions to characterize key program states.
- Analyze execution path structure path begins and ends with assertions.
- 3. Show that if each path begins with its initial assertion true, and execution reaches the end of the path, its final assertion is true.

(Initial assertion)

A Conditions under which path is taken

{Final assertion under variable substitutions due to assignments}

Method of Proof (continued)

• The method of *inductive assertions* requires that each loop is cut by a *loop invariant* – achieves proof by induction.

Software Example: Linear Search Formal Specification

Let y denote the function return value:

Pre-condition: $|A| \ge 0$

Post-condition:

 $(1 \le y \le |A| \land x = A[y] \land (\forall k (1 \le k < y) \supset A[k] \ne x))$

 $(y = 0 \land (\forall k (1 \le k \le |A|) \supset A[k] \ne x))$

Software Example: Linear Search English Specification

The function searches an integer array "A" looking for a value "X". If the value is found, then the function returns the index of the array element that is equal to "X"; otherwise the function returns "0".

Software Example: Linear Search

Ada Code

Verification Conditions and Proof

Path 2 $||A|| \ge 0$ $||A|| \le ||A|| \wedge 1 \ge 1 \wedge (\forall k (1 \le k < 1)) > 4[k] \ne x)$

Path 3 $1 \le i \le |A| \land (\forall k \ (1 \le k < i)) \supset A|k] \ne x) \land x = A[i]$ $\bigcup_{1 \le i \le |A| \land x = A[i] \land (\forall k \ (1 \le k < i)) \supset A|k] \ne x) \quad \checkmark$

Execution Path Analysis

The following paths must be considered:

1. A → C: Never entering the loop

2. A → B: Initial entry into loop

3. $\mathbf{B} \to \mathbf{D}$: Exit from loop because item is found

4. $\mathbf{B} \to \mathbf{C}$: Exit from loop because i > |A| (item not found)

5. B → B: Another iteration through the loop

Verification Conditions and Proof (continued)

4

 $1 \le i \le |A| \wedge (\forall k \ (1 \le k < i)) \land |A| | \ne x) \land x \ne |A| \land i + 1 > |A|$ $0 = 0 \wedge (\forall k \ (1 \le k \le |A|) \supset |A| k | \ne x)$ simplifying yields $i = |A| \wedge (\forall k \ (1 \le k \le i)) \land |A| \ne x)$

Path 5

 $1 \le i \le |A| \land (Ak (1 \le k < i)) \land Ak| \ne i) \land x \ne Ak| \land i > 1 | \le |A| \land i + 1 \le |A|$ 0 $1 \le i + 1 \le |A| \land (Ak (1 \le k < i + 1)) \land Ak| \ne x)$

 $\forall k \ (1 \le k \le \lfloor A \rfloor) \supset A[k] \neq x$

Q.E.D.

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Notes on the Proof

- We have shown partial correctness: for all input values that meet the pre-condition, the function returns the correct value if it terminates
- We have not shown total correctness: that the function is partially correct and that it terminates
- Demonstrating termination is a separate issue, which requires a slightly different proof technique
- For the example program, showing termination informally is simple

13

Mechanizing the Process (continued)

- Important trade-offs exist
- Specification languages/logics should be expressive to allow formalization of realistic problems
- More expressive languages complicate and slow down mechanical theorem proving

Mechanizing the Process

- Machine-readable specification languages are widely available.
- Verification condition generation is readily automated
- Assertions must be supplied by human analyst
- Correctness problem converted to theorem proving problem
- Theorem proving is partially automated

7

Mechanical Theorem Provers

- Provide more reliable proofs than hand methods
- Theorems shallow but numerous
- Contain substantial detail, much of it irrelevant
- Provide benefits of automation
- Discovering proofs
- Storing and replaying proofs
- Accumulating deductive knowledge

Mechanical Theorem Provers (continued)

- Two general types
- Automatic: Attempt proofs without human intervention (expensive in machine resources)
- Interactive: Require user direction in proof process (expensive in human resources)
- Primary limitation is provers' lack of "education"

Concluding Remarks

- We have discussed the basic ideas of code verification
- Possible benefits
- Simple example
- Mechanization
- You will not hear much more about code verification during this workshop

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The FAA DFCS Handbook Formal Methods Chapter

John Rushby SRI International

NASA Peer Review and Workshop, August 1992

FAA Digital Systems Validation Handbook Formal Methods Chapter

John Rushby

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FAA Chapter

How Airplanes Get Certifled

• The certification authority establishes the certification basis in consultation with the applicant

- Certification basis is the baseline of regulations with which the applicant must show compliance
- If existing regulations are not adequate, may apply special conditions for new and novel technologies and methods
- Applicant proposes Means Of Compliance (MOC) and associated Plan for Software Aspects of Certification

How Airplanes Get Certifled (ctd)

- certification authority reports any problems with MOC; iterate Based on System Safety Assessment and other lifecycle data, until satisfied
- software, complies with certification basis; done by evaluating lifecycle processes and products against the Plan; evaluations may occur at any time during lifecycle; may involve on-site Certification authority determines that system, including evaluations, witnessing of lifecycle processes

FAA Chapter

FAA Chapter

DO-178B (ED-12)

- . "Software Considerations in Airborne Systems and Equipment Certification" (Draft 6)
- Major revision to DO-178A
- Produced by Requirements and Technical Concepts for Aviation and EUROCAE WG-12
- Industry-accepted guidelines for meeting certification requirements
- Based on very formalized software development process; extensive documentation, reviews and analyses of the products of each lifecycle process
- Formal methods included among "alternative methods"

FAA Chapter

FAA Formal Methods Chapter

- The chapter is not
- A primer on formal methods
- A prescription for using formal methods (cf. UK 00-55 or US "Orange Book" for Computer Security)
- An endorsement of specific methods or tools
- Finished (but is very nearly so)
- The chapter is
- A very detailed exposition of issues in application of formal methods to critical systems
- Addressed to an audience wider than certifiers (developers, managers, engineers)

F/4

FAA Chapter

FAA Formal Methods Chapter

- A chapter on Formal Methods for the FAA Digital Systems Validation Handbook (a guide to certifiers)
- Sponsored by FAA Technical Center, Atlantic City
- Explains technical basis for formal methods
- Their use in specification and verification of software and hardware requirements, designs, and implementations
- Identifies benefits, weaknesses, difficulties
- Suggests factors for consideration when formal methods are offered in support of certification (cf. DO-178B)

FAA Chapter

Appendices

- Introduction to formal logic (up through set theory and higher-order logic)
- Examples
- Code verification (square root)
- Hardware verification (full adder)
- Abstract data type and its implementation (stack)
- Design-level modelization (library)
- Algorithm (Oral Messages algorithm for Interactive Consistency)

FAA Chapter

Extent of Application of Formal Methods

- Cannot (and need not) apply formal methods everywhere
- Four axes of selectivity:
- Components
- Properties
- Lifecycle phases
- Levels of rigor

FAA Chapter

58

Selected System Properties

- May not need to verify all functional properties
- Often, absence of specific malfunctions is most important property
- May be able to deal with these by fault-tree analyses and other techniques derived from system safety engineering; these can be done formally, but are different from conventional formal methods

FAA Chapter

10

Selected System Components

- Hazard analysis, system failure severity, and software criticality levels
- FAA failure effect severities: catastrophic (10⁻⁹ per hour), hazardous/severe-major, major, minor, no effect
- Must consider malfunction and unintended function as well as loss of function
- DO-178B assigns software criticality levels A through E according to maximum failure severity
- May be able to lower criticality levels of large bodies of software by providing components that limit consequences of failure
- Partitioning (fault containment)
- Monitoring
- Centralized redundancy management

FAA Chapter

Lifecycle Phases

- Pros and cons of applying formal methods in early and late lifecycle phases
- Late lifecycle

Pro: That's what runs

Con: Size of description is large; must often leave purely functional world of ordinary logic (i.e., need VCGs, Hoare sentences); traditional methods are very effective

Early lifecycle

Pro: That's where the serious errors are; that's where the concern is; few other rigorous techniques available

Con: front-loads development time and cost

Levels of Formal Methods

- 0. No use of formal methods
- 1. Use the ideas of formal methods, but ad-hoc notation, proofs based on informal argument, tools are pencil and eraser (the way conventional mathematics is done)
- 2. Formalize and maybe mechanize specification language and methodology, retain pencil and eraser for proofs
- 3. Full mechanization with automated theorem proving or checking

FAA Chapter

59

17

Benefits of Formal Methods

- Precise, unambiguous specifications, force early attention to
- Notions of completeness
- Ability to do validation early in lifecycle
- Proofs reveal assumptions
- And errors—tool of discovery, not just of certification
- Lead to improved understanding of possible system behaviors; allow it to be documented
- Guarantees?

FAA Chapter

Validation of Specifications

- How do you gain confidence that your specifications are right?
- Internal consistency
- Strong typechecking
- Definitional principle
- Exhibition of models
- Modules and parameters
- External fidelity
- Review
- o Analysis ("challenges")

FAA Chapter

13

Fallibilities of Formal Methods

- Naur's position
- DeMillo, Lipton and Perlis' position
- Fetzer's position

Formal Methods and Tools

Some Successful Applications of Formal Methods

- Traditions and styles of tools
- Design issues and tradeoffs
- Language issues
- Support for theorem proving lifecycle

Secure systems

Tektronix

• CICS

• SACEM

Soundness

FAA Chapter

16

FAA Chapter

11

Summary

- Not an introduction to formal methods
- A comprehensive, detailed, but accessible discussion of issues concerning formal methods in support of critical systems certification

all possible system behaviors: formal methods allows; you write

that understanding down and subject it to analysis

Formal methods expand design space for "confident

understanding"

"Engineering judgment" relies on confident understanding of

The impossibility of quantification

Formal Methods and Certification

- Reasonably nonpartisan
- Should be of use to developers as well as certifiers, and to other domains than aircraft
- Available for review in a couple of weeks

FAA Chapter

Commentary on DO-178B (formal methods allow analysis to

replace or supplement reviews)

Relation to "Design For Validation"

18

FAA Chapter

19

Survey of State-of-Practice Formal Methods in Industry

Dan Craigan ORA Canada

Overview of Presentation

Survey of State-of-Practice: Formal Methods in Industry

Dan Craigen ORA Canada

dan@ora.on.ca

NASA Langley, Virginia 11 August 1992

- Purpose, sponsors and researchers.
- Method for conducting survey.
- Cases: An overview.
- Example case: TCAS.
- Example feature: Tools.
- Observations.

· A A 接触的 (Procedure Consideration Consider

1

2

Purpose, sponsors and researchers

- To provide an authoritative record on the practical experience to date.
- To better inform industry and government bodies developing standards and regulations.
- To provide pointers to future research and technology transfer needs.
- Value added: Case studies and analysis.

Purpose, sponsors and researchers

- AECB, NIST, NRL.
- Dan Craigen, Susan Gerhart, Ted Ralston.

Method for Conducting Survey

Questionnaires

- Initial questionnaire and structured interview.
- Organizational context.
- Project content and history.
- Application goals.
- Formal methods factors.
- Formal methods and tool usage.
- Results.

5

Method for Conducting Survey

Product Features

- Client satisfaction.
- Cost.
- Impact of product.
- Quality.
- Time-to-market.

Method for Conducting Survey

Method for Conducting Survey Process

• Structured interviews (Second questionnaire).

• Raw notes, case report, review.

• Initial questionnaire.

Literature review.

Review committee.

Analytic framework

- Product features.
- Process features.
- FM R&D summary.
- Key events and timing.

Method for Conducting Survey

Process Features

Method for Conducting Survey

Process Features

- Cost.
- Impact of process.
- Pedagogical.
- Tools.

- Design.
- Developing reusable components.
- Using existing reusable components.
- Maintainability.
- Requirements capture.
- V&V.

10

Method for Conducting Survey

FM R&D Summary

- Methods: specification; design and implementation; validation and verification. [uses]
- Tools: language processors; automated reasoning; other tools. [tools]
- Recommendations to FM community. [needs]

Method for Conducting Survey

Key Events and Timing

- Starter.
- Booster.
- Status.

Cases: An Overview

• CASE

- SSADM toolset; commercial; Z.
- 340pgs Z/English; 550 schemas;
 37KLOC obj. C; 16.5 lines/day

• CICS

- Transaction processing; commercial; Z;
 PS/2 tools.
- 268KLOC new/modified code;
 50KLOC traced to Z specs;
 9% improvement in cost;
 60% reduction in APARS.

13

Cases: An Overview

LaCoS

- Engine management and a distributed controller; ESPRIT and commercial;
 Raise [Method].
- Multinet Gateway
 - Network security; NCSC; GVE, etc.
 - 10pgs math; 80pgs Gypsy; 6KLOC OS.

SACEM

- Automatic train protection system; safety critical and RER; B, Hoare triples; B tool.
- 9KLOC verified code; Total of 315,000 person hours.

Cleanroom

 COBOL structuring and Attitude control; commercial and government; functional specs. and testing. [Method]

Cases: An Overview

- 80KLOC; (20KLOC reused; 18KLOC changed; 34KLOC new)
- 34 lines/day; error rate of 3.4/KLOC
 (1/20th industry average).

Darlington

- Shutdown system; regulatory; A-7 style and program function tables.
- SDS1: 1362LOC Fortran; 1185LOC Assembler

SDS2: 13KLOC Pascal (??).

14

Cases: An Overview

TBACS

- Smartcard security application; security; FDM.
- 300 lines of FDM; 2500lines of C.
- Tektronix (oscilloscope)
 - Reusable software architecture; commercial;
 Z; Fuzz.
 - 200KLOC of code; 15pgs of Z specs (twice).

• TCAS

- CAS Logic and surveillance; regulatory; state charts with DNF tables.
- 7KLOC of pseudocode; specs about the same size.

Cases: An Overview

- Transputer
 - T-800 FPU, VCP; commercial; Z, HOL, mathematics.
 - FPU: 100pgs Z; 4KLOC Occam; VCP about 10⁶ states.
- HP-AIB
 - real-time data-base; commercial; HP-SL.
 - 55pgs HP-SL; 1290 lines of spec and design;
 4390 lines of code.

17

TCAS

- Players: RTCA Inc. (SC 147), FAA, UC Irvine, Mitre, Lincoln Labs.
- Interview profile: Leveson, Nivert, Lubkowski, White.
- CAS Logic and surveillance system.
 - 7 KLOC pseudocode.
 - 700 pages English description. [Terminated]
 - Loss of intellectual control.

Example case: TCAS

• Traffic Alert and Collision Avoidance System.

- TCAS I, II, III.
- Congressional fiat (1993).
- Grand Canyon collision.
- Time span from early 80s. Leveson in June 1990.

14

TCAS

- FM for safety analysis. [model checking and automated deduction]
- Statecharts.
- DNF tables for conditions.
- Iteration on notation.
- Strong support from SC 147 and industry.
- Currently at IV&V [15 pys over 8 months].

Product features

Client satisfaction	ł
Cost	n/a
Impact of product	n/a
Quality	n/a
Time to market	n/a

General process features

Cost	n/a
Impact of process	+
Pedagogical	+
Tools	n/a

Specific process features

Design	+
Developing r. comp.	n/a
Reusing r. comp.	n/a
Maintainability	n/a
Regts. capture	+
V&V	n/a

TCAS (Key Events)

- Starter: FAA seeking better rqts. for deployed and troublesome system; Leveson looking for demo project.
- Booster: SC 147 willing to accept new approach; Readable notation.
- Status: CAS Logic formalism and pseudocode in IVV. Surveillance logic current.

21

TCAS (R&D)

TCAS (R&D)

- Uses: Mod. to Statecharts
 - Concurrency as parallel state machines.
 - Tabular notation.
 - Specs. reviewable and IV&V.
 - CAS Logic from pseudocode and English.

- Tools: LaTeX.
- Needs:
 - Safety analysis tool.
 - Automated deduction and model checking.
 - Well-formedness checker.
 - Foundational issues.
- Conclusions: successful transition and application.

Tools (Usage)

- CASE (S\$ADM): Prototype Z parser and typechecker.
- CICS: PS/2 based toolsuite w/ editor, typechecker, semantic analyser (Z).
- Cleanroom: Editors, waste paper basket.
- Darlington: Microsoft Excel.
- LaCoS: Raise toolset.
- Multinet: GVE, Extractor.

25

Tools (Needs)

- CASE (SSADM): schema expander, enhanced editor, browsing and X-ref.
- CICS: schema expander, semantic analyzer (for all Z), configuration management.
- Cleanroom: Extracting and tracking verification events.
- Darlington: automated deduction, POG, bookkeeping.
- LaCoS: Experience with automated reasoning tools.

Tools (Usage)

• SACEM: B.

- TBACS: FDM, scrolling, pencil and paper Xref.
- Tektronix: Fuzz editor, typechecker and pretty printer.
- TCAS: LaTeX.
- Transputer: Occam transformation system, inhouse refinement checker.
- HP: HP-SL syntax checker.

26

Tools (Needs)

- Multinet: Better automated deduction, improvements for industrial scale, soundness, better notation.
- SACEM: Better integration with other V&V.
- TBACS: Better interface; large expressions and many proof steps.

Tools (Analysis)

Did the formal methods tools help or hinder the development of the product? Were the tools reliable?

CA CI CL DA LA MG SA TB TE TC TR HP
- + 0 n/a 0 0 + + - n/a + 0

- Not a large role (lack of tool support).
- Problems due to newness and primitiveness.
- Need for language checkers, bookkeeping.
- Don't be too ambitious.
- Automated deduction in critical applications.

30

Tools (Needs)

- Tektronix: schema expander, refinement proof tool, pre-condition calculator.
- TCAS: safety analysis tool, automated deduction, language checker, soundness.
- Transputer: refinement checker for large state spaces.
- HP: Language checker and better notation (not ambitious!).

Observations Features:

- Definite positive influence on design, requirements, V&V, and pedagogical.
- Positive influence on 'impact on process' and quality.
- Neutral on cost.

Observations Formal methods

- Methods: state machine; 1st-order predicate calculus; reviewability; complete refinement.
- Tools: Language processors; bookkeeping; browsing; x-ref.
- Needs: Integration with other V&V; concurrency and timing; lower barriers of entry.

Availability of Report

- Availability within 2-3 months.
- Send email to dan@ora.on.ca, or mail to:

Dan Craigen ORA Canada 265 Carling Avenue, Suite 506 Ottawa, Ontario K1S 2E1 Canada

Formal Modelisation

Susan Gerhart National Science Foundation

Modelisation

Sure you've proved it correct,

but what does the system REALLY do?

Susan L. Gerhart sgerhart@nsf.gov

Subjects:

The SACEM Case (continued from Dan Craigen's presentation)--how FM was embedded in an industrial process

Issues of "modelisation"

Software Engineering for a "Formal Methodist"

Background Point of View

SACEM: Train control for the Paris Metro

The Job:

Shorten the train intervals to 2 minutes to avoid a new Paris line and Convince the Paris Transit Authority the system was safe plus Build up an international business in safe train control systems

Who

GEC Alsthom/Matra/CSEE + Paris Transit Authority

The Process:

1970s Decided had to go with new software and hardware

Explored fault tolerance, discovered proof of correctness techniques, did safety studies

1980s Duilt prototypes verified code one way, found new way to specify and verify, worked with authorities to demonstrate safety, brought on-line

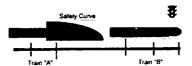
1990s demonstrated capability on other systems, commorcializing tools used in the process

The Results:

Ventication was demonstrated as an addition to simulation, without excess cost and with significant added assurance.

Specification and modelisation matured and an industrial process was defined.

SACEM System



Challenges

- Different kinds of "rolling stock" to detect, some protected and some not
- Variations in track-beacon technology, tunnels & rivers,
- Getting the train "home" when it's system does fail
- Encoded single-processor (rather than complex synchronized multi-processor) -- as fail-sale as possible

SACEM lessons for Formal Methods

An industrial process has been put in place that is evolving

Understood and documented

Measured and predictable

Regarded as cost effective

Tool supported

Probably comparable to MoD 0055

Many techniques can play together, (although not in concert yet)

SADT for graphical system decomposition and analysis

FSM (Graphcet) simulator

Hazard analysis

Operational scenarios (600 of them)

Real-time design simulation

Prototyped system

Code verification & specification refinement

Technology Transfer problems could be overcome

A manager understood and stuck with it

The customer was educated (and did their own thing)

Proving could be credibly compromised

Modelisation will help synthesize their results

Modellsation

The process of getting all the stakeholders to understand and agree that the working description conveys the intended system. Subsumes requirements analysis, methods itself and bling all. mathematical modeling, etc.

in SACEM.

Tracks, trains, beacons, encoded mproc, ...

Salety principles

The description notation itself

The process of using the description

Problems encountered with modelisation in SACEM:

Laborious code description disconnected from "the theorem"

Concurrency difficult to express in top level model

Different representations, different analyses were used for assurance (see tools list)

Many kinds of system views: certiflur, railway switching, microprocessor developer, formal verifler

Relinements were OK, but there was a code gap (now generated)

SACEM Background

maintained sp	ec outermost guided by design vvvv relined down vvvv until too detailed
maintained code	until too sophisticated ^^^abstracted up ^^^ innermost lollowing headers, not body

Total: 315,000 hours (V&V = 1.5 x Development)

32.4% formal proof module testing functional testing 25.9% re-specification 21.6%

Validation Effort			
Iran Irack			
Number of procedures proven formally:	111	21	
Number of procedures covered in semi-global tests	120	33	
Number of procedures tested semi-globally	79	67	
At what of procedures lested rijebility	180	167	

Carry-over from Requirements **Analysis**

Given a language and tools, how do you express the requirements and model the system?

Translate English and diagrams to sets, logic, etc. and translate back and forth, but

how do you read and check these?

what diagrammatic techniques match FMs?

CORE, JSD, GIST, SADT etc. provide:

standard system representations

ways to get different viewpoints

domain modeling techniques

Software process modeling offers:

Guidelines for use

Basis for data collection and eventual metrics

Opportunities for integration, e.g. with testing

Basic appearance of manageability

Modelisation Process

Identification

Entities

Constraints among entities

Operations and their parameters

Representation

Entities become values of a type

Types must be defined to construct, modify, and examine their contents

Representation issues are considered, e.g. ordering, duplication, primitive types, attributes

Additional properties of the data types from requirements

Operations defined with their parameters

Restrictions are expressed as pre-conditions

Its effects are defined in terms of parameter values before and after execution

System invariants are formulated from properties that the system is required or expected to have.

Invariants are proved by induction:

(And a collection of definitions is built up)

The limitations of the model are identified, e.g.

Omitted operations or data details

Implicit definitions

Assumptions about the operating environment (system and users)

Degree of concurrency expressed

Reliability of communication media

Performance, resource, and security requirements that must be met by the implementation

A plan for using the model is developed, e.g.

identifying the riskiest or least understood part for further analysis or refinement

iteration toward more extensive models

Formal proof of properties of the model

Validation, e.g. by

Prototyping from the model

Reviews, inspections, and other peer analyses

Animation of the model-

Scenarios to stimulate response from customers

Summary

SACEM Case

"Complete" application of formal methods

Shows us potential for integration of FM into broader system engineering

Displays interaction of problem domain and formalization

Modelisation

Process aspect to add to FMs as languages & tools

Integration of standard computer science with application domains

Challenge to FM Vendors: write down your process model and

show how modelisation is performed

Formal Methods Technology Insertion Into FTPP

Rick Harper Charles Stark Draper Labs

Formal Methods Technology Insertion

Into

The Fault Tolerant Parallel Processor

presented at the

Second NASA Langley Formal Methods Workshop

11-13 August 1992

presented by

Rick Harper Advanced Computer Architectures Group The Charles Stark Draper Laboratory, Inc.

Cambridge, MA 02139

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Manuary Protectional System Boundaries Cretion Personal Teaching Values of Personal Personal

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Formal Methods Technology Insertion into the FTPP

Objective:

Use formal specification and verification of critical FTPP hardware and software components to reduce the incidence of common-mode failures due to specification and implementation errors

Formal methods do not help avoid many sources of common-mode failures

environmentally-induced faults: EMI, radiation, heat, water, corrosives, sand (!)

Formal methods are not the only solution to common-mode fault avoidance, removal, and tolerance

Mature components, standards compliance, design automation tools, ruthless persecution of complexity, conservative design practices, simulation, testing, various CMF detection/recovery mechanisms

Fault Tolerant Parallel Processor (FTPP)

High-throughput high-reliability/availability computer for hard real-time applications

Uses many Processing Elements (PEs) in parallel for high throughput

Uses redundant PEs for high reliability

Tolerates arbitrary failure manifestations ("Byzantine Resilient")

Designed primarily to tolerate uncorrelated hardware faults

Programmed in Ada

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Fault Tolerant Parallel Processor (FTPP)

Can trade throughput (parallelism) for reliability (redundancy) in real-time

Can be dynamically reconfigured to optimize mission reliability and availability

Supports mixed simplex, triplex, and quadruplex redundancy

Allows heterogeneous processing resources

Parallelism = transparent to programmer

Fault tolerance = transparent to programmer

Current FTPP Applications

"The Army Fault Tolerant Architecture (AFTA) Program"

Funded by: Army Electronics Integration

Directorate / NASA

Application: Helicopter TF/TA/NOE/FCS

"Heterogeneous FTPP"

Funded by: Army Strategic Defense

Command

Application: Battle Management

"Fault Tolerant IMU Processor"

Funded by: a commercial aerospace company

Application: IMU processing

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Cluster 3 (C3) FTPP

Third-generation FTPP

Processing Elements

Support 3 to 40 PEs per cluster 680x0s, 80960s, MIPS R3000s, i860s, or DSP32C signal processors

Network Elements

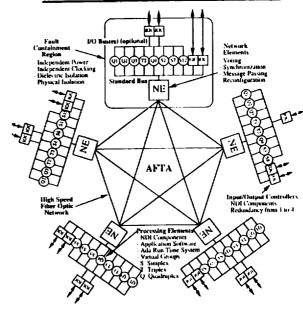
100 Mbit/sec fiber optic interchannel links facilitate fault containment and physical dispersion

Standard bus interface to Processing Elements

Software

XDAdaTM-based operating system with CSDL extensions

FTPP C3 Architecture



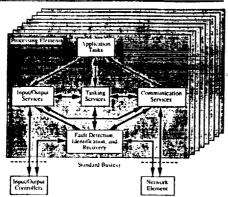
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Layered View of FTPP



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Processing Element

Formally specified / verified microprocessor can be used in FTPP

Processors interface to FTPP over standard bus (e.g., VMEbus)

Not all processors in FTPP need be formally verified

Could use small number of formally verified processors to form quad or triplex Byzantine resilient core VG which runs a simple verified kernel

Core VG responsible for monitoring other VGs (including CMFs) and resetting offenders using voted_reset capability of NE

Throughput of core VG not an Issue...can get desired throughput adding higher-throughput VGs in a heterogeneous parallel processing configuration

All VGs communicate using BRVC

Components of FTPP Suitable for Formal Methods Insertion

Processing Element

Network Element

FCR Backplane Bus

VG Synchronization Software

Task Scheduling Software

Inter-VG Communication Software

FDIR Software

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...

Network Element

Executes performance-critical Byzantine resilience algorithms

Provides BRVC abstraction

Generates vote, FTC, link, and other syndromes

All components execute specifiable and verifiable algorithms

Bus interface

Voter / syndrome accumulator =

FTC

Global Controller

Scoreboard

Substantial body of related work from formal methods community is relevant to these functions

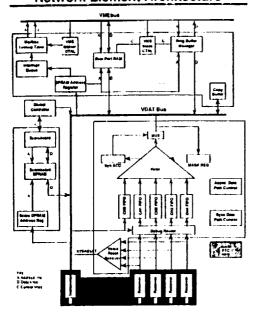
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Network Element Architecture



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13

FCR Backplane Bus

Backplane bus used for PE-NE communication

NE partitioned into bus-dependent and busindependent sections

Can retrofit NE to formally specified/verified backplane bus by modifying bus-dependent section

Formal model of backplane bus needed

Backplanes are a common component of many systems

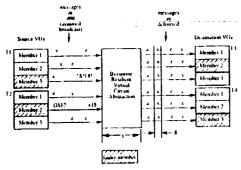
A formally specified and verified backplane could find wide use in critical systems

Powerful building block for ultrareliable systems:

Formally specified and verified processor resident on formally specified and verified backplane bus card

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Byzantine Resilient Virtual Circuit Inter-VG Communication Abstraction



Messages sent by non-faulty members of a source VG are correctly delivered to the non-faulty members of recipients

Non-faulty members of recipient VGs receive messages in the order sent by the non-faulty members of the source VG

Non-faulty members of recipient VGs receive messages in identical order

The absolute times of arrival of corresponding messages at the members of recipient VGs differ by a known upper bound δ

The time between a valid message transmission request and message delivery possesses a known upper bound :

The BRVC ebstraction is supported by the NEs

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VG Synchronization

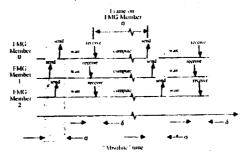
VGs are synchronized upon periodic timer interrupts (e.g., at 100 Hz)

Timer interrupts occur within a bounded skew on all members of VG

Upon timer interrupt a VG performs a synchronizing act (i.e., message passing using BRVC)

Send message to self

Await reception



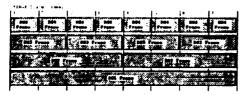
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Rate Group Scheduler

FTPP C3 uses timer-based preemptive rate group scheduler

Variant of rate-monotonic scheduling optimized for iterative task suites having harmonic iteration

Tasks interact only at frame boundaries



FTPP OS schedules appropriate tasks at each frame boundary

Frame Boundary	Completed RGs	Started RGs
7-0	4, 3, 2, 1	4, 3, 2, 1
0-1	4	4
1-2	4, 3	4, 3
2-3 3-4 4-5	4	4
3-4	4, 3, 2	4, 3, 2
4-5	4	4
5-6	4, 3	4, 3
6-7	4	4

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FDIR

FDIR partitioned for validatability

Local FDIR runs on each VG

System FDIR runs on designated VG (e.g., formally verified VG)

Algorithm:

Local FDIR

Executes self tests

Scrubs RAM (independent of characteristics of application task suite)

Periodically transmits self test results to system FDiR via "presence message"

System FDIR

Examines contents and syndromes of presence messages to diagnose senders

Failure to receive presence message within bounded time implies common-mode failure of sender

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Inter-VG Communication

FTPP tasks communicate using message passing queue_message OS call places message onto outgoing queue to NE

FTPP OS determines destination VG from task-to-VG mapping table

OS transmits message queue to destination VG using BRVC

Recipient VG's OS reads message from NE and places into destination task input message queue

retrieve message OS call accesses appropriate task input queue and delivers message to task

All scheduling and inter-VG communication assertions are independent of VG redundancy level

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Fault Recovery

Many recovery policies possible in FTPP

Reduce redundancy level

Reintegrate faulted component

Replace faulted component with spare

System FDIR determines appropriate recovery action and either

transmits recovery commands to local FDI for localized recovery or

performs global system-level recovery

Must show that system FDIR determines correct recovery action as a function of diagnosed component

Must show that local or system FDIR correctly carries out specified recovery

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Heterogeneous Kernels on FTPP

Not all kernels in FTPP need be identical as long as they can communicate using BRVC

FTPP can host rate group scheduler on production VGs and small formally verified kernel on formally verified VGs

Message passing through BRVC subsumes synchronization so the formally verified kernel would not explicitly perform synchronization of redundant sites

The formally verified VG would execute the system FDIR function

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Conclusions from Scoreboard Specification and Verification

Formalization of Scoreboard requirements uncovered several specification omissions and ambiguitles

Collaboration would have been closer and impact on design greater if Draper had been specifically funded to participate

Incremental cost on a \$2.4M brassboard development program is small

Benefit to cost ratio is very high during the conceptual study and detailed design phases

Work in Progress: Scoreboard Specification and Verification

Currently collaborating with ORA to formally specify Scoreboard

Scoreboard is a critical component of FTPP

Comprises approximately 50% of NE circuitry

Enforces BRVC abstraction

Business Model:

FM experts working closely with engineering staff having little exposure to formal methods

Separate funding (Draper not specifically funded to collaborate)

Scoreboard described in VHDL and constructed using automated synthesis (Synopsys)

VHDL used as common language between Draper and ORA

NASA Formal Methods Workshop 11-13 August 1992

Work Planned and Critical Needs

Work Planned

Components similar to remainder of NE (i.e., FTC, voter) have been formally specified/verified

Would like to adapt this work to FTPP

Actively seeking FV processor to design into FTPP

Planning to develop selected subset of RCP software for FTPP

Critical Needs

Viable processor

Formal subset of VHDL, with nonemply intersection of synthesizeable and formal subsets

Continued formalization of FTPP NE

Formal model for FCR backplane bus

Formalization of critical OS functionality

Business model for formal methods insertion

NASA Formal Methods Workshop 11-13 August 1992

11-13 August 1992 NASA Formal Methods Workshop

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Formal Methods at IBM Federal Systems

David Hamilton IBM Federal Systems

Formal Methods Technology Transfer

Some Lessons Learned

David Hamilton
IBM Federal Sector Corporation

Second NASA Langley Formal Methods Workshop

Aug/92

Introduction and Purpose Harlan Mills and SEW Cleanroom SEDL Stepwise Verification CICS TOP (Verification of ESe) Other Projects and Approaches Hote on Quality Emphasis Summary Conclusions 14

Introduction and Purpose

- To cover
 - Some IBM involvement in Formal Methods (FM) projects
 - 2. A perspective on difficulties of technology transfer (beyond a single project)
- Purpose is not to
 - sell the "IBM approach"
 - argue against feasibility of FM
- Purpose is to
 - learn from other FM technology transfer projects
 - suggest some possible future directions

Harlan Mills and SEW

Aug/92

- Mills led massive software engineering education program
 - Software Engineering Workshop was cornerstone
 - 2 week course
 - Taught to all programmers
 - Required to pass final exam
- SEW centered on mathematically-based verification
 - Functional instead of axiomatic
 - model oriented instead of property oriented
 - designed to scale up (stepwise refinement)
 - easier for programmers to understand
 - 2 pieces
 - 1. Deriving program functions
 - Trace tables (basically manual symbolic execution)
 - Recurson instead of loop invariants
 - 2. Module-oriented
 - abstract data types
 - constraints/closure on state data (abstract state machine)

Aug/92

Aug/32

Named after silicon chip manufacturing environment SEW designed to be practical relatively informal Built on SEW foundation, adding scaled up via abstraction/refinement lots of examples and exercises Continuous inspections (SEW style verification) final test : pass/fail Statistical testing (MTTF prediction) Advocated for all programming, not just critical parts Advertised through case studies, not classes no support beyond education no tools Demonstration projects using highly skilled developers no consulting General reaction was that it was impractical To demonstrate benefits too tedious To show it can be done, it is practical seemed only for toy problems Did not gain widespread use Demonstrations projects were success stories Aug/92 Aug/82 SEDL Cleanroom ... Intended to support SEW/Cleanroom verification Showcase project was COBOL/SF concepts Transforms unstructured COBOL into structured Built as an extension to Ada COBOL SEDL compiler generates Ada 52,000 SLOCS developed using Cleanroom Supports design execution Results though SEDL generated code my be inefficient 740 SLOCS / labor month Includes Abstract data types (set, list, map, etc.) 3.4 errors / KSLOC (before first execution) (70 User defined data models avg incl. UT) model vs. representation constraints no error ever found during operational use Supports mathematical notation {X in CHARACTER : x /= 'Q'} exists X in S: P(X) and exists Y in T: P(Y) P>1 and not (exists Q in 2..P-1 : P rem Q=0) **Advocacy of Cleanroom continues** • Use of SEDL is not widespread Widespread use not yet attained But there is a lot of interest in Cleanroom Aug/32 Aug/92

Cleanroom

Harlan Mills and SEW ...

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Other Projects and Approaches

- Application above the code level
 - Development of a "Box Structures" design language
 - Development of a "Box Structures" approach to requirements
 - Results
 - SA/SD approach to design most popular new approach
 - Requirements still written in English
- Emphasis on SEW concepts
 - Concepts generally well accepted
 - Loss of rigor reduces mathematical basis

Note on Quality Emphasis

- Software quality has extreme emphasis
 - Great emphasis on process improvement
 - Serious attention given to quality goals and measurement
 - Quality motivation programs
 - awards and recognition
 - Manned Flight Awareness program
- There is willingness to work hard and invest for quality
- The question is not what or how much but how
 - FM is generally perceived as not helping

Aug/82

11

Aug/92

12

Summary

- Goal was to increase the use of formal mathematical approaches to software development (beyond a single project)
 - 1. First through education
 - 2. Then through demonstration projects
 - 3. Then through tool support
 - 4. Then by making methods more practical
 - 5. Finally through direct support (consulting)
- There have been successes
 - not nearly as widespread as desired
- This story is not unique to FM
 - The problem is with technology transfer, not with technology

Conclusions

- Conclusion: Technology Transfer is very hard, even with
 - extensive education
 - tools support
 - demonstrated successes
- Possible future directions
 - More consulting ("hand holding") (product champions)
 - Use only a core group (FM may just not be for everybody)
 - Require use of FM (selected groups)
 - Success story close to home
 - technology transfer diminishes rapidly as a function of distance
 - long term committment is required (success story requires continued follow-up)
 - Different formal method(s)
 - Different toots (e.g., theorem prover)

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3 Aug/92

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Reliable Computing Platform

 $\underset{\mathrm{ViGYAN}}{\mathrm{Ben~DiVito}}$

ViGYAN, Inc. 30 Research Drive Hampton, VA 23666

Ricky W. Butler

NASA Langley Research Center Hampton, VA 23661

August 11, 1992

Flight Control Problem

Research Objectives

• Fault-tolerant Architecture

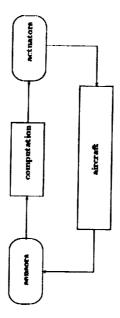
Transient Fault Recovery Capability

Verification Approach

• Specification Sketch of Design Layers

Flight Control Problem

Flight Control Problem

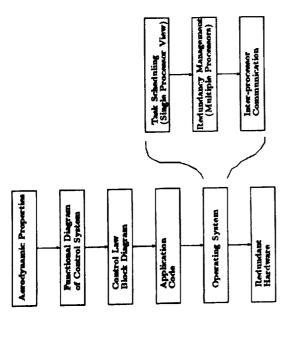


• closed-loop feedback control system

• life-critical

• failure prob < 10⁻⁹ for 10-hour mission

Hierarchical View of a Flight Control System



Research Objectives

Application Task Characteristics

- 1. The set of tasks is fixed
- 2. Hard deadlines
- 3. Multi-rate cyclic scheduling
- 4. Minimal jitter
- 5. Upper bound on task execution time
- 6. Precedence constraints

Research Objectives

- Establish hardware/software platform for ultra-reliable computing
- Use fault-tolerant computer architecture to compensate for physical hardware faults
- Use formal methods to prevent design and implementation errors
- Specify and mechanically verify using EHDM
 - Incorporate emerging technology as needed
- Construct reliability model to quantify reliability estimate

Design Philosophy

Competing objectives:

- Increased design complexity can be used to achieve more sophisticated fault-tolerant architectures — increased tolerance of physical hardware faults for given cost
- Decreased design complexity will lead to fewer design flaws increased avoidance of design faults

Most fault-tolerant systems emphasize (1) at the expense of (2) \longrightarrow we seek a more balanced tradeoff

- Functionality of RCP is modest (currently)—simpler than what can be built in practice today.
- But we have traded this off to achieve provability—better than what we have today.
- · Technology advances will narrow the gap.
- We are trying to push one part of the envelope.

Formal Methods is Enabling Technology For Synchronous Design

- · Design flaw in sync. algorithm is a logical single-point failure
- Clock synchronization notoriously difficult
- Without rigorous demonstration of synchronization, there can be little confidence in the system
- Formal Verification has been successfully applied to clock sync problems

First Design Decisions

Ukrarediabiliky ______ Panit Toberance ______ Redundancy

Fault-Tolerant Architecture

lancy Synchronination

(exact-exacts)

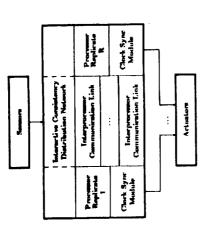
Libertactive Consistence

EMI/HIRF Threat ______ Transient-fauk Immunity

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Reliable Computing Platform

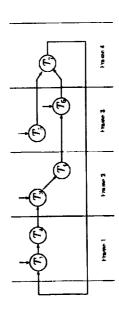
RCP supports execution of tasks for real-time control applications



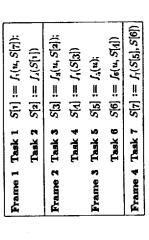
Special-purpose hardware enables exact match voting:

- Distributed agreement front end
- Clock synchronization subsystem

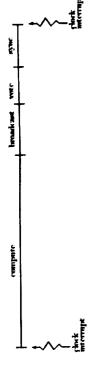
Task Execution in RCP



Task results are assigned to different cells within the state:



RCP's Sequence Of Operation



1. compute

- frame started by clock interrupt
- · execute all tasks scheduled is current frame
 - multiple frames constitute a cycle
- 2. broadcast
- broadcast outputs of task execution to other process
 - usually just a subset of the outputs are broadcast
- . vote broadcast data
- e replace memory with voted values
- · execute sync algorithm
- wait for next clock interrupt

Vote Location/Frequency

option 1: At the instruction level

--- Synchronization must be tight

- After task completion option 2: At the task level

- Loose synchronization

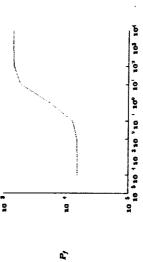
option 3: Asynchronous

--- End up synchronizing in control laws

Various Purposes of Voting

- 1. Voting at the actuators. This approach does not offer recovery from transient faults which can corrupt the state of a good processor unless it is combined with some scheme for periodically voting all the global processor states.
- 2. Voting the entire processor state (e.g. all memory). This approach deals with transients but requires a large CPU overhead.
- Voting only the state which is not recoverable from sensor input. This
 approach also deals with transients but involves increased
 complexity.
- 4. Voting to detect faults. Used in reconfigurable systems.

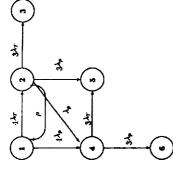
Transient Fault Recovery (N=4)



- Mean Time to Recover From Translent (bourn) [i.e. 1/p]
- · Shape of curve same for larger N
- The locations of the inflection points do not significantly change as N is increased

Reliability Modeling

Reliability Model of Quadruplex Version of System



 $\lambda_T =$ transient fault rate

 $\lambda_P = \text{permanent fault rate}$

 $\rho = \text{rate}$ of flushing effects of a transient

Summary Of Major Design Decisions

Design simplicity is emphasized to promote mathematical analysis

- RCP is non-reconfigurable
- RCP is frame-synchronous
- Scheduling deterministic: abstract axiomatic model
- Internal voting is used to recover (within a bounded time) the state of a processor affected by a transient fault

Consequences of nonreconfigurable architecture:

- · Voting serves no fault detection function
- · Transient fault recovery need not be rapid
- · Reliability models predict recovery time of one minute is adequate

Therefore, favor infrequent voting to reduce overhead

· Selective voting occurs at end of frame after all computation

Demonstrating between the control of the control of

Previous Efforts

1.4

- SIFT
- FTMP
- FTP
- MAFT
- M²FCS
- AIPS

FEATURES

- All had reconfiguration
- FTMP used instruction-level voting
- Only SIFT/MAFT applied formal methods
- MAFT: Level 2 formal methods applied to critical algo-
- -SIFT: Level 3 formal methods applied to fault-masking and reconfiguration design

Relationship Between Formal Methods and the Reliability Analysis

Formal Methods:

Proves formulas of the form:

ENOUGH_WORKING_HARDWARE > PROPER_OPERATION

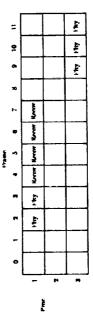
Reliability Analysis: Calculates the following probability:

Prob[ENOUGH_WORKING_HARDWARE]

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Verification Approach

Recovering from Transient Processor Faults



We allow processors to recover their state incrementally over multiple frames

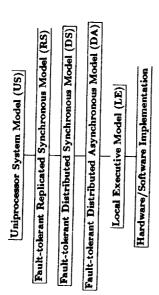
Processors have three fault modes:

- Faulty permanent or transient
- \bullet Recovering persists for N_R frames after disappearance of fault
- Working fully recovered

All theorems about state machine correctness are predicated on the assumption that a majority of working processors exists in each frame.

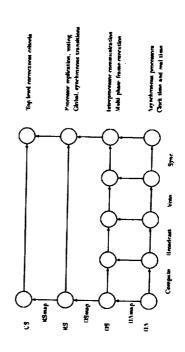
Hierarchical Design and Analysis of RCP

- Remove redundancy management from application domain
- Show that fault-tolerant system achieves same effect as an ultra-reliable uniprocessor
- -- Provided faults are limited



RCP State Machines

Single-frame state transition divided into four phases



Must show that net effect of four DA transitions is the same as single-frame US transition

Framework For Proving Design Correctness

Design layers formalized as nondeterministic state machines

- State represents memory contents and hardware status
 - Transition rulein specifies allowable state transitions
- Nondeterminism models arbitrary behavior by faulty components

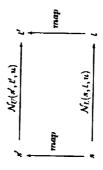
Interpretation maps lower level states into higher level states



Need to show that diagram "commutes" to establish that layer $i+\iota$ correctly implements layer i:

 $N_{i+1}(s_{i+1},t_{i+1})\supset N_i(Map(s_{i+1}),Map(t_{i+1}))$

Generalized Framework For Design Proofs



We must prove two theorems to show that lower level spec L correctly implements upper level spec ${\sf U}$

initial maps: Theorem initial $L(s) \supset \text{initial } U(\text{map}(s))$

frame commutes: Theorem reachable(s) $\land \mathcal{N}_{\ell}(s,t,u) \supset \mathcal{N}_{U}(\operatorname{map}(s),\operatorname{map}(t),u)$

Consider only states reachable via allowable state transitions

Restriction to reachable states allows state invariants to be expressed and proved using a specialized induction schema

Bounded Asynchrony

Extended state machine model used to capture timed behavior

- Clock time snapshots included in DA states
- Nominal durations modeled (state occupancy)
- Mappings to real time introduced

Existing clock synchronization theory available

- Based on Interactive Convergence algorithm
- Previously formalized and proved using EHDM

We assume clock hardware separate from processor

- Faulty clock impairs processor, but not vice versa

Limitations

- Requires two-thirds majority of nonfaulty clocks
- Unable to tolerate transient faults

Specification Sketch

Main Result

Assuming:

- Particular workload and user-selected vote pattern satisfies required abstract properties (Discharged for three examples)
- Clock synchronization properties (later to be refined into hardware circuit tolerant of transient faults)
- Enough functioning hardware in every frame
- Majority of working processors
- Two-thirds majority of nonfaulty clocks

Then under the cumulative state mapping $M = DAmap \circ DSmap \circ RSmap$,

DA has the same effect as US: 1. DA initia(n) \supset US initial(M(n)) 2. reachable(s) \land DA frame(s, t, u) \supset US frame(M(s),M(t),u)

where u denotes external inputs

This result has been formalized and proved mechanically using EHDM.

Representation of State Vectors

US: PRESENT TYPE

RS: ARRAY [processions] OF healthy: nat

percentare: Perare

DS: phase: phases

ARRAY [processors] OF healthy: nat processors. Parace mailton: MRvvv

DA: рыме: рымем

SETH ARRAY [processors] OF healthy: nar

procuestre: Parace mailton: MBvc khod: kegical shoktime camaletes, mmber

US Transition Relation

Top level requirement is the US transition relation:

N...: Definition function[Pstate, Pstate, inputs → boof] = $(\lambda n, l, n: l = f_c(u, s))$ $f_r(u, n) =$ the computation performed by the uniprocessor system.

- · Computation is deterministic and thus can be modeled by a function
- · The ideal uniprocessor model is assumed to always be nonfaulty
- Pstate assumed to have minimal structure
- Control state (e.g., frame counter)
- Array of cells (task outputs)
- Requirements on application task structure are introduced axiomatically
- Set of uninterpreted functions on Pstate values
- Derived functions to specify aggregate effects of task execution
- Axioms concarning state recovery properties
- · Application template can be instantiated in very different ways to achieve varied classes of fault-tolerant systems
- Similar to a general model developed by Rushby

RS Transition Relation

N..: Definition function (RSstate, RSstate, inputs → bool =

(λπ, l, u: (∃h: (∀i:

s(i).healthy > 0

 \supset good values sent(a, u, h(i)) \land voted-final state(a, t, u, h, i))) \land allowable faults(a, t)

allowable_faults: function[RSstate, RSstate → bool] ==

(λ s, t: maj_working(t)

 $\land (\forall \, i : \ell(i).healthy > 0 \supset \ell(i).healthy = 1 + n(i).healthy))$

good values sent: function[RSstate, inputs, MBvec \rightarrow bool] = $\{\lambda_n, u, w : (\forall j :$

s(j).healthy $> 0 \supset w(j) = f_s(f_o(u, s(j).$ proc_state))))

voted_final_state: function[RSstate, RSstate, inputs, MBmatrix, processors → boof

 $\label{eq:locality} (\lambda \, \varkappa, t, u, h, i: t(i). proc. state = f_n(f_n(u, \pi(i). proc. state), h(i)))$

- 2

RS State Vector

RS: ARRAY [processors] OF healthy: nat

provuente: Patate

healthy:

- 0 when a processor is faulty
- · Otherwise, it indicates the number of state transitions since the last transient fault.

proc_state:

- · computation state of the processor.
- takes values from the same domain as used in the US specification.

DEFINITIONS:

- A permanent fault is indicated by a perpetual healthy = 0.
- · A recovering processor has a value of healthy less than the constant recovey period, whose value depends on the task schedule and voting pattern.
- A processor is said to be working whenever healthy \geq recovery period.

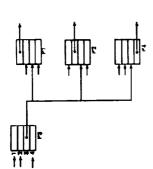
Sample Interpretations for Vote/Scheduling Functions

The three sample interpretations correspond to three types of voting:

- Continuous voting $[N_R = 2]$
- This specifies that the entire state will be voted every frame.
- -Not very practical, but proof that it satisfies application task properties is simple
- Cyclic voting $[N_R = M + 1]$
- This specifies that only the data produced during the frame will be voted.
- SIFT approach
- Minimal voting
- Vote only portion of state that will not be recovered from new sensor
- Construct vote pattern to ensure each cycle of graph is cut by at least one vote.
- N_k is a function of data dependencies and specific vote pattern

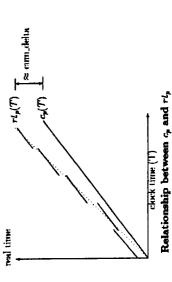
DS Specification

- Decompose frame into four phases: phases: TYPE (compute, broadcast, vote, sync)
- Explicitly model interprocessor communication via a mailbox mechanism



DA Model: Key Concepts (Definition Of a Clock)

- A clock is modeled as a function from clock time T to real time t NOTATION:
- c(T) =an uncorrected (non-synchronized) clock
- $rt^{(i)}(T) =$ the synchronized clock during its ith frame



OS Transition Relation

frame. N de: function[DSstate, DSstate, inputs \rightarrow boof] = $(\lambda s, t, u: (\exists x, y, z: N \land N_{d}(x, y, u) \land N_{d}(x, z, u) \land N_{d}(x, y, u)) \land N_{d}(y, x, u) \land N_{d}(z, t, u)))$

 $\mathcal{N}_{d_{n}}(x,x,u)$: phase 1 — compute $\mathcal{N}_{d_{n}}(x,y,u)$: phase 2 — broadcast $\mathcal{N}_{d_{n}}(y,z,u)$: phase 3 — vote $\mathcal{N}_{d_{n}}(x,z,u)$: phase 4 — sync

 N_{Ai} : function[DSatzle, DSatzle, inputs \rightarrow boof] = { λ a.f. u : maj.averling(i) \wedge t.phase = next.phase(a.phase) \wedge (\forall i: if a.phase = sync. then $N_{Ai}^{i}(a,t,i)$ also then $N_{Ai}^{i}(a,t,i)$ and the $N_{Ai}^{i}(a,t,i)$ \wedge (a.phase = compute $\supset N_{Ai}^{i}(a,t,i)$) \wedge (a.phase = bookstat $\supset N_{Ai}^{i}(a,t,i)$) and (a.phase = bookstat $\supset N_{Ai}^{i}(a,t,i)$) and (a.phase = both $\supset N_{Ai}^{i}(a,t,i)$)

rame commutes: Theorems A frame. M. $da(a,t,u) \supset \mathcal{N}_{u}(DSmap(a),DSmap(t),u)$

The proof involves stepping through the four phases in order and showing that the net result implies the RS relation.

Definition Of Synchronization

KEY PROPERTY OF CLOCK SYNCHRONIZATION SUBSYSTEM: Theorem 1: Theorem

$$\begin{split} \text{SIA}(i) \supset (\forall P, q: (\forall T: \\ \text{nonfaulty.clock}(p, i) \land \text{nonfaulty.clock}(q, i) \land T \in R^{(i)} \\ \supset |rt_{i}^{(i)}(T) - rt_{i}^{(j)}(T)| \leq \delta) \end{split}$$

Theorem 2: Theorem $|Corr_p^{(i+1)} - Corr_p^{(i)}| < \Sigma$

WHERE

S1A : function[period \rightarrow bool] == (λ i : enough_clocks(i)) enough_clocks : function[period \rightarrow bool =

 $(\lambda\,i:3*\mathsf{num}_\mathsf{good}.\mathsf{clocks}(i,\mathsf{nrep})>2*\mathsf{nrep})$

DA Transition Relation

 \mathcal{N}_{μ} includes the advance of local clock time for each transition

```
\land (\mathsf{nonfaulty\_clock}(i, s.\mathsf{sync.period}) \supset
                                                                                                                                                                                      else l.proc(i).healthy = n.proc(i).healthy
                                                                                                                                                                                                                                                                                                                                                                      clock_advanced(s.proc(s).lclock,
\mathcal{N}_{de}: function[DAstate, DAstate, inputs 
ightarrow bool] =
                                                                                                                                                                                                                                                                                                 \wedge L.sync_period = *.sync_period
                                                                                                                                                                                                                            A L-proc(i).cum.delta ==
                                                                                                                                                                                                                                                                   *.proc(i).cum.delta
                                                                       \wedge L.phase = rext_phase(s.phase) \wedge (\forall i : if s.phase = sync
                                         (\lambda s, t, u: enough hardware(t)
                                                                                                                                                  then \mathcal{N}_{\mathcal{L}}(s,t,i)
```

Summary

- Simple fault-tolerant design postulated and refined to a design that models the effects of bounded asynchrony
- Formal four-level hierarchical specification of design constructed
- Mechanical verifications performed
- Reliability model constructed
- · Will continue with more detailed design and verification
- Will extend functionality later

 $\land (a, phase = \mathsf{vote} \supset \mathcal{N}_{k}^{n}(a, l, i)))$

duration(s.phase))

L.proc(i).lclock,

Clock Synchronization Verification and Implementation

Paul Miner
Systems Validation Methods Branch
NASA Langley Research Center

Specification of Clock Synchronization

from Shankar's mechanical verification (using EHDM) of Schneider's A formal specification of the clock synchronization system is drawn general paradigm for fault-tolerant clock synchronization. The main result, given that the implementation satisfies certain constraints,

Clock Synchronization Verification and Implementation

NASA Langley Research Center Hampton, VA 23681

August 11, 1992

Paul S. Miner Peter A. Padilla Wilfredo Torres

Theorem 1 (bounded skew) For any two logical clocks VC_p

 $|VC_p(t) - VC_q(t)| \le \delta$

Example System

1,0 7

and VC, that are nonfaulty at real time t,

Algorithm

A generalized view of the algorithm employed by each clock p is:

do forever {

determine local time to apply correction determine adjustment for this interval when time, apply correction} exchange clock values

The general algorithm is parameterized by a convergence function that determines both the magnitude and time of adjustment.

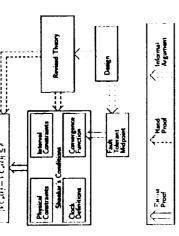
Theory

- Derived from Shankar's EHDM verification of Schneider's general theory.
- Mechanically checked proof of some of Shankar's constraints using new assumptions.
- Hand proof of general approach for transient recovery, some mechanical proofs completed
- Demonstration that conditions of revised theory can be satisfied

Design and Implementation

- Design attempts to use same basic approach for initialization, transient fault recovery, and maintenance of synchronization
- Abstract design derived from formal theory
- Implementation is an instance of abstract design
- Characteristics of Implementation
- Four clock design
- Point-to-point optical communication
- 10Mhz frequency
- External control for experimentation

Verification Overview



Design

- Employs the fault-tolerant midpoint convergence function from Welch and Lynch's algorithm.
- Discard the ${\cal F}$ largest and ${\cal F}$ smallest clock readings
- Return the midpoint of the range of the remaining readings.
 - Average of 2nd and 3rd reading for four clock system.
- Transmit synchronization signal at fixed point in each interval
- Estimate remote clock's value from difference between actual and expected arrival time of signal.
- $\delta \le 11$ ticks; approximately one $\mu \mathrm{sec.}$
- Exploit properties of convergence function for initialization and transient recovery.

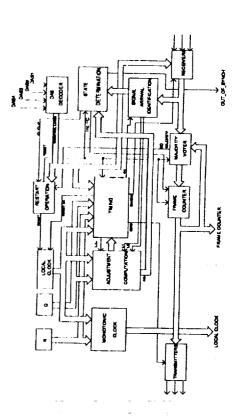
Initialization

- Interval duration is R ticks.
- \bullet Transmit offset of R/2 gives largest window for reading remote
- If N-F signals observed within < R/2-x, system converges within $\log_2(R/2)$ intervals.
- \bullet If fewer than N-F signals observed, either
- compute no correction (Assumed Perfection), or
- compute correction as if missing signals arrived at end of interval (End of Interval).

Each option exhibits pathological cases. For a four clock system, a 2-2 split is possible. The End of Interval approach combined with a simple time-out guarantees initialization, unless a malicious fault is present.

Simulation results confirm expected behavior.

Block Diagram



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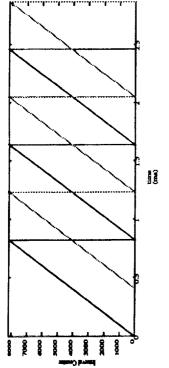
Transient Recovery

- Revised mechanical theory includes uninstantiated predicate that defines a nearly recovered clock.
- A clock is working in the current interval, iff it was either working or nearly recovered in the previous interval (and a sufficient number of other clocks were working).
- Sufficient conditions for the final recovery step are included as assumptions in the mechanical theory.
- The necessary proofs to discharge the assumptions have similar structure to those needed for the general theory.
- For four clock system (using End of Interval), recovery conditions satisfied within two intervals.

Implementation

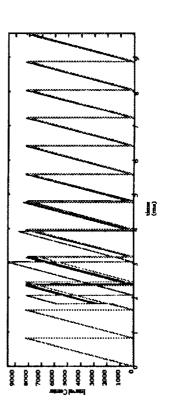
- Off the shelf fiber-optic communication devices
- Remainder of design uses programmable logic devices (PLDs)
 - 0.8192 msec interval, 1.1 µsec skew
- 10MHz frequency
- Synchronization state information available
- Experimental control allows emulation of Byzantine faults
- Both initalization options available
- Key parameters can be modified to explore performance tradeoffs

Simulation of Algorithm



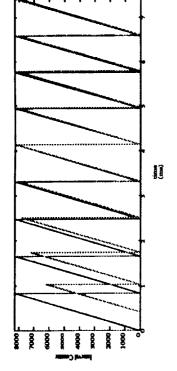
2-2 Split. No jitter or drift

Simulation of Algorithm



Upset Response, No Permanent Faults

Simulation of Algorithm



2-2 Split. With jitter and drift

Concluding Remarks

- General theory for clock synchronization revised to provide simpler verification conditions.
- Fault-tolerant clock synchronization system designed to meet requirements of formal theory.
- Design attempts to use the same basic algorithm for proven initialization, transient recovery, and maintenance of synchronization.
- Implementation uses off-the-shelf communication circuits and PLDs.
- Simulation results confirm behavior predicted by theory.

NASA's Strategy for Technology Transfer

Sally Johnson
Systems Validation Methods Branch
NASA Langley Research Center

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NASA'S STRATEGY FOR TECHNOLOGY TRANSFER

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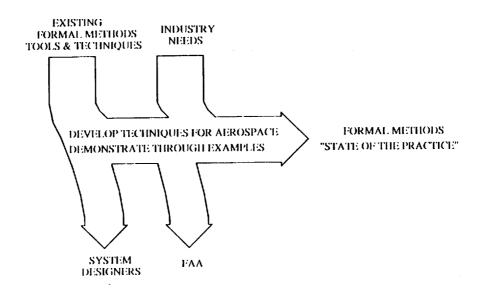
Sally C. Johnson NASA Langley Research Center

GOAL

Technology Transfer to Industry

One of NASA's major goals is to provide the U.S. aerospace industry with the tools and techniques they will need to be world-class competitors in the coming decades.

Technology Transfer



Working with Industry

- Boeing PIU hardware verification
- Boeing SVM hardware verification
- CSDL/ORA Scoreboard hardware verification
- ORA Verification of Ada application software from NASA Goddard and Johnson
 - Formal specification and verification of calendar utilities
 - Mode-control panel logic of Boeing 737 experimental system specified in Larch
- Currently pursuing future projects

Working with the FAA

- Digital Systems Validation Handbook Chapter
- Tutorial presentation to SWAT (SoftWare Advisory Team)
- Formal specification of GCS application
- RTCA committee DO 178B standard

Verification of FTPP Scoreboard and Spectool

Mark Bickford Odyssey Research Associates, Inc.

Moving Formal Methods into Practice

Verifying the FTPP Scoreboard: Phase 1 Results

Mark Bickford Mandayam Srivas ORA Corporation 301 Dates Drive Ithaca, NY 14850 NASA Contract NAS1-18972, Task 5

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ORU



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Formulate abstract requirements

Phase 1 Goals:

Describe high-level design

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Byzantine resilient virtual bus Scoreboard

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FTPP - Charles Stark Draper Laboratory

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AFTA - NASA/Army

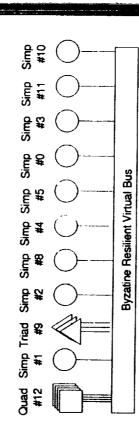
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Context:

Verify that the design meets some of the requirements

D

The FTPP Logical Configuration



Byzantine-Resilient Virtual Circuit

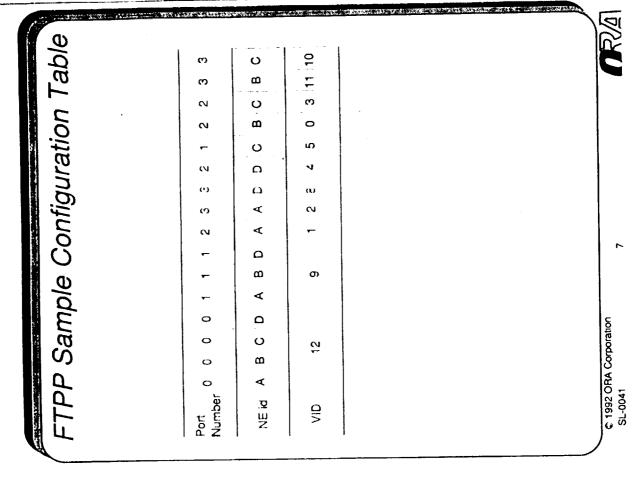
- Reliable delivery: Messages between virtual groups are delivered. Θ
- Group consensus: Each nonfaulty member of a group will receive identical copies of the message delivered to the group. 0
- Order preservation: All non-faulty members of a group receive messages in identical order. **@**
- receive corresponding messages simultaneously within δ Synchronous operation: Non-faulty members of a group ⅎ

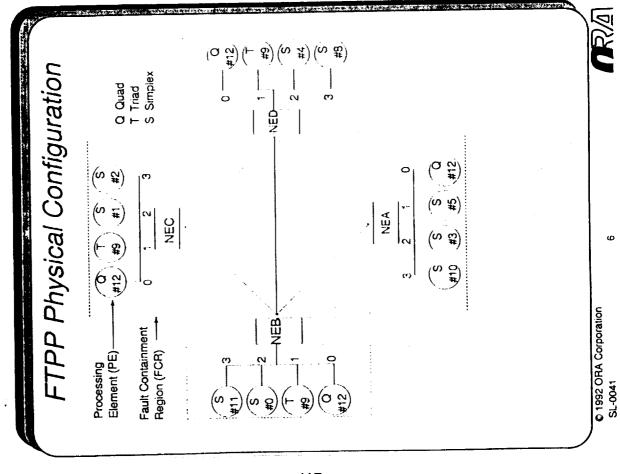
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Network Element Cycle

	Frame 1	Exchange Request Pattern
	Frame n+2	Transmit E
1 Cycle	Frame 3	Transmit Request 1
	Frame 2	Execute Approval F
	Frame 1	Exchange Request Pattem

Exchange Request (LERP):

- IBNF: ready to recieve D
- OBNE: ready to send
- DEST: destination VID
- Other message data

SERP: Poll of LERPs for each PE Scoreboard:

- Vote SERP → VSERP
- Validate and approve messages D

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Actual Behavior = Expected Behavior (provided Liveness) Abstract operations: clear_tmo, update_ct, Expected Behavior → Constraints Abstract view of scoreboard state Requirements: Ξ process_serp © 1992 ORA Corporation SL-0041 \Box \Box \Box \Box

Unanimity or timeout for IBNF, OBNE

Θ

Broadcast takes precedence

@

DEST unique

(3)

Approval:

117

Majority of source group have OBNE

Θ

Majority of dest group have IBNF

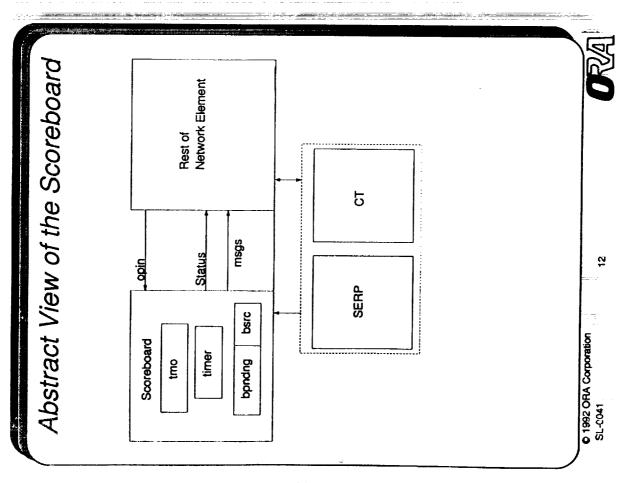
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Other validity conditions

(6)

Valid Message:





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Requirements - Constraint Form

ApprovalCond 'S' 'vid' :=
'OBNEtimeoutcond S vid ' = 'False'

& 'IBNFtimeoutcond S

(voteddstn S vid)' = 'False'

& 'voteddstn S vid)' = 'False'

& 'voteddbne S vid ' = 'True'

& 'votedibnf S

ApprovedMsgs s = MsgOut (trui (Step s))

<<ApproveMsgs s, FinalState s>>

ActualBehavior s =

FinalState s = Final (trut (Step s,

s : trui (Step s)

true s = [s], is idle s

(voteddsin S vid)' = "rrue"
If no broadcast is pending and a message is not broadcast, then a mesasge must be sent if the message satisfies the

general approval conditions.

September 1

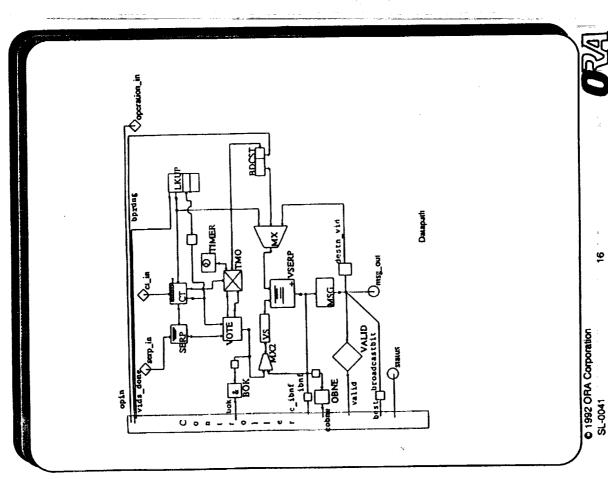
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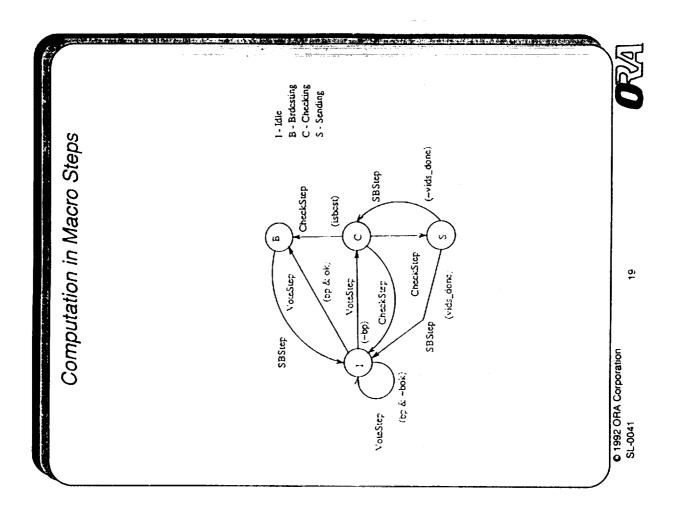
MsgOut (sl:s2:more)

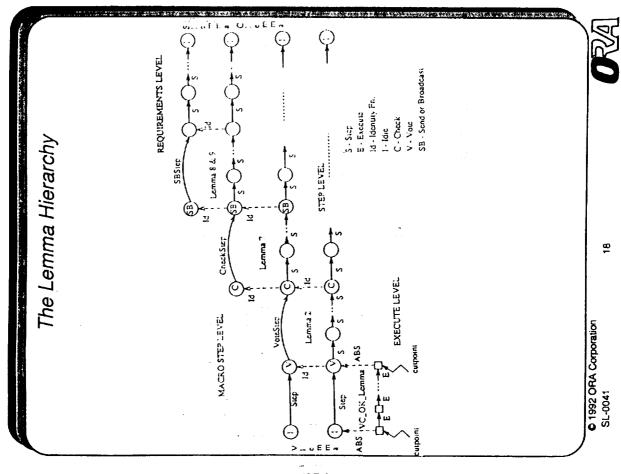
MsgOut [] = [] MsgOut [s] = [] MsgOut (s1:s2:more) = MsgOut (s2:more)

Final (a:x) = Final x

Final [s] =







Main Theorem

MAIN THEOREM :=

(StartSerp 's' 'Succ n'

& ProperABS 's'

& Liveness 's')

= ExpBehavior s' -> 'ActualBehavior s'

Msglemma :=

(ProperABS 's'

& StartSerp 's'

& Liveness 's'

= 'expected_messages s' => 'Msgs(ActualBehavior s)'

ExpBehavior s =

<<expected_msgs s, expected_final s>>

expected_msgs s{bpendingof (ABS_bpndingof s)}= bcst_approved s

expected msgs s =

(ABS_lkupof s) exp_msgs_from_check (VotedSerp s)

checked_msgs (all-clear vs fn num) exp_msgs_from_check vs lkup =

vs 1kup

checked_msgs bok vserp lkup = bcst_truncate bok

(sieve_dest (message_list vserp lkup))

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Ambiguities:

Must validity of pending broadcast be rechecked?

Should invalid broadcast be sent to null?

More than one message to null?

Free-running timer or freeze? 0

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Macro-Step lemmas

Proof of MsgLemma:

Use Viemma, Clemma, SBlemma.

"Sehavior (trui (CheckStep s))' Normallkup (ABS_lkupof s)' (VoceSter s) = /(.s. gara(Step s.)' = StartSerp %' Suco n' Benarior (trunks)' Beharror Clemma := Temma :=

'Sehavior (trut s)' S_emma_s

Moons (ABS_msgof s)

(Behavior (trui (SBSter s))), 'is_send s'='True' & Liveness 's'

exp_mgs(SBStep(CheckStep s))

tl (exp_msgs s)

Induction on length (exp_mgs s)

Check → Send → Check

(•)

Check → Send → Idle

(m)

Check → Bcst → Idle

(c)

Check → Idle

(-)

Four cases:

General lemmas about map, filter, fromto, all

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Proof of Viemma:

- Strengthen induction hyp
- Formulate loop invaraiant Lemma2 :≖ 0
- "VotingStep i s' StartSerp 's' 'n' & 'i <= n' 'iterate i Step s' (i::NAT) (n::NAT)

New Techniques:

- Semi-automatic abstraction used to find definition of Step
- Theory files added to Clio 0

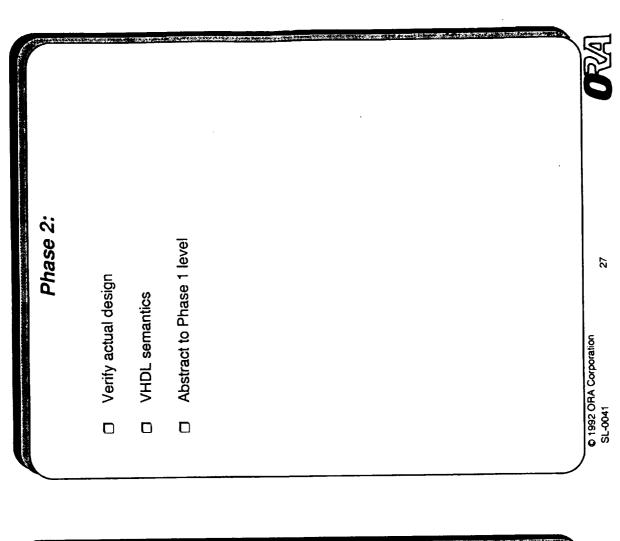
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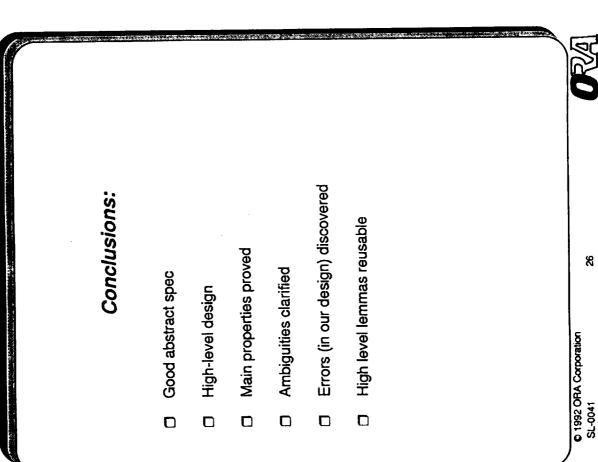
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Boeing's Work in Formal Methods

Dave Fura
The Boeing Company

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Agenda

Application of Formal Methods within the Boeing Defense & Space Group

Presented by

Devid Fura

The Boeing Company Seattle, Washington

Motivation

SAFETY CRITICAL APPLICATIONS:

Military Aircraft

Air Force F-22 fighter aircraft

- Army Comanche Light Helicopter (LH)
 Marine Corps Osprey V-22 titrotor
 Navy A-X attack sircraft
 Ar Force Multirole Fighter (MRF)

Launch Vehicles

NASA/Air Force National Launch System (MLS)

Space Transportation Systems

Moon-Mars Initiative

 Modeling Methodology Current Work Conclusions

System Verification

 Objectives Motivation

Objectives

TO FORMALLY VERIFY SYSTEMS FOR SAFETY CRITICAL APPLICATIONS, INCLUDING BOTH HARDWARE AND SOFTWARE.

Fault Tolerant Computing Platform

Vehicle Management System

Processor Bus Fault-Tolerant Clock Operating System

Targeted systems:

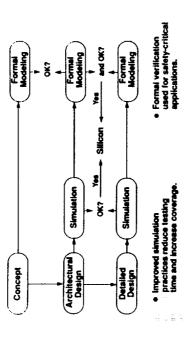
- iFTAS (Integrated Fault-Tolerant Avionics System),
 - FTEP (Fault-Tolerant Embedded Processor).

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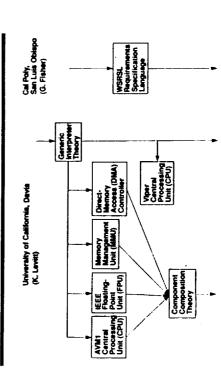
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Objectives (cont'd)

TO DEVELOP AN INTEGRATED DESIGN/VERIFICATION ENVIRONMENT INCORPORATING FORMAL AND TEST-BASED TECHNIQUES:



Background Work



Objectives (cont'd)

Transferring Formal Methods Ideas to Simulation:

 Interpreter models ideas:

Methods of abstraction:

• Temporal • Deta

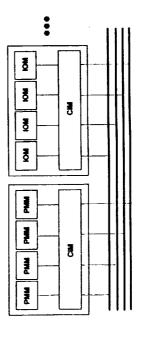
Notions of "correctness"

Improvements:

Chip- and system-level simulation models.
 Facilitated test vector selection and application.
 Automated test result certification.

FTEP Subsystem Configuration

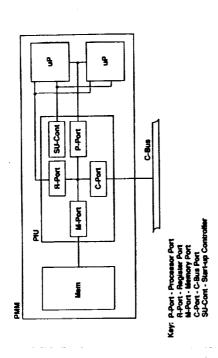
A family of ultra reliable high performance embedded processors based on a set of <u>common</u> hardware/software <u>building blocks</u>:



Key: PMM - Processor-Memory Module IOM - Input Output Module CIM - Core Interface Module

Boeing FTEP Processor-I Space Group





Example HOL Code

Latches:

• D O O + DLAYOCK State (1+1) = PtAlice Dit (State 1) A (1+1) | PtA

Bosing 4 PIU Specification Hierarchy Specification

PIU Specification Summary

Detense & Space Group SUMMARY OF RESULTS:

 The PHJ design specification was formalized in HOL using a 5-level specification hierarchy, using existing toots/techniques (Le., Windley's Generic interpreter Theory):

 The lowest level is a structural representation corresponding to the design that was input to a silicon compiler (model size: 290 state variables, 50 outputs).

 The highest level is a behavioral representation of the entire chip (model size: 150 state variables, 20 outputs).

 A number of design mistakes were uncovered during the specification process.

process.

A modeling approach was identified for the <u>regulrements specification</u>.

 A projotype translator was developed and used to convert, into HOL, suitably formatted descriptions written in the simulation language M.

=

PIU Specification Summary (cont'd)

SUMMARY OF PROBLEMS ENCOUNTERED:

Some standard HOL low-level component models falled to work correctly when applied to the PIU design.

Fixed by straightforward modifications to the models.

Transaction-level behavior of the PIU cannot be modeled as single state transitions of a finite-state machine (FSM), thus it cannot be modeled using Windley's Generic Interpreter Theory.

Being addressed by Windley as part of NASA Contract Tasks 9 and 10.

Generating the specification models for the PIU was a labor-intensive process requiring an enormous amount of effort and time.

The M-to-HOL translator developed by Windley will help in future specifications, but more work is needed in automating this process.

Applying Formal Methods Techniques to Simulation (cont'd)

ABSTRACTION TECHNIQUES:

<u>Temporal Abstraction: relating time</u> at two different levets of a specification hierarchy. <u>Data Abstraction</u>: relating <u>data values</u> at two different levets.

Example: Automating test result certification.

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Applying Formal Methods Techniques to Simulation

case SET: new_0 = HGH; case RESET: new_0 = LOW; case IDLE: new_0 = G; case ILLEGAL: "error handler" and switch: (Behavior partitioned for easier understanding.) Next State Operation Execution: switch (Decode (S,R)) if S and -R then SET; essif -S and R then RESET; essif -S and -R then IDLE; else ILLEGAL); Operation Decode Function: (All input assumptions explicitly specified.) function Decode (S,R) Current_State Inputs INTERPRETER EXECUTION MODELS: Example: SR Latch

Conclusions

Formal methods have an important role to play in the aerospace industry:

Correctness proots for hardware, software, and system implementations. Application:

Application:

Representation of <u>requirements</u> and <u>specifications</u>. (It has been suggested that 70% of our problems are associated with incomplete requirements and specifications.)

Difficult problems remain to be solved:

Modeling approaches for requirements and apecifications need refinement and integration into existing specification hierarchies. (For example, transaction-level model - how many others will be Problem:

needed?)

Tools to efficiently generate correct formal specifications from industry-standard CAD models need development. Problem:

Tools to incresse verification efficiency need development. Problem:

DO-178B and Formal Methods

George Finelli Assistant Head, System Validation Methods Branch NASA Langley Research Center

RTCA BACKGROUND

DO-178B AND FORMAL METHODS

George B. Finelli

Formal Methods Workshop

August 12, 1992

NASA Langley Research Center

SC-167 BACKGROUND

- · Open public forum
- · Terms of Reference (TOR) derived between RTCA and FAA
 - · Plenary and Working Group Meetings
- EUROCAE "shadow" meetings, than joint meetings (January 1991)
 - 5 Working Groups:
- System Issues
- Software Development
- Software Verification
- Quality Assurance and Configuration Management

THE COURSE OF THE PERSON OF TH

- Hequirements and Technical Concepts for Aviation
 Formerly Radio Technical Commission for Aeronautics
 Funded by FAA and industry to provide forums
- DO-178--Software Considerations in Airborne Systems and Equipment Certification (November 1981) Joint activity with European Organization for Civil Aviation
 Electronics (EUROCAE)
- .DO-178A (March 1985)
- DO-178B:

- Currently at Draft 7 ("Final Draft")
 Process initiated October 1989
 Final Plenary meeting—October 1992
- · Special Committee 167.-Digital Avionics Software

TABLE OF CONTENTS

- 1.0 Introduction
- 2.0 System Aspects Relating to Software Development
 - 3.0 Software Life Cycles
- 4.0 Software Planning Process
- 5.0 Software Development Processes

 - 6.0 Software Development Process
- 7.0 Software Configuration Management
- 8.0 Software Quality Assurance Process
 - 9.0 Certification Liaison Process
- 10.0 Airborne System
- 11.0 Software Life Cycle Data
- 12.0 Additional Considerations

HISTORY OF TEXT ON FORMAL METHODS

- Topic addressed by Working Group 2 (Software Verification) under TOR 2 (...nature and degree of analysis, verification, test...activities.)
 - Succession of position papers and presentations on Formal Methods
 - Received working group joint approval
- Decided in plenary to become part of Alternative Methods section (under control of WG2)
 - Received joint approval with Working Group 2
 - . Received Plenary approval
- First appeared in Draft 6, April 1992
- · Currently Draft 7 has been released for final review
 - RTCA Phone: 202-833-9339; FAX 202-833-9434

SUMMARY OF FORMAL METHODS SECTION

- Introductory paragraphs (2) describing general concepts, objectives, and relationship to testing
- Discussion of factors to consider in applying Formal Methods
- Framework for trade-off against other methods
 - Not an "all-or-nothing" proposition

FORMAL METHODS TEXT

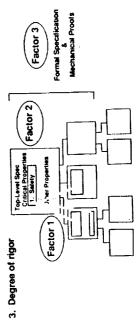
12.0 ADDITIONAL CONSIDERATIONS

12.3 ALTERNATIVE METHODS—General guidance for using alternative methods "...to replace or supplement methods used to satisfy one or more objectives of this document"

12.3.1 FORMAL METHODS

FORMAL METHODS APPLICATION FACTORS

- 1. Levels of Design Hierarchy
- Coverage of software requirements and software architecture



Introduction to the Boyer–Moore Theorem Prover

Warren Hunt Computational Logic, Inc.

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The Nqthm Logic and Theorem Prover

J Strother Moore

April, 1992

Background

- "Ngthm" is the name of both
- a mathematical logic and
- a computer program that mechanizes deduction in that logic.

Nqthm is sometimes called "the Boyer-Moore system."

CLI

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Outline

In this talk we will sketch

- the Nqthm logic,
- its use to formalize and reason about computing machines, and
- the Ngthm mechanization.

Characteristic

CLI

The Nqthm Logic

The Nqthm logic is

- a first-order, quantifier-free logic providing
- inductively defined data types (e.g., integers and lists) and
 - recursively defined functions.

See Chapter 4 of A Computational Logic Handbook, Boyer and Moore, Academic Press, 1988, for details.

CIT

<u>5</u>.

In general, a mathematical logic is defined by

- a formal language,
- a set of axioms expressing assumed truths in the language,
- a set of *inference rules* permitting the derivation of 'new' truths from 'old' ones.

Northm also contains extension principles by which one can soundly add new axioms to the logic.

CLI

The Nqthm Language

A term is either a variable symbol or an n-ary function symbol followed by n terms. We enclose function applications in parentheses.

Here are some Nqthm terms:

(QUOTIENT (TIMES H (SUBL H)) 2)

(PROPER-LISTP X)
(EQUAL (REVERSE (REVERSE X)) (X (IDELIES

5

(IMPLIES (PROPER-LISTP X)
(EQUAL (REVERSE (REVERSE X)) (QUOTIENT (TIMES N (SUB1 N)) 2)

 $(n\times(n-1))/2.$

is printed as

Infix Syntax

is printed as

proper-listp $(x) \rightarrow$ reverse(reverse(x)) = x.

5... -

Boyer and Moore's Personal Thoughts on Infix

Infix is provided to help us communicate our results to those who do not happily read Lisp.

We think that serious users of the theorem prover would be harmed more than helped by its adoption as the interface syntax.

CTI

Propositional Calculus and Equality

AXIOM: true() \neq false() (abbreviated by $t \neq f$)

AXIOM: $x = f \rightarrow if x$ then y else z endif = z.

AXIOM: $x \neq f \rightarrow if x$ then y else z endif = y.

DEFINING AXIOM:

 $b \lor d$

if p then if q then t else f endif else f endif.

CE

Ordered Pairs (Lists)

AXIOM: listp(cons(x, y)).

AXIOM: car(cons(x, y)) = x.

AXIOM: cdr(cons(x, y)) = y.

AXIOM: $\neg \text{ listp}(x) \rightarrow \text{car}(x) = 0$.

AXIOM: $\neg \text{ listp}(x) \rightarrow \text{cdr}(x) = 0$.

etc.

Rules of Inference

In addition to the rules of inference for propositional cal-culus and equality, Ngthm provides

AXIOM: zero() \in N (abbreviated by $0 \in$ N)

Peano Arithmetic

AXIOM: add1(x) \in N.

AXIOM: $add1(x) \neq 0$.

AXIOM: $x \in \mathbb{N} \to \text{subl}(\text{add}1(x)) = x$.

- Instantiation. From the theorem p(x) one may derive the theorem $p(\alpha)$ for any term α .
- Induction. For example, from the theorem p(0) and the theorem $(x \in \mathbb{N} \land x \neq 0 \land p(x-1)) \to p(x)$, one may derive the theorem $(x \in \mathbb{N}) \to p(x)$.

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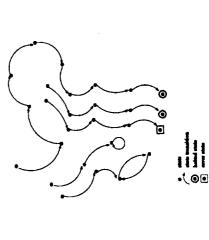
Extension Principles

- Shell Principle. One may add axioms defining new inductively constructed "data types" following a certain schema.
- Constraint Principle. One may add axioms introducing new function symbols with arbitrary properties provided one exhibits old function symbols ("witnesses") with those properties.
- Definitional Principle. One may add axioms defining new recursive functions provided certain syntactic restrictions are met and each recursion can be proved to terminate.

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Using Nqthm Logic to Formalize a Computing Machine



173

Suppose 'step' is the state transition function.

Then the machine is formalized with:

DEFINITION: m(s, n)

. .

if n=0

then s else m(step(s), n-1) endif.

A theorem about this machine is:

THEOREM. m(s, i+j) = m(m(s, i), j).

E)

Shell Introduction.

Let a state be constructed by st (pc, stk, mem, haltedp, defs), where

- pc is the location, in defs, of the "current instruction;"
- stk is a stack recording the currently active subroutine calls;
- mem is a list recording the values of successive memory locations;
- haltedp is a flag indicating whether the state is "running," "halted," or "erroneous;"
- defs is a list of programs, each of which is a named list of instructions.

CLI

```
CLI
             pc
stk
mem
haltedp
defs
                      '(01234567...),
                                           (movi 0 77)
(movi 1 88)
(call times)
                                                                   (ret)
(movi 2 0)
(jumps 0 5)
(add 2 1)
(subi 0 1)
(jump 1)
(ret)))
An example state is
           st(' (main . 0),
                                                                            (times
                                            (main)),
```

if op=' mov1 then movi(a, b, s) elseif op=' add then add(a, b, s) elseif op=' jump then jump(a, b, s) elseif op=' call then call(a, s) elseif ... endif

endlet.

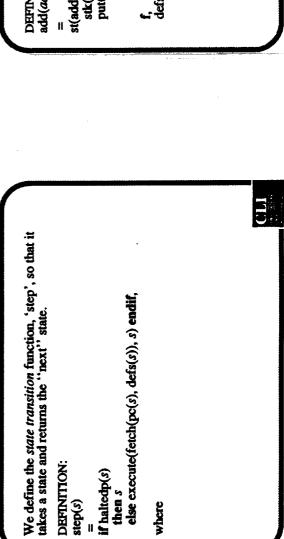
x; x is of the form x; ' (op a b)

let op be car(x)
a be cadr(x)
b be caddr(x)

.5

DEFINITION: execute(x, s)

5



where

step(s)

5. * st(add1-pc(pc(s)),
stk(s),
put(addr1,
get(addr1, mem(s)) + get(addr2, mem(s)), DEFINITION: add($addr_I$, $addr_2$, s) mem(s)), **f,** defs(s)).

(jumpr 0 5)
(add 2 1)
(subi 0 1)
(jump 1)
(ret)) st(add1-pc(pc), stk, list*(0, r_1 , $r_0 \times r_1$, mem), \mathbf{f} , defs). \rightarrow m(st(pc, stk, list*(r_0 , r_1 , r_2 , mem), f, defs), 4+4× r_0) fetch(pc, defs) = ' (call times) assoc('times, defs) = '(timesAnother theorem about 'm' is THEOREM: ro∈N

The machine 'm' is unrealistically simple. More interesting machines have been defined in the Nqthm logic:

• FM8502 (a microprocessor designed and verified by CLI)

• Piton (a stack-based assembly language)

• Micro-Gypsy (a subset of Gypsy)

• NDL (hardware description language of LSI Logic, Inc.)

• FM9001 (a microprocessor designed, verified, and fabricated by CLI)

• MC68020 (a commercial microprocessor by Motorola,

• KIT (a multiprocessor implemented on a uniprocessor)

3 Given two formalized machines, 'hi' and 'lo,' one can derive relations between them, e.g., 汪 2 hi(s, n) = up(lo(down(s), clk(s, n))).good-hi-statep(s)

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(meain (movi 0 77) (movi 1 88) (call times) (ret) (times (movi 2 0) (jumps 0 5)

(movi 0 77)
(movi 1 88)
(call times)

(ret)) times

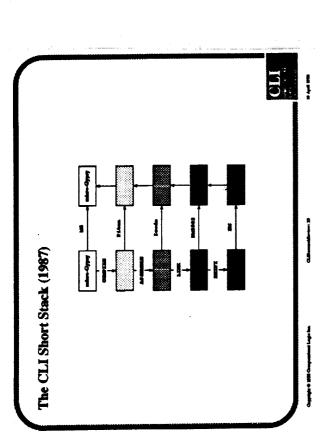
jumps 0 5) (movi 2 0)

st(' (main . 3), nil, ' (0 88 6776 3)

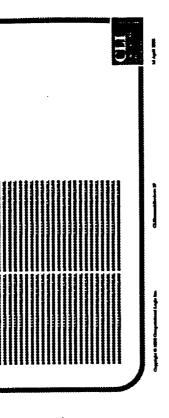
st(' (main . 0), nii, '(0 1 2 3) f,

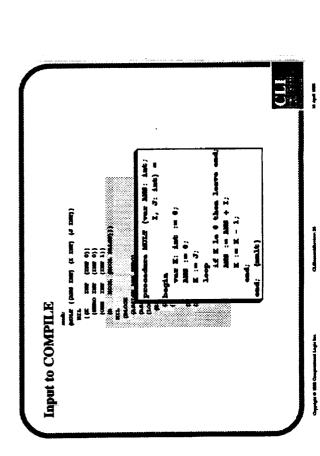
m(s0, 315)

Execution of Nqthm Logic



The Output of REIFY





Functional Instantiation (a derived inference rule)
THEOREM:

m(s, i+j) = m(m(s, i), j).

can be constructed without knowing anything about 'step.'

It is a general property of any "iterated step function," i.e., any 'm' whose definition is

DEFINITION:

m(s, n)

if n = 0

if n = 0

then s

else m(step(s), n-1) endif,

for some 'step' function.

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This can be formalized by

- introducing 'step' without defining it (i.e., by constraining it to be any function);
- \bullet defining 'm' in terms of the undefined 'step'; and then
- proving m(s, i+j) = m(m(s, i), j).

CLI

Suppose later some very complicated machine, e.g., 'Ada', has been defined in terms of some very complicated 'Adastep.' It is possible to derive

Ada(s, i+j) = Ada(Ada(s, i), j).

from

m(s, i+j) = m(m(s, i), j)

by functional instantiation, replacing 'm' by 'Ada' and 'step' by 'Ada-step,'

provided one can show that the axioms used in the original proof are true of the new functions.

CLI

If you functionally instantiate

DEFINING AXIOM:

m(s, n)

then s if n=0

else m(step(s), n-1) endif,

replacing 'm' by 'Ada' and 'step' by 'Ada-step,' you get

THEOREM? Ada(s, n)

 $lf_n = 0$

else Ada(Ada-step(s), n-1) endif. then s

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The Ngthm Theorem Prover

The Nqthm system is an interactive computer program which can be used to help discover and check proofs of theorems in the Nqthm logic.

Some facts about Nqthm:

- It is fully documented in A Computational Logic Handbook.
- It is distributed without fee (but under license) by CLI.
- It is heavily used at CLI and elsewhere to formalize and reason about computational problems.

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- code developed by Boyer and Moore (often in response to Nqthm consists of about 1Mb of Common Lisp source users' needs or suggestions) over the past 21 years.
- There are over 16,000 theorems in its standard benchmark now. These 11Mb of examples, contributed by 20 users, are distributed with the system.

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THEOREM: app(app(a,b),c) = app(a,app(b,c)).

Proof. Call the conjecture *1. Perhaps we can prove it by induction. Three inductions are suggested by terms in the conjecture. They merge into two likely candidate inductions. However, only one is unflawed. We will induct according to the following scheme:

 $((\text{listp}(a) \land p(\text{cdr}(a), b, c)) \rightarrow p(a, b, c))$

 $(-iistp(a) \rightarrow p(a,b,c))$. Linear arithmetic and the kemma cdr-leasp can be used to prove that the measure count(a) decreases according to the well-founded relation '<' in each induction step of the scheme. The above induction scheme leads to two new goals:

Case 2. (listp(a) \wedge app(app(cdr(a), b), c) = app(cdr(a), app(b, c))) \rightarrow app(app(a, b), c) = app(a, c), which simplifies, applying the lemmas cdr-cons and car-cons, and opening up the definition of 'app', to t.

That finishes the proof of *1. Q.E.D.

Case 1.— $\operatorname{listp}(a) \to \operatorname{app}(\operatorname{app}(a,b),c) = \operatorname{app}(a,\operatorname{app}(b,c)),$ which simplifies, unfolding the function 'app', to t.

Nqthm's behavior is determined by previously proved theorems.

The theorem

proper-listp(x) \rightarrow reverse(reverse(x)) = x,

when used as a rewrite rule, is interpreted to mean: replace "reverse(reverse(α)""

by "a,"

provided "proper-listp(α)" can be established.

The experienced user "programs" proof strategies into Nqthm by carefully selecting the theorems to be proved.

CLI

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A typical interchange between the user and Nqthm:

- The user submits a theorem to prove.
- Ngthm applies its proof techniques, guided by its data base. It prints a running commentary on its progress.
- The user reads the commentary and discovers that Nqthm is failing because it does not "know" a certain rule.
- The user aborts the proof.
- The user formulates the appropriate theorems and starts

Interaction Styles

Suppose the final sequence of theorems is as shown below.

LEMMA 1.1.1

LEMMA 1.1

LEMMA 1.2

THEOREM 1

THEOREM 2

LEMMA 2.1

THEOREM 3

MAIN THEOREM

The user who initially submits the theorems in this order (due to a thorough analysis of the problem) experiences Nqthm as a proof checker.

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The user who starts by submitting the MAIN THEOREM and is forced by the theorem prover's difficulties to discover the need for the others

Lemma 1.1.1

Lemma 1.1

Lemma 1.2 Lemma 2. Theorem 1

Theorem 2

MAIN THEOREM Theorem 3

is delegating the proof strategy to Nqthm. Such users often experience Nqthm as unbelpful.

CE

Experienced users generally use a mixed strategy in which the basic outline of the proof is discovered "off-line" and submitted coherently, expecting Nqthm to help fill in the gaps.

Lemma 1.1.1 LEMMA 1.1

Lemma 1.2

THEOREM 1

Lemma 2.1

THEOREM 2

MAIN THEOREM THEOREM 3

Such users experience Nqthm as a very helpful assistant.

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Proof Maintenance

Each theorem proved adds one or more new rules to the data base.

(rule 1.1.1) (rule 1.1) **LEMMA 1.1.1** LEMMA 1.1 LEMMA 1.2

(rule 1.2) (rule 2.1) (rule 2.1) (rule 2) LEMMA 2.1 THEOREM

THEOREM 2 THEOREM 3

MAIN THEOREM

The experienced user designs general but efficient strategies (making heavy use of simplification, avoiding case splits when possible, and terminating quickly with or without suc-



14 April 1988

When the main theorem is changed "slightly" the old strategy often still works.

(rule 1.1.1)
(rule 1.1)
(rule 1.2)
(rule 1.2)
(rule 1.3)
(rule 2.1)
(rule 2.3)
(rule 3.3) **LEMMA 1.1.1** LEMMA 1.2 LEMMA 1.1 THEOREM 1

THEOREM 3
MAIN THEOREM' LEMMA 2.1 THEOREM 2

If not, the failure leads, via the normal process, to a reformulation of some of the lemmas.

Nqthm-1992

We are about to release a new version of Nqthm, providing:

- constrained function introduction,
- functional instantiation,
- support for enabling/disabling theories,
- cond, case, let, list*, and "backquote" notation,
- improved performance on large case analyses,
- improved performance when many rules are disabled,
- "endorsement" tools for event scripts,
- over 11Mb of endorsed example scripts, and
- a Second Edition of the Handbook.

Introduction to PVS

Natarajan Shankar SRI International

Specification and Verification using PVS

N. Shankar shankar@csl.sri.com

Computer Science Laboratory SRI International

Outline

This talk is a short tutorial on specification and verification, using PVS as an illustrative example.

- Background to PVS
- Overview of PVS
- Some Examples

Background: Past Experience

Considerable accumulated experience on verification at SRI

Systems developed at SRI include: Boyer-Moore Prover, HDM, OBJ, STP, EHDM, etc.

Other Systems used include: Affirm, RRL, Gypsy, Muse, etc.

Verifications include: Byzantine fault-tolerant clock synchronization, Byzantine Agreement, Gödel's first incompleteness theorem, and many others.

Background: EHDM

Designed at SRI around 1984.

A specification environment based on higher-order logic with parametric modules, implementation mappings, Hoare logic prover, etc.

Theorem prover based on skolemization, manual instantiation, and Shostak's decision procedures.

Example verifications include: Byzantine fault-tolerant clock synchronization, Ramsey theorem, Byzantine Agreement, Fault-masking and Transient recovery, etc.

Background: Lessons Learnt

Decision procedures are extremely useful but only a small part of what is needed.

Highly automatic theorem provers are inappropriate: difficult to control, and provide very little useful feedback.

Low-level proof checkers are inefficient (both in machine and human terms), and also fail to yield a satisfactory proof.

Logics with limited expressibility are easily mechanizable, but place a large burden on the specifier.

Some highly expressive notations are nice for pencil-and-paper work, but might be difficult to adequately mechanize.

5

PVS: Overview

PVS has been used to check proofs of

- the Boyer-Moore majority algorithm
- ordered binary tree insertion
- a version of the Schröder-Bernstein theorem
- Byzantine Agreement
- a pipelined processor (due to Saxe), and other hardware examples.

These proofs can typically be completed in less than a day.

PVS

Started in mid-1990.

The goal was to combine clear notation with a productive proof development environment to produce machine-checked, yet "humanly readable" proofs.

PVS was primarily influenced by EHDM, but also adapts ideas on language and inference from IMPLY, Boyer-Moore prover, LCF, HOL, ML, Nuprl, Veritas, OBJ, and many other systems.

PVS consists of a core language definition, parser, typechecker, and proof checker.

Contributors to PVS include Sam Owre, John Rushby, Friedrich von Henke, David Cyrluk, Judy Crow, Carl Witty, and Steven Phillips.

6

Overview: Decision Procedures

PVS proofs make heavy use of arithmetic decision procedures. Any THEOREM below is automatically proved. CONJECTURES are either false or unproved by decision procedures.

```
arithmetic : THEORY
BECIE
 x,y,v: VAR number
arith: THEOREM
    x < 20y AND y < 30v INPLIES 30x < 180v
  badarith: CDWJECTURE
    x < 2*y AND y < 3*v IMPLIES 3*x < 17*v
  badarith2: CONJECTURE
    x<0 AWD y<0 IMPLIES x+y>0
  baddiv: COMJECTURE
    (x/y) > v IMPLIES x > (y+v)
  gooddiv: COWJECTURE
    y/=0 AND (x/y) > v IMPLIES x > (y+v)
  anotherdiv: THEOREM
    y \neq 0 AND (x/y) > (v/y) IMPLIES ((x-v)/y) > 0
  intarith: THEOREM
2-1 < 5 AND 1 > 1 IMPLIES 1 = 2
  bederith3: COMJECTURE
    2+x < 5 AND x > 1 INPLIES x = 2
EMD arithmetic
```

8

Type Correctness Conditions

Denominator for division must be non-zero. Typechecking the previous theory generates type correctness conditions. baddiv_TCC1 is not provable, hence a type error.

```
arithmetic: THEORY
 BEGIN
  x, y, v: VAR number
  arith: THEOREM
   x < 2 + y AND y < 3 + v IMPLIES 3 + x < 18 + v
 badarith: CONJECTURE
   x < 2 + y AND y < 3 + v IMPLIES 3 + x < 17 + v
 badarith2: CONJECTURE
   x < 0 AND y < 0 IMPLIES x + y > 0
 baddiv: CONJECTURE
   (x / y) > v IMPLIES x > (y + v)
 % Subtype TCC generated for ;
 baddiv_TCCi: OBLIGATION (FORALL (y: number): y /= 0)
 gooddiv: COMJECTURE
   y \neq 0 AND (x \neq y) > y IMPLIES x > (y + y)
 anotherdiv: THEOREM
   y = 0 AND (x / y) > (v / y) IMPLIES ((x - v) / y) > 0
 interith: THEOREM 2 + i < 5 AND i > 1 IMPLIES i = 2
 badarith3: CONJECTURE 2 + x < 5 AND x > 1 IMPLIES x = 2
```

Example: Binary Trees

Binary trees can be defined as abstract datatypes.

The following datatype declaration introduces the *constructor* leaf with recognizer leaf?, and constructor node with *accessors* val, left, and right, and recognizer node?.

Typechecking this datatype declaration generates the theories binary_tree_adt and binary_tree_rec_mod (shown below).

```
binary_tree[7 : TYPE] : DATATYPE
BEGIN
leaf : leaf?
node(val : T, left : binary_tree, right : binary_tree) : node?
EMD binary_tree
```

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Abstract datatype theory

```
binary_tree_adt[T: TYPE]: THEORY BEGIN
 BEGIN
binary_tree: TYPE
 leaf?, node7: PRED[binary_tree]
leaf: (leaf?)
 node: [T, binary_tree, binary_tree -> (node?)]
val: [(node?) -> T]
left: [(node?) -> binary_tree]
 right: [(node?) -> binary_tree]
 leaf_extensionality: AXION
    (FORALL (leaf?_var: (leaf?)): leaf = leaf?_var)
 node_extensionality: AXIOM
   (FORALL (node?_war: (node?)):
    node(wal(node?_war), left(node?_war), right(node?_war))
      = node?_var)
 val_node: AXIOM
   (FORALL (node1_var: 7), (node2_var: binary_tree),
     (node3_var: binary_tree):
val(node(nodei_var, node2_var, node3_var))
     = node1_var)
   (FORALL (node1_var: 7), (node2_var: binary_tree),
            (node3_var: binary_tree):
     left(node(node1_var, node2_var, node3_var)) = node2_var)
 right_node: AXION
   (FORALL (node1_var: 7), (node2_var: binary_tree),
     (node3_var: binary_tree):
right(node(node1_var, node2_var, node3_var)) = node3_var)
```

11

```
binary_tree_nat_rec((leaff_fun: mat),
                       (node?_fun: [T, nat, nat -> nat])):
  [binary_tree -> nat] =
  LAMBDA (binary_tree_var: binary_tree):
CASES binary_tree_var DF
leaf: leaf?_fun,
       node(node1_var, node2_var, node3_var):
            node?_fun(node1_var,
                        binary_tree_nat_rec(leaff_fun,
                       node?_fun)(node2_var),
binary_tree_nat_rec(leaf?_fun,
                                               node?_fun)(node3_var))
     ENDCASES
binary_tree_ordinal_rec((leaf?_fun: ordinal),
                            ((lear:_lun: viulnul),
(node?_fun: [7, ordinal, ordinal
-> ordinal])):
  [binary_tree -> ordinal] =
  LAMBDA (binary_tree_var: binary_tree):
     CASES binary_tree_var DF
       leaf: leaf?_fun,
       node(nodei_var, node2_var, node3_var):
    node7_fun(nodei_var,
                       binary_tree_ordinal_rec(leaf?_fun,
                       node?_fun)(node2_ver),
binary_tree_ordinal_rec(leaf?_fun,
                                                    node?_fun)(node3_var))
     PERCESES
END binary_tree_adt
```

Recursion combinator

12

Ordered Binary Trees

```
obt [T : TYPE, <= : (total_order?[T])] : THEORY
REGIE
USING binary_tree_adt, binary_tree_rec_mod
A, B, C: VAR binary_tree[T]
x, y, x: VAR T
pp: VAR PRED[T]
checkell((pp : PRED[T]), A): bool =
  i, j, k: VAR net size(A) : net =
  binary_tree_rec(0, (LANBDA x, i, j: i + j + 1))(A)
ordered?(A) : RECURSIVE bool :
  ELSE TRUE ENDIF)
  BY size
insert(x, A): RECURSIVE binary_tree[T] =
  (CASES A OF
    leaf: node(x, leaf, leaf),
    node(y, B, C): (IF x<=y THEH node(y, insert(x, B), C)
ELSE node(y, B, insert(x, C))
                      PROTE
   EWDCASES)
  BY (LAMBDA x, A: size(A))
ordered?_insert_step: FORMULA
    pp(x) AND checkall(pp, A) IMPLIES
    checkall(pp, insert(x, A))
ordered?_insert: FORMULA
  ordered?(A) IMPLIES ordered?(insert(x, A))
END obt
```

Example Proof

```
ordered?_insert :
{1} (FORALL (x: 7), (A: binary_tree):
ordered?(A) IMPLIES ordered?(insert(x, A)))
Rule? (Induct "A")
Inducting on A,
this yields 2 subgoals:
ordered?_insert.1
{1} (FORALL (x: T): ordered?(leaf) IMPLIES ordered?(insert(x, leaf)))
Rule! (skolem!)
For the top quantifier in 1, we introduce Skolem constants: (x/3) this simplifies to:
ordered?_insert.1 :
(1) ordered?(leaf) IMPLIES ordered?(insert(x!3, leaf))
Rule? (dsimp)
Applying disjunctive simplification,
this simplifies to:
ordered?_insert.1 :
{-1} ordered?(leaf)
{i} ordered?(insert(x!3, leaf))
Rule? (rewrite "insert")
Rewriting using insert, this simplifies to:
```

```
ordered?_insert.1 :
[-1] ordered?(leaf)
                                                                                          Rule? (then (split)(rewrite "checkall"))
{1} ordered?(node(xi3, leaf, leaf))
                                                                                          Splitting conjunctions, this yields 2 subgoals:
Rule? (rewrite "ordered?" +)
                                                                                          ordered?_insert.i.i :
Rewriting using ordered?,
this simplifies to:
ordered?.insert.1:
                                                                                          [-1] ordered?(leaf)
                                                                                          {1} checkell((LAMBDA (y: T): y \leftarrow x!3), leaf)
[-1] ordered?(leaf)
                                                                                          Rewriting using checkall,
{1} (checkall((LANBDA (y: T): y <= x!3), leaf)
AND checkall((LANBDA (y: T): x!3 <= y), leaf)
                                                                                          This completes the proof of ordered?_insert.1.1.
             AND ordered?(leaf) AND ordered?(leaf))
                                                                                           ordered?_insert.1.2 :
Rule? (assert)
Invoking decision procedures,
this simplifies to:
                                                                                           [-1] ordered?(leaf)
ordered?_insert.1 :
                                                                                           {1} checkall((LAMBDA (y: T): x!3 <= y), leaf)
[-1] ordered?(leaf)
                                                                                          Rewriting using checkall,
{1} checkall((LAMBDA (y: T): y <= x!3), leaf)
AND checkall((LAMBDA (y: T): x!3 <= y), leaf)</pre>
                                                                                           This completes the proof of ordered?_insert.1.2.
Rule? (auto-rewrite "binary_tree_rec[T, bool]")
                                                                                           This completes the proof of ordered? insert.1.
Installing automatic rewrites:
  binary-tree_rec[7, bool],
this simplifies to:
ordered?_insert.1 :
 [-1] ordered?(leaf)
ordered?_insert.2 :
                                                                                           Rule? (dsimp)
                                                                                           Applying disjunctive simplification, this simplifies to:
 {1} (FORALL (node1_war: T), (node2_war: binary_tree),
                                                                                           ordered?_insert.2 :
                (node3.var: binary_tree):
            (FORALL (x: T):
                                                                                           {-1} (FORALL (x: T):
              erdered?(node2_var) IMPLIES ordered?(insert(x, node2_var)))
                                                                                                      ordered?(node2.var!5)
                                                                                                      IMPLIES ordered?(insert(x, node2.var!5)))
              (FORALL (x: T):
ordered?(node3_var)
                                                                                                      UMRLL (X: T):
ordered?(node3_var!6)
                                                                                           {-2} (FORALL (x: T):
                IMPLIES ordered?(insert(x, node3_var)))
                                                                                                      IMPLIES ordered?(insert(x, node3_var!6)))
              IMPLIES
              (FORALL (x: T):
                                                                                           {1} (FORALL (x: T):
                ordered?(node(node1_var, node2_var, node3_var))
IHPLIES ordered?(insert(x, node(node1_var,
                                                                                                      ordered?(node(node1_var!4, node2_var!5, node3_var!6))
                                                                                                        IMPLIES ordered?(insert(x, node(node1_var!4,
                                               node2.var,
                                                                                                                                    node2_var!5.
                                               node3.ver)))))
                                                                                                                                     node3_var(6))))
 Rule? (skolem!)
 For the top quantifier in 1, we introduce Skolem constants: (nodel_vari4 mode2_vari5 node3_vari6)
                                                                                           Rule? (skolem!)
                                                                                           For the top quantifier in 1, we introduce Skolem constants: (x!7)
                                                                                            this simplifies to:
 this simplifies to:
                                                                                           ordered?_insert.2 :
 ordered?_insert.2 :
                                                                                           [-1] (FORALL (x: 7):
ordered?(node2-var!5)
 {i} (FORALL (x: T):
                                                                                                      IMPLIES ordered?(insert(x, node2_var!5)))
          ordered?(node2_var!5) IMPLIES ordered?(insert(x, node2_var!5)))
                                                                                            [-2]
                                                                                                   (FORALL (x: T);
ordered?(node3_var!6)
          (FORALL (x: T):
                                                                                                      INPLIES ordered?(insert(x, node3_var!6)))
            ordered?(node3.var!6)
            IMPLIES ordered?(insert(x, node3_var!6)))
                                                                                            [1] ordered?(node(node1_var!4, node2_var!5, node3_var!6))
          INPLIES
                                                                                                    IMPLIES ordered?(insert(x!7, node(node1_var!4,
          (FORALL (x: T):
                                                                                                                                   node2.var!5,
            ordered?(node(node1_var!4, node2_var!5, node3_var!6))
                                                                                                                                   node3.ver(6)))
```

=

INPLIES ordered?(insert(x, node(node1.var!4,

node2_var!5,

node3_var!6))))

```
Rule? (rewrite "ordered?" +)
Rewriting using ordered?,
this simplifies to:
ordered?.insert.2
[-1] (FORALL (x: T):
             orderedf(node2_ver!5)
             IMPLIES ordered?(insert(x, mode2_ver!5)))
         (FORALL (x: T):
[-2]
             ordered?(node3_var!6)
             IMPLIES ordered?(insert(x, mode3_var!6)))
{1} (checkall((LAMBDA (y: T): y <= node1_var!4), node2_var!5)
AND checkall((LAMBDA (y: T): node1_var!4 <= y), node3_var!6)
AND ordered?(node2_var!5) AND ordered?(node3_var!6))
           IMPLIES ordered?(insert(x!7, mode(modei_var!4,
                                                 node2-var!5.
                                                 modeS_ver(6)))
Rule? (dslmp)
 Applying disjunctive simplification,
this simplifies to: ordered?_insert.2:
       (FORALL (x: T):
ordered?(node2_var!5)
              IMPLIES ordered?(insert(x, node2_var!5)))
          (FORALL (x: T):
              ordered?(node3_var!6)
              IMPLIES ordered?(insert(x, mode3_var!6)))
          checkell((LAMBDA (y: T): y <= node1_var!4), node2_var!5)
checkell((LAMBDA (y: T): node1_var!4 <= y), node3_var!8)
ordered7(node2_var!6)
          ordered?(node3_var!6)
        ordered?(insert(x!7, mode(model_war!4,
                                              node2.var!5
                                              node3_var(6)))
```

```
this simplifies to:
ordered?-insert.2:
         (FORALL (x: 1):
              ordered?(node2_war!5)
IMPLIES ordered?(insert(x, node2_war!5)))
          (FORALL (x: T):
[-2]
              ordered?(node3_var!6)
          IMPLIES ordered?(insert(x, node3_var!6)))
checkell((LAMBDA (y: T): y <= node1_var!4), node2_var!5)
checkell((LAMBDA (y: T): node1_var!4 <= y), node3_var!6)
[-3]
[-4]
 [-8]
          ordered?(node2_var!5)
          ordered?(node3_ver!6)
 [-6]
         ordered?((IF x!7 <= node1_var!4
                         THE
                         node (model_var!4,
                                insert(x!7, node2_var!5),
node3_var!6)
                      ELSE
                         node (node1_var!4,
                                node2_ver!5.
                                insert(x!7, node3_ver!6))
                      EMDIF))
 Rule? (lift-lf)
 Lifting IF-conditions to the top level, this simplifies to:
```

Rule? (rewrite "insert" +)

Rewriting using insert,

```
ordered?_insert.2 :
      (FORALL (x: T):
             ordered?(node2_var!6)
IMPLIES ordered?(insert(x, node2_var!5)))
         (FORALL (x: T):
             ordered!(node3_var!6)
        INPLIES ordered(insert(s, node3_var!8)))
checkell((LAMBDA (y: 7): y <= node1_var!4), node2_var!5)
checkell((LAMBDA (y: 7): node1_var!4 <= y), node3_var!8)
Ī-43
        ordered?(node2_var!b)
        ordered! (node3.var!6)
{1} IF x!7 <= node1_var!4
          THEN
          ordered?(node(node1_var!4,
insert(x!7, node2_var!5),
                            node3_var(6))
        ELSE
          ordered?(node(node1_var!4,
                            node2_var!5,
                            insert(x!7, node3_ver!6)))
        ENDIF
Rule? (propS)
By propositional simplification,
this yields 2 subgoals:
```

```
ordered?_insert.2.1 :
          x!7 <= node1.var!4
           (FORALL (x: T):
ordered?(node2_var!5)
                IMPLIES ordered?(insert(x, node2_var!5)))
           (FORALL (x: T):
                ordered?(node3_var!6)
          ordered*(nodes_varie)
INPLIES ordered*(insert(x, nodes_varie)))
checkall((LAMBDA (y: 7): y <= node1_varie), node2_varie)
checkall((LAMBDA (y: 7): node1_varie <= y), node3_varie)
ordered*(node2_varie)
[-4]
[-5]
[-6]
           ordered?(node3_ver!6)
{1} ordered?(node(node1_var!4, insert(x!7, node2_var!5), node3_var!5))
Rule? (rewrite "ordered?" +)
Rewriting using ordered*, this simplifies to:
 ordered?_insert.2.1 :
 [-1] x17 <= node1_var!4
           (FORALL (x: T):
ordered?(node2_var!5)
 [-2]
                IMPLIES ordered?(insert(x, node2_var!6)))
 [-3]
           (FORALL (x: 7):
           (FURALL (x: 1):
    ordered?(node3_var!6)
    IMPLIES ordered?(insert(x, node3_var!6)))
checkell((LAMBDA (y: T): y <= node1_var!4), node2_var!6)
checkell((LAMBDA (y: T): node1_var!4 <= y), node3_var!6)</pre>
 [-6]
           ordered? (node2_ver!5)
 [-6]
           ordered?(node3_var!6)
 [-7]
          (checkall((LAMBDA (y: T): y <= node1_var!4),
                           insert(x!7, node2_var!5))
                AND checkall((LAMBDA (y: T): nodei_var!4 <= y), node3_var!8)
AND ordered?(insert(x!7, node2_var!8))
AND ordered?(node3_var!8))
```

```
Rule? (quant?)
Found substitution:
 x gets x17,
Instantiating quantified variables,
this simplifies to:
ordered?_insert.2.1 :
          z!7 <= node1_var!4
          ordered?(node2_var!5) IMPLIES ordered?(insert(x!7, node2_var!5))
           (FORALL (x: T):
               ordered?(node3_var!6)
          IMPLIES ordered?(insert(x, node3_var!6)))
checkall((LAMBDA (y: T): y <= node1_var!4), node2_var!5)
checkall((LAMBDA (y: T): node1_var!4 <= y), node3_var!6)
 [-6]
          ordered?(node2.var!5)
 [-6]
          ordered?(node3.var16)
[1] (checkall((LAMBDA (y: T): y <= nodei_var!4), ...
insert(x!7, node2_var!5))

AND checkall((LAMBDA (y: T): node1_var!4 <= y), node3_var!5)

AND ordered?(insert(x!7, node2_var!5))
                     AND ordered?(node3_war(6))
 Rule? (prop$)
By propositional simplification, this simplifies to:
```

```
Rule? (rewrite "ordered?" +)
Rewriting using ordered?,
this simplifies to:
ordered?_insert.2.2 :
        (FORALL (x: T):
              ordered?(node2_war!5)
              IMPLIES ordered?(insert(x, node2_ver!5)))
          (FORALL (x: T):
         ordered?(node3_var!6)
IMPLIES ordered?(insert(x, node3_var!6))
checkall((LAMBDA (y: T): y <= node1_var!4), node2_var!6)
checkall((LAMBDA (y: T): node1_var!4 <= y), node3_var!6)
ordered?(node2_var!6)
[-3]
[-5]
         ordered?(node3_var!6)
[-6]
        x!7 <= node1_var!4
        (checkall((LAMBDA (y: T): y <= node1_var!4), node2_var!5)
{2}
              AND ordered?(insert(x!7, node3_var!6)))
Rule? (quant? -2)
Found substitution:
x gets x!7,
Instantiating quantified variables,
this simplifies to:
```

```
ordered?_insert.2.1 :
        ordered?(insert(x!7, mode2_ver!6))
        x!7 <= node1_var!4
(FORALL (x: 7);</pre>
[-3]
            ordered?(node3_var!6)
        IMPLIES ordered?(insert(x, node3_var!6)))
checkell((LAMBDA (y: T): y <= node1_var!4), node2_var!5)
checkell((LAMBDA (y: T): node1_var!4 <= y), node3_var!6)
[-6]
        ordered?(node2.var!5)
        ordered?(node3_var!6)
Rule? (rewrite "ordered?_insert_step")
Rewriting using ordered?_insert_step,
This completes the proof of ordered?_insert.2.1.
ordered?_insert.2.2 :
[-1] (FORALL (x: 7):
            ordered?(node2_var!5)
IMPLIES ordered?(insert(x, node2_var!5)))
        (FORALL (x: T):
            ordered?(node3_var!6)
IMPLIES ordered?(insert(x, node3_var!6)))
        checkell((LAMBDA (y: T): y <= nodel_var!4), node2-var!5)
checkell((LAMBDA (y: T): nodel_var!4 <= y), node3_var!8)
ordered?(node2_var!5)
[-4]
[-6]
        ordered?(node3_var!6)
    ordered?(node(node1_var!4,
                          node2_var!5,
                          insert(x!7, node3.var!6)))
```

```
ordered?_insert.2.2 :
        (FORALL (x: T):
            ordered?(node2_var!5)
         IMPLIES ordered (insert(x, node2_var!5)))
ordered (node3_var!6) IMPLIES ordered (insert(x!7, node3_var!6))
{-2}
[-3]
         checkall((LAMBDA (y: T): y <= node1_var!4), node2_var!5)
        checkall((LAMBDA (y: T): nodei_var!4 <= y), node3_var!6)
ordered?(node2_var!5)
ordered?(node5_var!6)</pre>
[-6]
       z!7 <= node1.var!4
       (checkall((LAMBDA (y: T): y <= node1_var!4), node2_var!5)
             checkell((LAMBDA (y: T): node1_var!4 <= y),
insert(x!7, node3_var!6))
               AND ordered?(node2.var!5)
                 AND ordered?(insert(x!7, node3_var!6)))
Rule? (prop$)
By propositional simplification,
this simplifies to:
ordered? insert.2.2 :
         ordered?(insert(x!7, node3_var!6))
{-1}
[-2]
         (FORALL (x: T):
             ordered?(node2_var!5)
             IMPLIES ordered (insert(x, node2_var 15)))
        chechall((LAMBDA (y: T): y <= nodel.var!4), node2.var!5)
chechall((LAMBDA (y: T): node1.var!4 <= y), node3.var!6)
ordered?(node2.var!5)
[-3]
[-4]
(-5)
         ordered?(node3_var!6)
       checkull((LAMBDA (y: T): nodei.var!4 <= y),
                     insert(x!7, node3_var!6))
       ri7 <= node1_var!4
```

```
Rule? (rewrite "ordered?_insert_step")
Rewriting using ordered?_insert_step, this simplifies to:
ordered7.insert.2.2 :
[-1] ordered?(insert(x!7, node3_var!8))
[-2] (FORALL (x: T):
              ordered?(node2_var!5)
              IMPLIES ordered?(insert(x, mode2.ver!6)))
         checkall((LAMBDA (y: T): y <= node1_var!4), node2_var!5) checkall((LAMBDA (y: T): node1_var!4 <= y), node3_var!6) ordered?(node2_var!6)
[-3]
[-5]
         ordered?(node3_var!6)
[-6]
        node1_var!4 <= x!7
        checkell((LAMBDA (y: 7): model_var'4 <= y),
insert(x'7, model_var'6))
[3] x!7' <= modei.var!4
Rule? (typepred "obt.<=")
Adding type constraints for obt.<-, this simplifies to: ordered?_insert.2.2:
         total_order ! [T] (obt . <=)
{-1}
[-2]
         ordered?(insert(x!7, mode3_war!6))
        (FORALL (x: T):
             ordered?(node2_var!5)
IMPLIES ordered?(insert(x, node2_var!5)))
       checkell((LAMBDA (y: T): y <= nede1_var!4), nede2_var!5)
checkell((LAMBDA (y: T): nede1_var!4 <= y), nede3_var!6)
ordered?(nede2_var!5)</pre>
[-6]
[-6]
         ordered! (node3_var!6)
[-7]
[1] node1_var!4 <= x!7
[2] checkell((LAMBDA (y: T): nodei_wari4 <= y),
                    insert(x!7, node3_var(6))
[3] x17 <= mode1_var14
```

```
Rule? (rewrite "total_order?")
Rewriting using total_order?,
this simplifies to:
ordered?_insert.2.2 :
          FORALL (x, y: 1): x <= y OR y <= x ordered?(insert(x!7, mode3_var!6))
          (FORALL (x: T):
              ordered?(mode2_var!5)
         INPLIES ordered?(insert(x, node2.var!5)))
checkall((LAMBDA (y: T): y <= node1.var!4), node2.var!5)
checkall((LAMBDA (y: T): node1.var!4 <= y), node3.var!6)
ordered?(node2.var!5)
[-4]
[-6]
[-6]
[-7]
          ordered!(node3_var!6)
        nodel_var!4 <= x!7
[1]
        checkell((LAMBDA (y: T): model.var!4 <= y),
insert(x!7, model.var!6))
[2]
[3] z!7 <= mode1_var!4
Rule? (quant?)
Found substitution:
y gets x!7.
z gets nodel_var!4,
Instantiating quantified variables, this simplifies to:
ordered?_insert.1 :
```

```
ordered?_imsert.2.2 :
        nodel_war!4 <= x!7 OR x!7 <= nodel_war!4
{-1}
[-2]
        erdered?(insert(x!7, mode3_var16))
(FORALL (x: 7):
[-3]
            ordered?(node2_var!6)
        INPLIES ordered?(insert(x, node2_var!6)))
checkell((LAMBDA (y: 7): y <= node1_var!4), node2_var!6)
checkell((LAMBDA (y: 7): node1_var!4 <= y), node3_var!6)
[-4]
[-6]
        ordered?(node2_var!5)
        orderedf(node3_ver!6)
[-7]
      nodei_var!4 <= x!7
checkall((LAMBDA (y: 7): nodei_var!4 <= y),
insert(x!7, node3_var!6))
[3] x!7 <= node1_var!4
Rule? (prop$)
By propositional simplification,
This completes the proof of ordered?_insert.2.2.
This completes the proof of ordered?_insert.2.
Save the new proof? (Yes or No) yes
Would you like a brief printout of the proof? (Yes or No) yes
ordered?_insert :
Inducting on A,
which yields 2 subgoals:
```

```
ordered?_insert.2 :
```

For the top quantifier in 1, we introduce Skolem constants:
(node1.var!4 node2.var!5 node3.var!6)
Applying disjunctive simplification,
For the top quantifier in 1, we introduce Skolem constants: (x!7)
Rewriting using ordered?,
Applying disjunctive simplification,
Rewriting using insert,
Lifting IF-conditions to the top level,
By propositional simplification,
which yields 2 subgoals:

ordered?_insert.2.i :

Rewriting using ordered?, Instantiating quantified variables, By propositional simplification, Rewriting using ordered?.insert.step, This completes the proof of ordered?.insert.2.1.

node3_var!6))

ordered?_insert.2.2 :

insert(x17, node3.var(6)))

Rewriting using ordered?,
Instantiating quantified variables,
By propositional simplification,
Rewriting using ordered?_insert_step,
Adding type constraints for obt.<=,
Rewriting using total_order?,
Instantiating quantified variables,
By propositional simplification,
This completes the proof of ordered?_insert.2.2.

O.E.D.

Notes on the Language

The core logic is a simply typed higher-order logic.

Specifications are structured into parametric theories.

Types can be parameters.

Assumptions can be used to constrain the parameters.

Set-like predicate subtypes can be defined. These make the domains and ranges of operations explicit.

Theorem proving is employed to carry out typechecking.

Automatic facility for generating abstract datatype theories.

15

Notes on the Proof checker

Sequent representation for proof goals.

Backwards proof construction by applying reductions.

Heavy use of powerful decision procedures for equality and inequality.

Powerful primitive inference steps. Roughly twenty such steps.

Strategy mechanism for encapsulating proof patterns.

Ability to save and rerun proofs and partial proofs, and display proofs.

Conclusions

PVS exploits the synergy between language and inference.

The combination of powerful inference steps: decision procedures, rewriting, propositional simplification, etc., makes it effective to develop proofs that are both certified and convincing.

Future goals:

- To enhance the language to further exploit the inference capabilities
- To generate readable proof outlines
- To make proofs robust and easier to maintain

Logical Foundations of Computing over the Floating Point Reals

Richard Platek Odyssey Research Associates, Inc.

Logical Foundations of Computations over the Reals

Richard Platek
Odyssey Research Associates
ORA

12 August 1992 NASA FM Workshop

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Two ORA Technical Reports

"Verification of Numerical Programs Using Penelope"

"Denotational Semantics of Numerical Programs"

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2



Basic Problem

What does it mean to say that a given program "computes" a real valued function such as sine x or e when it never really does?

Classical answer:

The program computes an approximation which is "sufficiently accurate"

But what does that mean?

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Two Fundamental Problem Areas

Scientific Computations

simulations, cacluation of engineering solutions, numerical experiments to explore theories, "number crunching" as part of experiments

correctness is vital for decision making

Embedded Computations

computers as part of coninuous systems

sense-compute-activate

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Botton Up Interpretation

We reason at the level of the CPU and Floating Point processor so that we can calculate tight error bounds and we use numerical analysis techniques to estimate the accuracy of the computation.

Perfectly fine, but too concrete

- A. Numerical Programs are not written in machine language or assembler. They are written in higher order languages like Fortran, C, Ada. The concrete analysis is not portable across CPU's.
- B. The concrete analysis is not portable across FPP's. We should reason in terms of the IEEE floating point standard or the Brown model.

In particular, our specs and proofs should be independent of the word length of the machine reals except in so far as the word length is knowable at the programming language level (e.g., Ada's float'small)

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	the state of the s	
	Verifying floating point computations	
0	Algebraic properties of floating point operations are a mess; and detailed descriptions are highly implementation dependent.	
0	Little automated support exists.	
σ	We are incorporating support for both quantitative and qualitative error analysis into Penelope.	
This talk concerns qualitative error analysis.		

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Sources of error

Roundoff er	ror
-------------	-----

- ☐ (Mathematical) Truncation error
- Implementation strategies (modeled by non-determinism)

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Example of Compiler Implementation Strategies

In both C and Ada the statements

may set w to either 0 or 1 !!!

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Qualitative error analysis

Intuitively: prove programs under the assumption that various sources of error are present but "negligible"

Not equivalent to assuming that error is non-existent

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Qualitative analysis of roundoff error: asymptotic correctness

Mathematical model via limits

If a program is run on increasingly accurate machines, then its answer approaches the specified result in the limit.

Mathematical model via algebra

Use a model of "approximate reasoning."

The algebraic model is easier to use

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10



Algebra for approximate reasoning

Introduce additional predicates on the "real numbers"

 $x \approx y$ x is close to y

 $x \not\approx y$ x is not close to y

 $x \lesssim y \quad x < y \text{ or } x \text{ is close to } y$

 $x \nleq y$ x < y and x is not close to y

Relations to standard operations

$$x = y \Rightarrow x \approx y$$

$$x \not \lesssim y \Rightarrow x < y \Rightarrow x \leq y \Rightarrow x \lesssim y$$

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Substitution in Approximate Reasoning

If f is continuous, $x \approx y \Rightarrow f(x) \approx f(y)$

Therefore,

 $x pprox x_1$ and $y pprox y_1 \Rightarrow x + y pprox x_1 + y_1$

But comparisons are not continous

 $x\approx y$ and $x\leq z$ does not imply $y\leq z$

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12



Algebra of approximate reasoning

Mechanical translation of (many) facts of ordinary algebra to facts of approximate algebra.

For example:

$$(x+1)^2 > x$$

translates to

$$(x+1)^2 \gtrsim x$$

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Modeling Ada floating point operations

Introduce specification predicate for each basic operation

fplus(x, y, z):

z is a possible result of evaluating x + y

Sample property:

 $fplus(x, y, z) \Rightarrow z \approx x + y$

fle(x, y, b):

b is a possible result of evaluating $x \leq y$

Sample properties:

 $fle(x, y, true) \Rightarrow x \lesssim y$ $fle(x, y, falsc) \Rightarrow x \gtrsim y$

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14



Example specification and proof

function mysqrt(a, small : in float) return float; should compute the square root of a to within small

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Naive specification of mysqrt

IN a \geq 0.0 and small > 0.0 RETURN z SUCH THAT $|z^2-{\bf a}| \leq {\rm small}$

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Amended specification of mysqrt

IN a \geq 0.0 and small \gtrsim 0.0 RETURN z SUCH THAT $|z^2-a|\lesssim$ small

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Calculation will use Newton's method

For any $a \ge 0$,

 $\sqrt{a} = \text{limit}_{i \to \infty} x_i$

where

 $x_0 = a+1$ $x_{i+1} = 1/2(x_i + a/x_i)$

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18



Code for mysqrt

```
function mysqrt (...) is
    x : float;
begin
    if (a <= small) then
        return 0.0;
    end if;
    x := a + 1.0;
    while (x*x-a >= small) loop
        x := (x+(a/x))/2.0;
    end loop;
    return x;
end mysqrt;
```

Loop invariant annotation:

small,
$$x$$
, a , $(x^2 - a) \gtrsim 0.0$

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Proving termination of the loop

Proving termination of the loop

Loop bound annotation:

loop bound $x^2 - a$ contraction 1/4 lower bound small

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20



Accurate Square Root

function sqrt (a:= in float) return float

is

begin

return mysqrt (a, float'small);

end;

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Embedded Systems

Want to be able to reason about computer controlled real world systems. Want to know what the system does in real space/time.

The total syste can be described by logico-differential equations.

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22



Example

State variables

x(t : Real) : Real
y(k : Int) : Int

Transition Relations

$$\frac{dx}{dt} = f(x(t), y(t))$$

y(k+1) = g (x(1), y(k))

t₁ = max integer ≤ t

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Formal Safety Analysis

Nancy Leveson University of California at Irvine A System Engineering Approach:

· Identify system hazards

• Evaluate or prioritize hazards

As define required functionality and allocate to components:

Apply formal hazard analysis to emerging design Optimize design for safety and other constraints

Identify and resolve potential conflicts

Results in identification of particular behaviors of individual components that could contribute to a system hazard.

- After completing allocation of functionality, do system and subsystem hazard analysis to ensure requirements specification of each component consistent with system safety constraints.
- Design and build components with safety constraints in mind (design safety into individual components).

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SOFTWARE SAFETY RESEARCH

Nancy G. Leveson University of California, Irvine (university of washingrou)

A Safety-Oriented Software Methodology

System Requirements Specification and Analysis

Modelling language

Analysis Criteria and Procedures

System Hazard Analysis

Determine whether system can reach a hazardous state if:

Performs as specified

Plausible or likely failures occur

Special and standard hazard analysis techniques

· Design for Safety

Design for protect against safety failures

Analyze design for safety

To aid in construction of safety features

To minimize and protect safety-critical code

To produce a verifiable and certifiable design.

Code Verification

Informal, formal, semi-formal techniques

Software Fault Tree Analysis

Analysis Criteria and Procedures

System Hazard Analysis

Determine whether system can reach a hazardous state if:

Performs as specified

Plausible or likely failures occur

Special and standard hazard analysis techniques

Design for Safety

Design for protect against safety failures

Analyze design for safety

To aid in construction of safety features

To minimize and protect safety-critical code

To produce a verifiable and certifiable design,

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Code Verification

Informal, formal, semi-formal techniques

Software Fault Tree Analysis

SOFTWARE HAZARD ANALYSIS

1) If operates "correctly," will any hazardous states result?

SOFTWARE HAZARD AND REQUIREMENTS ANALYSIS

2) If there are failures, will hazards result?

Single failures?

Multiple failures?

APPROACHES ENDUCTIVE

· reasoning from individual to general

· reasoning from general to specific

A P PROACHES

DEPUENN

· determine what system states possible

system state an occur · determine how given

· postulate system has failed could cause or contribute in certain way + thy to find out what behavior effect in system operation · postulate Particular fault or untating condition + attempt to ascertain

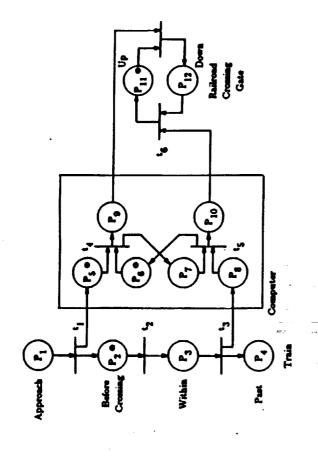
parhedus emtral surbeer after Augist of aircraft

e.g. how will loss of some

could have caused it? e.g. Hane enshes, what

· for complex systems, impressible o difficult to find all course. to wenthy all possible component sequences forlure modes

. when subsystems put together, new failure modes my appear



The Figure 2, A Petri Net Graph with the Next State Shown

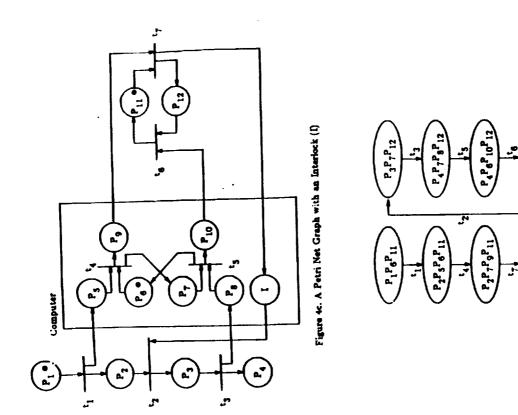
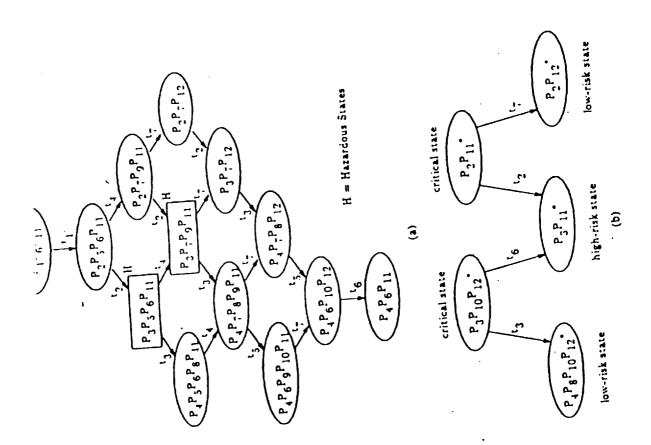


Figure 4d Reachability Graph for Figure 4c



Types of control failures:

a required event that does not occur

an undesired event

an incorrect sequence of required events

two incompatible events occurring simultaneously

timing failures in event sequences

exceeding maximum time constraints between events

failing to ensure minimum time constraints between events

durational failures

Figure 5a. Desired Event t1 Does Not Occur

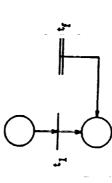


Figure 5b. Undesired Event t₁ Occurs

Jaulty state: every path to it from the initial state contains a failure transition.

cess is not lost, and in an acceptable amount of time, it will return to Recoverable: after the occurrence of a failure, the control of the pronormal execution.

- 1) the number of faulty states is finite
- 2) there are no terminal faulty states
- 3) there are no directed loops containing only faulty states
- to a correct state is less than a predefined acceptable amount of 4) the sum of the max times on all paths from the failure transition time.

correct behavior path: a path in the failure reachability graph from the initial state to a final state which contains no failure transitions.

1) a correct behavior path is a subsequence of every path from the Fault Tolerant Process.

initial state to any terminal state.

2) the sum of the maximum times on all paths is less than a predefined acceptable amount of time.

Feil-Safe: all paths from a failure F contain only low-risk states.

PETRI NET MODELS

Have developed analysis procedures to:

- identify hazards and safety-critical single and multiple failure sequences
- determine software safety requirements including timing prequirements
- analyze the design for safety and fault tolerance
- e. guide in the use of failure detection and recovery procedures

Analysis of Completeness in Requirements Specification

- Most of accidents involve software requirements deficiencies.

 Many (if not most) of failures associated with requirements involve incompleteness.
- Completeness (informally): Requirements must be sufficient to distinguish the desired behavior of the software from that of any other, undesired program that might be designed.
- Completeness vs. sufficiency
- Relative to life cycle phase.

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Approaches to finding errors in requirements specifications:

- Prototyping
- Executable specifications
- Scenarios
- Informal reviews
- Formal modeling and analysis

Build model of software behavior and its interface with other components and analyze to ensure behavior and properties of model match desired behavior and properties.

GENERAL APPROACH:

1) Model the:

Required black-box behavior of the software, Interfaces with the rest of the system,

Basic assumptions about behavior of other components. In System of environment.

- 2) Analyze model to:
- Ensure modeled software behavior implements required control function,
- Ensure modeled software behavior satisfic required constraints (including safety),
- Ensure modeled system behavior is fault tolerant and robust in the event of component failures,
- Identify and resolve conflicts and tradeoffs.

REQUIRES:

A formal modeling language

Analysis criteria and algorithms

Validation on a realistic testbed

System Supplies of variables | Process | System Oo |

Manipulated variables | Process | System Oo |

Accustor | Constrol Comment | T |

Output | Constrol Comment | T |

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Figure 1: The control loop

The RSM is denoted as a seven-tuple $(\Sigma,Q,q_0,P_T,P_0,\delta,\gamma)$ where:

- Σ is the set of input/output variables, I and O,
- Q is the set of states of the control component C.
- $90 \in Q$ is the initial state of C; the software is in this state before startup.
- Pr is the set predicates on the values and timing of the inputs (I). They state change in the RSM.
 - ullet P_O is the set of predicates on the outputs (O)
- δ is the state transition function $Q \times P_T$ to Q.

/ is the trigger-to-output relationship $Q \times P_T$ to P_O .

186

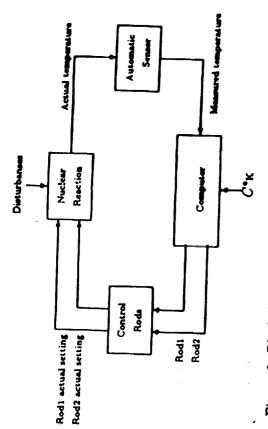


Figure 2: Block diagram of the temperature control system.

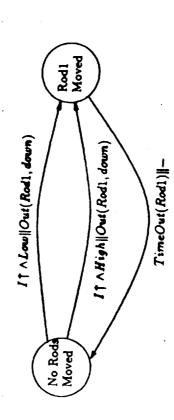


Figure 3: A fragment of an RSM



Input/Output variables (Σ)

• States (Q, q_0)

Startup and Shutdown Modes

Trigger Predicates (P_T)

Taurology Requirements
Essential Value Assumptions
Essential Timing Assumptions
Properly bounded ranges
Capacity and Load
Minimum arrival rates, etc.

Criterion 6.1 Every state must have a behavior (transition) defined for every possible input. Formally,

$$\forall I,q \exists q_1,p: (\delta(q,p)=q_1) \land (p \in P_{T_i})$$

where $I \in \Sigma$, q, $q_1 \in Q$ and P_{T_i} is defined as in section 4.

Criterion 6.2 The logical OR (v) of the input predicates on the transitions out of any state must form a tautology:

where the p_i s are the input predicates leading out of the state of interest.

Criterion 6.3 Every state must have a behavior (transition) defined in case there is no input for a given period of time, i.e., a timeout.

Criterion 6.4 The RSM must to be deterministic. Let p. represent the input predicate on the ith transition out of a state. Then deterministic behavior is guaranteed by:

$$\forall i \forall j (i \neq j) \Rightarrow \neg (p_i \land p_j)$$

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• Output Predicates (P_O)

Environmental capacity assumptions
Data Age
Latency

Trigger-to-Output Relationship (y)

Graceful Degradation and Hysteresis Responsiveness and Spontaneity (Feedback)

Transitions (δ)

Basic Reachability

Recurrent Behavior

Reversibility

Reachability of Safe States

Path Robustness

Constraint Analysis

REVERSIBILITY

an operation y (performed in a state $q \in Q_y$) requires a path between q_x and a state belonging to Q_y . Formally, Reversibility of an operation x (performed in a state qs) by Criterion 9.3

 $\exists q\exists s: (\hat{\delta}(q_x,s)=q)\wedge (\phi(s_i)).$

where $q \in Q_y$.

Ann Robustudes

hazard-reducing outputs. Formally, let Q_s and Q_y be the sets of states where actions x and y are performed. The loss Soft and hard-failure modes should be eliminated for all of the ability to receive I is a soft-failure mode for the paths from action x to action y iff Criterion 9.5

 $\exists q \forall q_1, s[(\hat{b}(q,s) = q_1) \Rightarrow (\neg \phi(s_i) \lor I \uparrow)]$

where $q \in Q_x$ and $q_1 \in Q_y$. The loss of the ability to receive I is a hard-failure mode iff

 $\forall q \forall q_1, s[(\dot{\delta}(q,s) = q_1) \Rightarrow (\neg \phi(s_i) \lor I \uparrow)]$

where $q \in Q_x$ and $q_1 \in Q_y$.

Path robustness and safety:

Soft failure mode: loss of ability to receive an particular input could inhibit a particular output event.

Hard failure mode: loss will inhibit the event.

The more failure modes a set of requirements contains, whether soft or hard, the less robust will be the system that is correctly built to that specification.

Note that robustness in this sense is not only attribute that needs to be considered when specifying requirements and may not even be desirable, e.g., may conflict with safety.

An unsafe state should have at least one, and possibly several, hard failure modes for the production of an unsafe output command: No input received from proper authority, no weapons launch.

A fail-safe system should have no soft failure modes, much less hard ones, on paths between dangerous and safe states.

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Criterion 9.4 There must be no paths to undesired hazardous states.

 $\forall q_s, q_h, s \ (\hat{\delta}(q_s, s) \neq q_h) \lor (\neg \phi(s_i))$

where $q_s \in Q_s$ and $q_k \in Q_k$.

Criterion 9.5 Every path from a hazardous state must lead to a safe stat.

 $\forall q_h, s \; ((\hat{\delta}(q_h, s) = q) \wedge (\phi(s_i)) \Rightarrow (q \in Q_s))$

Criterion 9.6 If a safe state cannot be reached from a hazardous state all paths from that state must lead to minimum risk states

 $\forall q_{h} \ (\forall q_{o}, s \ ((\hat{\delta}(q_{h}, s) \neq q_{o}) \lor (\neg \phi(s_{i}))) \Rightarrow \\ \forall s, q \ ((\hat{\delta}(q_{h}, s) = q) \land (\phi(s_{i})) \Rightarrow q \in Q_{MinRich})).$

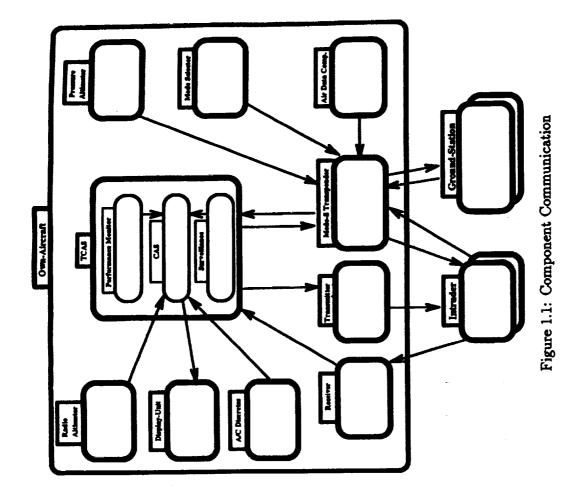
TESTBED:

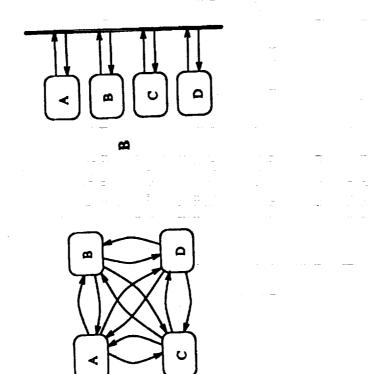
TCAS II: Traffic Alert and Collision Avoidance System

- Family of airborne devices functioning independently of the ground-based ATC system.
- Provides traffic advisories to assist pilot in avoiding intruder aircraft.
- Provides resolution advisories (recommended escape maneuvers) in a vertical direction to avoid conflicting traffic.
- Communicates with intruder aircraft TCAS systems, transponders on intruder aircraft. pilot, and ground-based radar beacon system.
- Used by airline aircraft and larger commuter and business aircraft.
- We will provide a system requirements specification and a safety analysis of the specification.

DESIGN CRITERIA FOR THE SPEC. LANG. -

- · black box behavior ruly
- · minimatica
- · simplicaty
- cohurnay, constatuay, concisentas
- · unambiguous, underlying language must have a formal foundation for emelysis
- . readable, renewable, usable by developers
- · use notation to bust convey type of intermetron graphuse, symbols, totales
- · when recessory, chrose redubility our writability · overcome personal protocess
- · information exposure

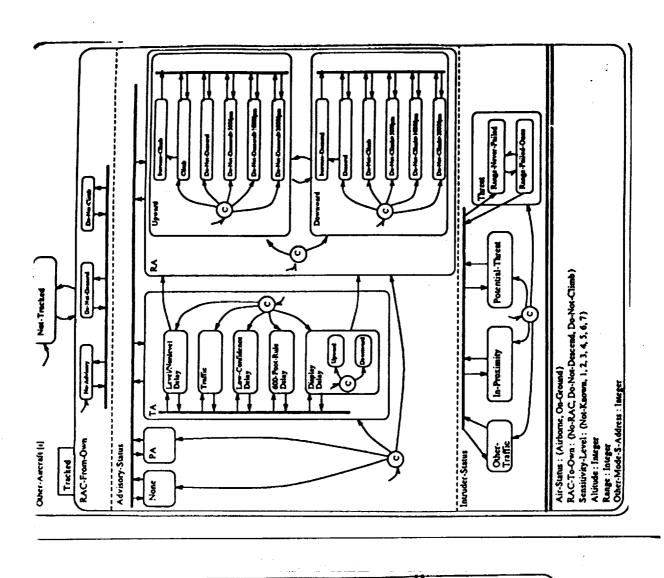




Power-On Fully-Operational Own-Aircraft, i:[1..30] Mode-S-Ground-Station, i:[1..15]

Contents

8 9 12 e 8	29 30 10 5	167 168 193 279	287 291 307
1 High Level Requirements 1.1 Goals 1.2 Constraints	 2.1 Component Communication Interfaces 2.2 Communication Protocols 2.3 Behavioral Assumptions 	3 TCAS 3.1 Own Aircraft 3.2 Other Aircraft 3.3 Mode S Ground Station	A Glossary B Reference Algorithms C Notation



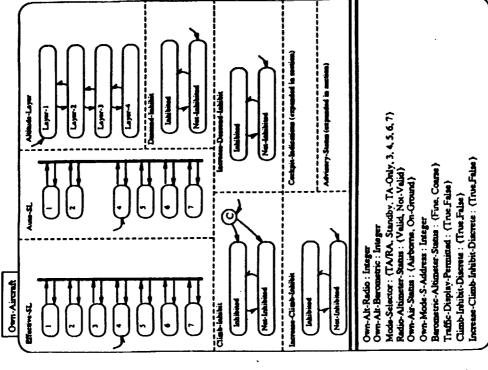


Figure 1.2: Own-Aircraft

Variable: Own-Alt-Radio Location: Own-Aircraft, 10

Source: Radio Altimeter

Type: Integer

Expected Range: -20...2150

Granularity: 1...10 is acceptable

Units: Feet

Load: 1/s for CAS. (hardware sends more often)

Exception handling information: Need valid data indicator. CAS should have a period of coasting before ignoring radio altitude when data is no longer valid. Large negative values must be handled.

Description: Feet above ground level (AGL)

thus affecting logic switchpoints based on altitude above ground. Hardware can be analog or digital. Analog input to TCAS box is in a voltage range that must be converted to ft. Comments: Hardware differ in available range. A smaller range will cause radio altitude status to become invalid at a lower altitude above ground than intended by the CAS logic, Digital input is in binary via 429 data word.

Transition(s): Threat - Other-Traffe

Location: Other-Aircraft . Intruder-Status...

Trigger Event: Effective-SL-Evaluated-Event

Condition:

Range-Validm 148 Proximate-Traffic-Condition 133 Other-Alt-Reporting - 53 = True Potential-Threat-Conditions 134 Bearing-Validm-148 AND

Output Action: Intruder-Status-Evaluated-Event

Description:

Columns 1-2 Non-altitude-reporting and either the bearing or range inputs are invalid.

Column 3 Non-altitude reporting and both range and bearing are valid, but neither the pronor potential threat classification criteria are satisfied.

Macro: Proximate-Traffic-Condition Definition:

OR	E	F	F-	·	Ŀ
	Other-Air-Status, se in state Airborne	Other-Tracked-Rangeries < 6.0 nmirrorga	Other-Alt-Reporting, a True	Own-Tracked-Altrisi > 15500 ft, anovency	Current-Vertical-Separations, 135 < 1200 (tenora)
			AN		

To be considered In-Proximity the intruder must be within a range c 6.0 nmigraoxa). Additionally, if the intruder is altitude reporting, its relative altitude mus be within 1200 ftenoxa. If the intruder is not altitude reporting, then it considered proximat traffic only if own altitude is below 15500 ft, and the bearing and range reports ar considered valid. Description:

MOPS Ref. TRAFFIC ADVISORY. Proximity test.

Return type: $(-10000...+\infty)$ Definition: Climb-Goal Function:

Climb-Goal =

Composite-RA-se in state No-RA or

Climb-VSL in state No-Climb-VSL

if Climb-VSL in state VSL2000 if Climb-VSL in state VSL1000 if Climb-VSL in state VSL500

-2000 ft/min p. cumaconum -1000 ft/min (P. CLIMBOOAL(3)) -10000 ft/min_{(*)#8683}

max(1500 ft/min, Alt-Rate-Pos-RA-es[Each]) -500 ft/mine clinesoades 2500 ft/minge mc clumate) 0 ft/ming cumscoaus)

if Composite-RA-so in state Climb . Nomin if Composite-RA-10 in state Climb . Increas if Climb-VSL in state VSL0

Note: if Alt-Rate-Pos-RA-48[i] is not defined for Other-Aircraft, 77[i], then do not consider it into the max above. Also note that all positive RA's are in the same direction.

Reference: MOPS: Determine goal rate (p. 389).

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· Simulator (FALL '92) formulas definition of language done

· TEST DATA GENERATAR (ELANT WEYNERR-NYU)

· ANALYSIS TOOLS

[model cheeker] [automotic deduction]

"completuness" and robustness checker (Semantic analyzer)

software hazard analyteer
11sk assessment and system hazard analyses
1.9. FINSA
1.9. FINSA
1.9. FINSA
1.9. FINSEA
1.9. FINSEA

· DEVELOPMENT TOOLS

ANALYSIS

Software Hazard Analysis

Semantic Analysis of Requirements

"Completeness" Robustness System Engineering Analyses

ASSESSMENT

The FM9001

Warren Hunt Computational Logic, Inc.

FM9001 Verification and its use in the A Formal HDL

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Tel: +1 512 322 9951 FAX: +1 512 322 0656

Hunt@CLI.COM

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Talk Topics

- Hardware Verification
- The FM9001
- Examples of our HDL
- The FM9001 proof effort
- Conclusions

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Solution Approach

We use the Boyer-Moore logic as our hardware specification vehicle.

specifies the operation of a hardware component.

With respect to digital systems, we want to:

Completely replace programmer's manuals,

timing diagrams, interface specifications,

power requirements, etc. with clear precise

Provide a perfectly clear foundation upon

which systems can be built.

We envision providing a mathematical statement,

which we call a formula manual, that completely

Hardware Verification: What is It?

Some benefits of using a formal logic are:

- logic expressions are quite compact,
- single interpretation of each logical formula, and
- a clearly defined set of axioms and rules of inference exists.

A mechanization of the Boyer-Moore logic, known as the Boyer-Moore theorem prover, provides us with:

- a definition and formula data-base manager,
- an automatic theorem prover and interactive proof checker, and
- the ability to execute our (hardware) definitions.

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formulas.

Boyer-Moore Logic Usage

Within the Boyer-Moore logic we:

- axiomatize properties of digital logic circuits,
- formalize our HDL, and
- write specifications.

The mechanization of the logic insists on:

- uniqueness of definitions and
- rigorous proofs.

constructed—larger than can be carried out by hand. The mechanization allows very large proofs to be

The FM9001 Fabrication

we manufacture mathematically modeled circuits and This fabrication effort is a test-of-concept; that is, can get them working?

our implementation description includes the test logic. many engineering issues as possible; for example, We are attempting to deal mathematically with as

The FM9001 microprocessor is a 32-bit, generalpurpose microprocessor with:

- 32-bit addressing,
- 16 general-purpose registers,
- two-address architecture,
- 5 addressing modes,
- a 16-function ALU, and
- conditional result assignment.

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OP-CODE	OF-CODE OPERATION	DESCRIPTION	STORE-CC	CONDITION
0000	• > 9	More	0000	Curry clear
1000	b <- a+1	Increment	1000	Curry set
0100	b <- a+b+c	Add with carry	0010	Overflow clear
1100	b <- b+a	Y q q	1100	Overflow set
0010	b <- 0 -> d	Negation	0100	Not negative
1010	b <- a - 1	Decrement	1010	Negative
0110	b <- b-e-c	Subtract with borrow	0110	Not zero
0111	b < b-1	Subtract	1110	Zero
1000	b <- a>>1	Rotate right through curry	1000	Higher
1001	b <- a>> 1	Arithmetic shift right	1001	Lower or same
1010	b <- a>> 1	Logical shift right	1010	Greater or equal
101	b <- b XOR :	XOR	101	Less
1100	b < bOR a	ğ	1100	Greater
1101	b <- b AND	AND	1011	Less or equal
1110	b <- NOT	NOT	1110	Ę
===	b < a	Move	1111	Felse

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The FM9001 Architecture

The FM9001 implementation architecture has:

- a pipelined, hard-wired control unit;
- a programmable program counter; and
- three asynchronous inputs: reset, data acknowledgement, and hold.

The FM9001 internal state (expect for the register file) is connected together into a scan chain. The FM9001 register file can be tested using the scan chain.

The next slide displays the FM9001 internal architecture.



DATA-IN **♀** DBC/ HOLD DADA/ DTACK FM9001 A-RBG REGISTER FILE RESET CNTL-STATE PC-RBG NT/ 0 > Z N 8

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LSI L1A6477

FM9001

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0.0101

A: Addro CTR: CH-eta D: Data-b DR: Disable DTCK: Disable Rt.G: Flags

The FM9001 Pinout

Valiak

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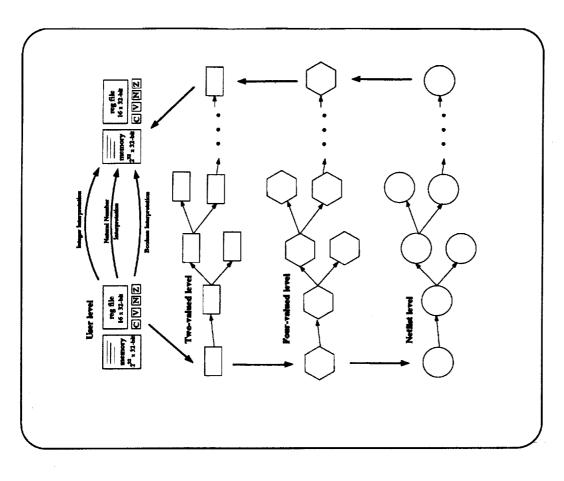
The FM9001 Specification levels

The FM9001 is specified at four levels:

- user,
- two-valued,
- four-valued, and
- netlist.

Each level is specified as an interpreter, except the netlist level.

The netlist is given meaning with our unit-clock simulator.



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The FM9001 Implementation Specification

Our HDL provides our lowest-level model for the FM9001 implementation:

- every internal gate and register is described, and
- every I/O pad buffer is defined.

Our HDL specification also includes all of the internal test logic.

We have proved the correctness of our FM9001 HDL description.

A Formal HDL

We have formalized a netlist-based, hierarchically-structured, occurrence-oriented hardware description language (HDL) using the Boyer-Moore logic.

- A predicate recognizes well-formed circuits.
- An interpreter defines the logical semantics.

Well-formed circuits contain:

- well-formed module, input, and output names;
- no combinational loops;
- · no loading and fanout violations; and
- no wire type (clock, Boolean, tri-state) mismatches.

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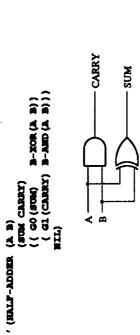
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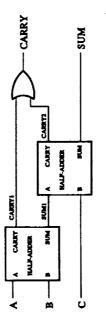
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Circuit Examples



The following full-adder specification refers twice to the half-adder specification above.

```
((TO(SUNI CARRYI) HALF-ADDER(A B))
(TI(SUNI CARRYZ) HALF-ADDER(SUNI C))
(T2(CARRY) B-OR(CARRYI CARRYZ)))
(FULL-ADDER (A B C)
(SUM CARRY)
```



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Translating Into LSI Logic Format

With just a few lines of Lisp program code, we are able to convert our full-adder boxlist into a form acceptable to LSI Logic.

CONTINE; DIRECTORY MASTER;

```
(( TO (FORG CARBET) BALF-MODER (A N))
( T1 (FOR CARBET) BALF-MODER (FORG C))
( T2 (CARBET) B-OR (CARBET) CARBET)))
HT1)
( (PULL-ADDER
(A B C)
(FUR CABEZ)
                                                                                                      TO (FORE, CARRY) = HALF-ANDER (A.B.);
TI (FORE, CARRY) = HALF-ANDER (FORE, C);
TE (CARRY) = ORE (CARRY), CARRYE);
                                           DOTEOTE FOR, CAUSE;
MODULA FULL-ADDER;
                         DATE ALB, C;
```

((00(stan) 8-308 (A B)) (01(camer) 8-300 (A B))) MILL)) (a a) (area cases) HALF-ADORR 00 (FCM) = BO (A, B); 01 (CABOT) = BHZ (A, B); COTFORE FOR CARRY LEVEL FORCETOR; HODOTE BALF-MORR

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Tri-state Circuits with Latches

A Circuit with Tri-state and Latches

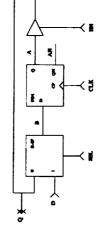
The following is a circuit with two latches that can

exchange values over a tri-state bus.

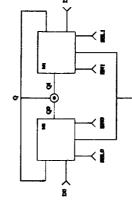
Below are pictorial representations of modules M1 and

를

Module M1 defines the module used on both ends of



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Module M2 defines a bus interconnecting two M1 modules.

(SEL D Q))
(B CLK))
(EN A)))

(B) B-IF (A AN) FD1 (Q) T-BUF (

(Q) ((MUX (LATCH (TBUF (AATCH)

(MI (CIK EN SEL D Q)

the bus.

(M2 (CLK ENO EN1 SELO SEL1 DO D1)

(CLK END SELO DO Q)) (CLK EN1 SEL1 D1 Q)) (Q0 Q1))) (Q) ((OCCO (QO) MI (((OCCI (QI) MI (((WIRE (Q) T-WIRE ((

This is similar to the FM8502 memory interface,

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Verified Synthesis

Using our HDL, we have been able to verify that circuit generating programs synthesize correct circuits.

We perform synthesis by

- writing circuit generator programs,
- verifying the circuit generator programs, and
- then executing the generators to generate correct circuits by construction.

In other words, a synthesized circuit has already been proved correct.

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An ALU Generator

We have an arbitrary size, 16-function ALU generator which is:

programmable—ALUs with different internal

structure can be produced;

- "intelligent"—internal buffers are only added when needed; and
- has been verified to generate correct n-bit, gatelevel ALU descriptions.

The FM9001 netlist is constructed by a Boyer-Moore function.

Summarized below are some characteristics of the

ALUs generated by our verified ALU generator.

Delay 12

Fanout

Gate Count 126

8 5 5 7

00

ALU Characteristics

7

4

2 bits

4

8

4 bits

ន

297

8 bits

8

491

16 bits

8

88

32 bits

8

1665

64 bits

3227

128 bits

30

ALU Generator Output Summary

The FM9001 Netlist

Most of the modules in the netlist are synthesized from *n*-bit module descriptions.

The FM9001 netlist contains over 91,000 characters in 2215 lines.

There are 85 modules that reference 1800 primitives of 48 types.

On average, each primitive output is connected to 3.4 other primitives.

There are 95 I/O pins, 32 are bi-directional.

It only takes a few seconds to generate these ALUs.

fm0001 mes; 23

3 December 1991

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fm0001.mms: 24

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3 December 1991

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The FM9001 Correctness Theorem

An abstract statement of the proof is below.

Jimplementation, 3clock

FM9001_specification(user_state,n)

map_up(simulate(map_down(user_state), implementation, clock)) We break the statement of the proof into five pieces.

Prettyprinted	11106 915	197	3459	3479	1942	
	User-lavel semantics of FM9001	Statement of theorem	Semantics of HDL	TM9001 implementation description	Existential witness for the clock	

9992

Total:

The FM9001 Mechanical Proof

Our FM9001 definition and lemma input script contains 2957 entries; these entires expand into 4851 theorem prover events.

For the Boyer-Moore theorem prover to check the FM9001 input script takes about 4 hours on a Sun SparcStation 2.

A comparison to some other proofs is given below (see A Computational Logic Handbook.)

Number of lines in understandable statement	ent	Max concept depth in proof	Number of supporters	Lines of supporters	Depth of proof		18	58	97
derstand	Concept depth of statement	pt depth	ber of s	Lines		_	2171	20002	28784
무	epth o	00000	Man	-	_	_	230	1741	1894
1100	cept d	X	_	-	-	_	152	48 40414	128
er of	Č	_	-	_	_	_	157	8	120
	_	_	-	_	_	_	991	864	1112
							85 TM8501	86 Goedel	91 m60001

CEL

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3 December 1991

Undetectable FM9001 Faults

CLOCK-PRO (PI): 0 CLOCK-PRO (PI): 0 EVEN DE (PI): 0 EVEN DE (PI): 0 EVEN DE (PI): 0 EVEN DE (PI): 1 EV				
# 10			i	•
## 1		87.40		•
TO MC/1/ 1677 1890 1874 1890 1874 1890 1874 1890 1874 1890 1874 1874 1874 1874 1874 1874 1874 1874	CHITYCH (F):0	2060		•
#0 ME/4/ 1743 1750 1750 1750 1750 1750 1750 1750 1750		151		• •
# 14.3 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0 ## 19.0	E-PAD (PT) :1	23/4	Î	• •
TO MC/6/ 6743 THO		6743	-	•
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1678 1211 170 ME/1/ 8077 009 33 8075 009 33 4923 009 33 4923 009 33 9):1 391 009 33 601 009 33 601 009 33 1699 000 100 1700 000 100 1700 000 100 1833 000 100 1834 000 100 1835 000 1835 000 1835 000 1835 000 1835 000 1835 000 1835 000	DRITTOR (III) : 1	5061		•
TO MC/1/ 8077 UNF 33 1075 UNF 33 4923 UNF 33 4923 UNF 33 1075 UNF	CHITOR(8):1	1678	1	
#0 MG/1/ #075 UDF 3 # #075 UDF 3 # #075 UDF 3 # #077 UDF 3 # #078 UDF 3 # #078 UDF 3 # #078 UDF 3 # #078 UDF 3 # #079 UDF 3 # #079 UDF 3 # #076 UDF 3 # #077 UDF 3	I-PAD (FI) :1	9744		• •
## 100	5 OHIE -			•
# 6925 UDF 3 4 6 2 2 UDF 3 4 6 2 2 UDF 3 4 6 2 2 UDF 3 4 6 2 UDF 3 4 6 1 UDF 3 4 0 UDF 3 4 0 UDF 3 4 U		5077		8
## 4925 UNF 3 3 1	ADDR-007-PADS/0.0(MK/3):1	8075	8	2
# 1.1	· · · · · · · · · · · · · · · · · · ·		i	1
#):1 397 UNF 3 B):1 397 UNF 3 601 UNF 3 601 UNF 3 1699 UNF 3 1700 UNF 3 1700 UNF 3 1833 UNF 3 1834 UNF 3	T: (7/000) A: A / 000 - A / 000		8	7
9):1 391 UNG 2 601 UNG 2 601 UNG 2 1,699 UND 1,700 UND 1,700 UND 1,700 UND 1,700 UND 1,700 UND 1,700 UND 1,800 UN	ACA-1908-1908/0.0 (191/3):1	4923	B	ï
## 1.1 391 UDF 3.2 D UDD	DODY/A-1884/4.0 (CP):1	788	B	Ħ
601 UNDERTREED CONSTORT 1699 UND 1700 UND 1700 UND 1700 UND 1807 UND 1838 UND 1834 UND 1845 UND	ODY/CVIE-FLAGS/G-LANCE(GF):1	166		ä
1699 UND 1700 UND 1700 UND 1700 UND 1700 UND 1700 UND 1833 UND 1834 UND 1834 UND 1834 UND 1834 UND 1834 UND 1837 UND 1837 UND 1837	**************************************	601	B	#
1699 UND 1700 UND 1700 UND 1877 UND 1834 UND 1834 UND 1834 UND 1834 UND 1834 UND 1834 UND 1834 UND 1837 UND 1837 UND		CORROR		
1700 UND 8076 UND 8076 UND 1833 UND 1834 UND 1894 UND 1897 UND 1987 UND 1987 UND 1987 UND	 DDB-007-PADS/0.0 (BM/1):0	1699	•	•
8076 UND 1833 UND 1834 UND 1834 UND -29 (A) :1 9442 UND 1 96 (S) :1 9877 UND 1 96 (S) :1 9877	DDB007-FADS/G.0 (BE/1) :1	1700		• •
8074 000 1833 000 1834 000 1834 000 -36(5):1 9442 000 1 98(7):1 9877	DDR-COT-PADS/Q.0 (NW/2);0	5076		• •
1833 CMD 1834 CMD 1834 CMD -26 (5) :1 9442 CMD 1 9877 CMD 1 8874 CMD	MDB001-1MDS/G.0 (MM/3):0	B074	8	•
29 (A) :1 9442 UND -36 (C) :1 947 UND -1 1 9477 UND -1 1 88774 UND	0. (1/2m2)		!	•
+29 (A) : 1 9442 CMD +29 (A) : 1 9442 CMD +36 (C) : 1 9877 CMD +36 (C) : 1 8874	5 (7 (m)) : (m) (m) (m) (m) (m) (m) (m) (m) (m) (m		3	•
29 (A) :1 9442 36 (C) :1 9577		1634	•	•
36 (C) :1 8577	COX/MESS-STACE/MESSACE/G-29 (A) : 1	2776	8	۰
200	COY/MEXT-STATE/MESTATE/0-36(C):1	772	ê	•
	ODY/NEGS/MOX-CONTRIDE (C) : 1	200		•

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undefined and undetectable faults.

Notice on the next slide the duplication of the

Our testing approach is to build a design that can be

tested using a single, stuck-at fault model.

We needed to be able to test the FM9001, as the

manufacturing process is flawed.

Testing the FM9001

SUMMATION PARAMETERS	FEC's	FAULTS REPRESENTED
Fotal Faults Faults tied to MC/0/ or /1/	9559	13098
Total Faults Sampled :	1916	12633
Faults included this run : Faults ancluded this run :	1367	1415
PAST CUMULATIVE RESULTS		
Varsion A Fmit Coverage (*): 72 B Fmit Coverage (*): 82 J Fmit Coverage (*): 82 J Fmit Coverage (*): 83 Fmit Coverage (*): 83 X Fmit Coverage (*): 83 K Fmit Coverage (*): 83	72.89 - 76.69 82.03 - 85.77 82.89 - 87.18 83.83 - 88.05 85.08 - 89.25 85.08 - 89.25 85.19 - 89.28	76.17 - 79.01 85.89 - 88.36 86.43 - 89.61 87.25 - 80.50 88.80 - 91.92 88.96 - 91.92 95.46 - 94.99

HOUST MAKE - FRANK NEWSTAN (0-29 (A) 1.1 BODY NEXT - FRANK NEWSTAN (0-36 (C) 1.1 BODY NEGO (MOX - CONTROL (C) 1.1 UND = UNDERSOYND

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fm0001.mes: 27

3 December 1991

Conclusions

A hardware description language has been formalized.

The FM9001 user-level specification has a mechanically proved implementation.

We hope this effort represents a start towards the notion of a formula manual.

It was a lot more work than we expected. Why? Because of the formalization of many engineering issues.

We believe that formalization of the design process is more important than this specific verification exercise.

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3 December 1991

CH

Derivational Techniques for Hardware

Steve Johnson Indiana University

Design Derivation*

Steven D. Johnson and Bhaskar Bose

Computer Science Department Indiana University

Design derivation
formalised methods
deduction, derivation, stc.
The DDD system
Syntax
Aspects of design algebra
Experimentation
FM850x derivation
FM9001 derivation
Conclusions
Multimodal reasoning

Hetergeneous formal sys

Thanks to: NSF MIPOS-21842, NGT 50051

9117/111 August 18, 1997

Design derivation

formal system

- a language, rules of syntax
- transformations, rules of reasoning

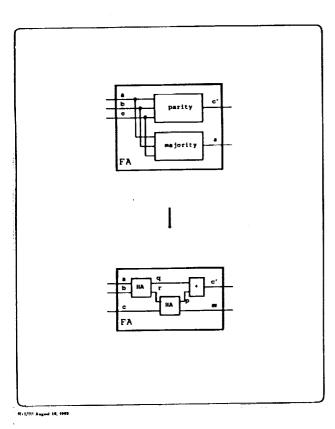
formalization

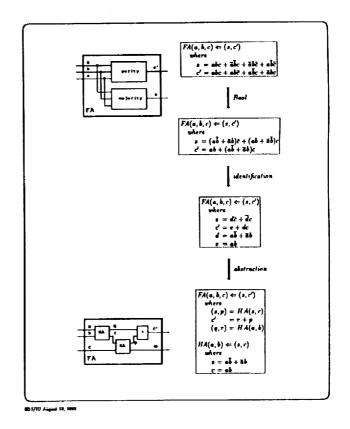
- representing designs as expressions
- representing designing as an inference process

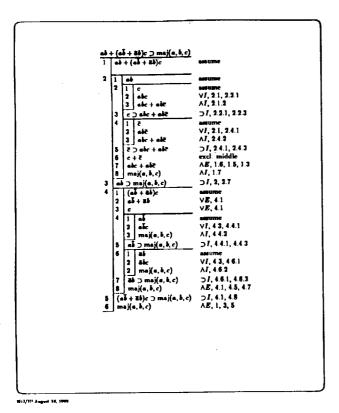
For example, verification

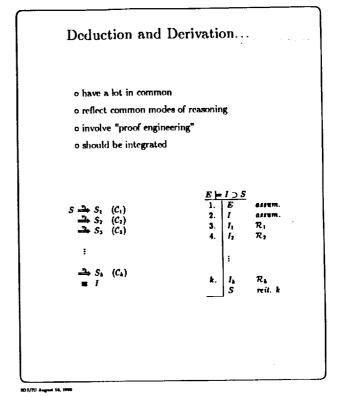
- \bullet proof of an implementation, $E \models I \supset S$
- ullet derivation of an implementation, $S \stackrel{E}{\Longrightarrow} I$

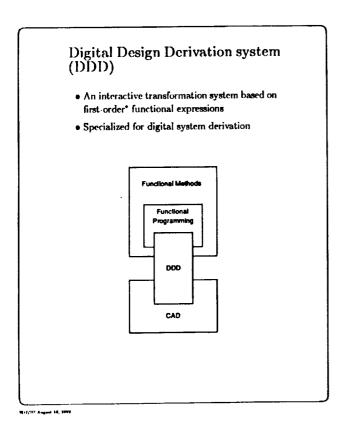
201/TU August 12, 1995

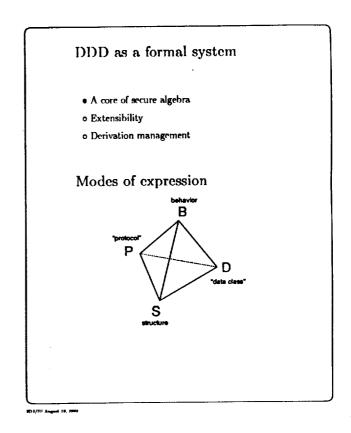








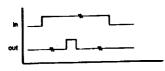




Single Pulser

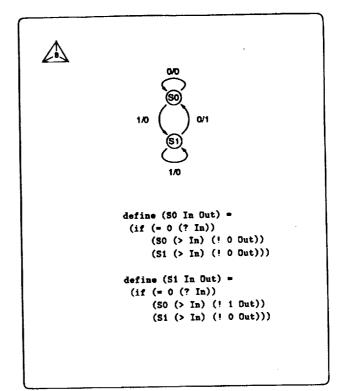


"SP generates a unit pulse for every pulse received"

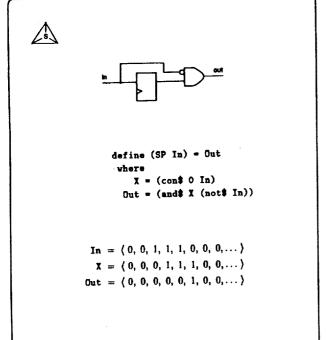


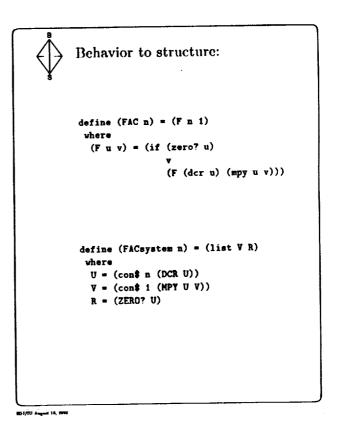
SD | /|TT August 18, 1985

R11/717 August 18, 1993



D)/TU August 16, 100





FM8501 specification [Hunt]

```
(defn SOPT (reg-file venl-mem c-fing v-fing n-fing n-fing let)
(if (alisty int)
(lite reg-file venl-mem c-fing v-fing n-fing n-fing)
(SOPT (reg-file -infter-opyrd-b-post-licrosent)

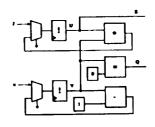
reg-file real-mem c-fing v-fing n-fing n-fing)
(real-mem fiter-venl-mrity

reg-file real-mem c-fing v-fing n-fing n-fing)
(update-v
(b-cc-set (current-instruction reg-file real-mem))
c-fing
(cur-min-currentla reg-file real-mem c-fing))
(update-v
                                     (c twrstrer-results registers (rejector)
(bec-est (current-instruction Teg-file resi-men))
v-fing
(v (br-mlu-cu-results reg-file resi-mem c-fing)))
(spintor)
                                                (b-cc-set (current-instruction reg-file real-nee))
                                     (b-cc-set (current-instruction reg-file real-mee))
(update-v
(b-cc-set (current-instruction reg-file real-mee))
                                      n-flag
(negativep (bv-to-tc (bv (bv-slu-cv-rosultz
reg-file reel-men c-flag))))
(cdr lat))))
```



Scrialization

```
define (FACsystem n) = (list V R)
 where
  U = (con * n (DCR U))
  V = (con$ 1 (MPY U V))
  R = (ZERO? U)
```



SDJ/It! August 16, 196

RF1/ITT August 18, 1982

```
define (FAC n) = (F0 n 1)
 where
  (FO u v) = (if (zero? u)
                  (Fi u (mpy u v)))
  (Fi u v) = (F0 (dcr u) v)
                    <u>-</u>
                        •/.
```

FM8501 implementation [Hunt]

(defn BIG-MACHIFE (our reed write disel reset he-stere data-out reg-file addr-out c-file r-file s-file a-file a-reg b-reg i-reg visual-seu Yesl-seu seury-eatch-dog-history oracle)

(if (aliety oracle)

(list may rood write dtack roset no-store data-out reg-file addr-out c-flag w-flag m-flag m-rag b-rag i-rag wismal-mem roal-mem pemory-match-dog-bistory)

defront crima visua react no-store data-out reg-file

addrout crima vilug arilag arilag areg breag ireg

visual-mem real-mem nemovy-match-dog-history)

(Bid-RACRIFE (cor nex irrag datch react no-store)

(read mer irrag)

(croite mer irrag datch react no-store)

(datch (cur orecle))

(react (cur orecle))

(no-store no-store crima vring nefleg nefleg

irrag mer)

(data-out data-out ureg breag crima irrag mer)

(reg-file reg-file data-out irrag mer No-store

react)

(addrout addrout veg-file irrag mer no-store

react)

(addrout addrout reg-file irrag mer no-store

(s-file g-file areg breag irrag mer)

(s-file g-file areg breag irrag mer)

(s-file g-file areg breag irrag mer)

(s-file g-file areg breag crima irrag mer react)

(b-rag breag visual-mem reg-file irrag mer react)

(s-file g-file areg visual-mem mer)

(visual-mee real-mem read write addr-out

memory-metch-dog-history

(datch (cur oracle)))

(react-dog real-mer)

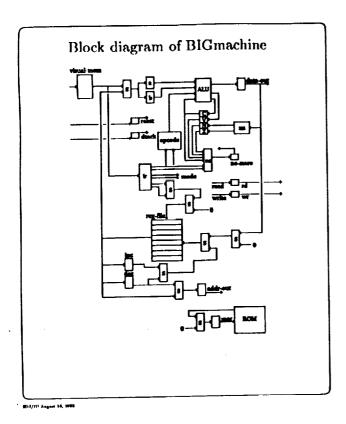
(datch (cur oracle))

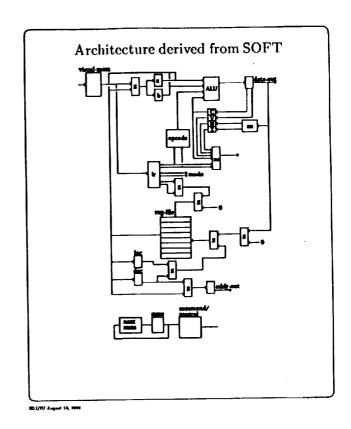
(match-dog read write (datch (cur oracle))

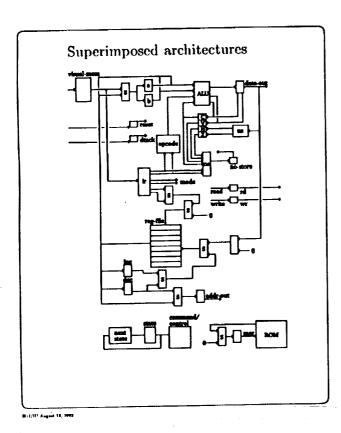
data-out addr-out)

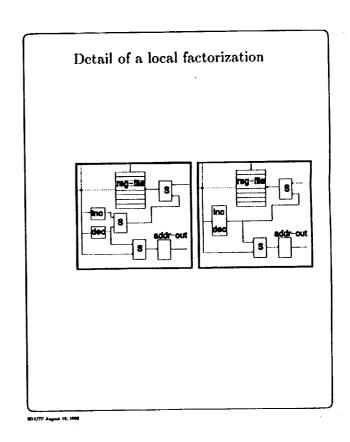
(data-out addr-out)

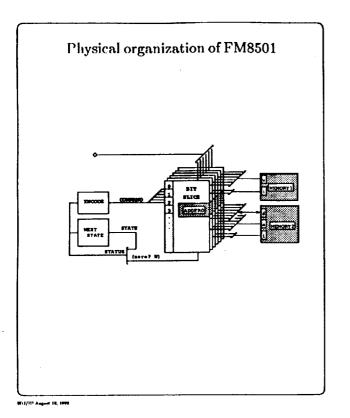
8D 1/1U August 18, 1991

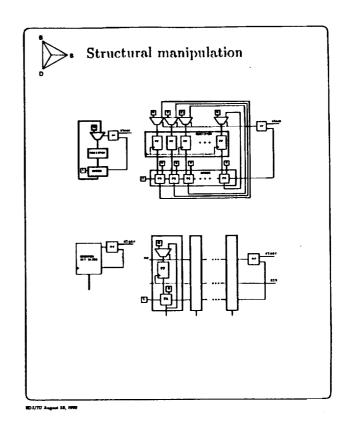


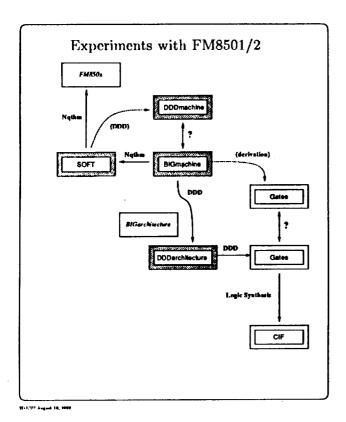


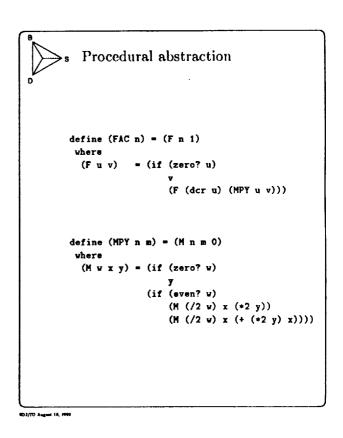






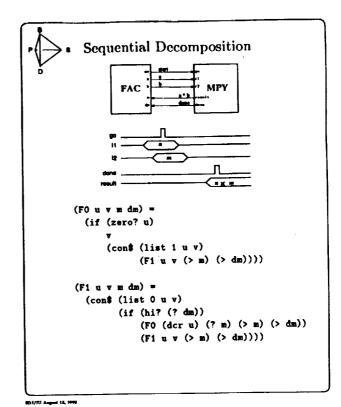








Incorporating procedures



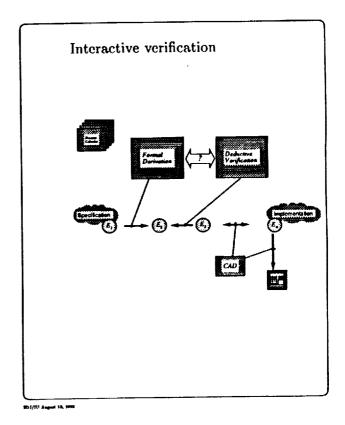
51/20 Access 12 150

Design derivation

Construction of an implementation by equivalence preserving transformations.

$$\mathcal{E}_0 \xrightarrow{\mathbf{r}_1} \mathcal{E}_1 \xrightarrow{\mathbf{r}_2} \mathcal{E}_2 \xrightarrow{\mathbf{r}_3} \cdots \xrightarrow{\mathbf{r}_k} \mathcal{E}_k$$

- @ maintaining the global view
- making local transformations
- ① mundane design
- ⊖ no "complete" algebra
- ⊖ fixes "equivalence"
- ⊖ inhibits eleverness



N13/11! August 18, 1003

Results of Workshop Survey

Each participant at the workshop was asked to complete a detailed survey. Fifty-three people returned the survey; this section presents the results.

For each question asked on the survey, the specific question is reproduced and the answers to the question are tabulated below. If a person circled multiple answers to a question for which only one answer was expected, the results were weighted. For example, in response to question 2, one Formal methods developer circled both b and c. This was tabulated as 0.5 for b and 0.5 for c.

Totals or averages are given where appropriate. Not every person answered every question on the survey, so the totals for different questions may vary.

- 1. What is the nature of your organization?
 - a. University
- b. Formal methods developer
- c. Government
- d. Aerospace industry

Question 1					
	a	b	c	d	е
Industry	0	0	0	22	6
Government	0	0	14	0	0
University	2	0	0	0	0
FM Developers	0	9	0	0	0

Note: Six people did not believe that the four listed choices accurately described the nature of their organization. The specific answers given were: transportation, railway transportation, non-profit R&D org, industry/commercial, other, and don't know. For the purpose of recording the answers, these 6 surveys are grouped with Industry.

- 2. What is your primary job function?
 - a. Basic research
- b. Applied research
- c. Product development

- d. Management
- e. Other

Question 2					
	a	Ъ	c	d	е
Industry	1	17	5	2	3
Government	1	5	0	4	3
University	1	1	0	0	0
FM Developers	3	1.5	0.5	4	0
Totals	6	24.5	5.5	10	6

- 3. Please rate your understanding of formal methods theory and practice:
 - a. Novice

- b. Somewhat familiar
- c. Knowledgable

- d. Considerable
- e. Expert

Question 3					
	a	Ь	c	d	e
Industry	8	10	6	4	0
Government	Ģ	4	3	0	1
University	0	0	0	1	1
FM Developers	0	0	0	1	8
Totals	14	14	9	6	10

¹NASA Langley personnel involved in planning and conducting the workshop did not fill out a survey.

Note: One of the goals of the workshop was to attract people with widely varying understanding of formal methods. These numbers suggest that this goal was met.

- 4. What is the general level of awareness of formal methods within your organization?
 - a. None

- b. Minimal
- c. Sparse

- d. Moderate
- e. Considerable

Question 4					
•	a	b	c	d	е
Industry	7	13	4	1	3
Government	4	8	1	0	1
University	0	0	0	2	0
FM Developers	0	0	1	0	8
Totals	11	21	6	3	12

- 5. Before attending this workshop, how would you have rated the state-of-the-art of formal methods in terms of its potential for immediate application?
 - a. Not usable
- b. Needs more time
- c. Mearly ready

- d. Ready now
- e. Has been ready

Question 5					
•	a	ь	c	d	е
Industry	4	16	4	3	1
Government	2	5	4	1	1
University	0	1	1	0	0
FM Developers	0	0	6	1	1
Totals	6	22	15	5	3

Note: Three FM developers, one who answered d and two who answered c augmented their responses with the comment "for some applications."

- 6. How that you've attended this workshop, how would you rate the state-of-the-art of formal methods in terms of its potential for immediate application?
 - a. Not usable
- b. Needs more time
- c. Mearly ready

- d. Ready now
- e. Has been ready

Question 6					
•	a	Ъ	c	d	е
Industry	1	16	8	3	0
Government	0	4	6	2	0
University	0	0	2	0	0
FM Developers	0	0	7	1	1
Totals	1	20	23	6	1

Note 1: See note for Question 5.

Note 2: The results to this question demonstrate that the workshop did alter some people's perceptions of the state-of-the-art. Particularly interesting is that before the workshop, the perception of the state of the art by nine people was at one or the other extreme, but after the workshop, the number of people at one or the other extreme was reduced to two.

- 7. Please rate the extent to which formal methods is practiced today within your organization:
 - a. Hever

b. Seldom e. Often

c. Sporadically

d. Occasionally

Question 7					
	a	b	c	d	e
Industry	15	9	2	1	1
Government	9	3	0	2	0
University	0	0	0	1	1
FM Developers	1	0	2	1	5
Totals	25	12	4	5	7

Note: One FM developer answered a, and added the comment "on our own systems."

- 8. When do you think that formal methods will be used often in your company?
 - a. 0-2 years
- b. 2-5 years
- c. 5-10 years

- d. 10-20 years
- e. Never

Question 8					
	a	Ь	С	d	е
Industry	5	7	12	3	1
Government	4	3	3	2	0
University	1	0	1	0	0
FM Developers	5	2	1	0	0
Totals	15	12	17	5	1

Note: An individual from industry answered c with the comment "unless required by customers earlier."

- 9. How difficult do you feel it is to put formal methods into practice?
 - a. Extremely
- b. Very

c. Moderately

- d. Somewhat
- e. None at all

Question 9		•			
	a	b	c	d	е
Industry	7	9	12	0	0
Government	2	7	4	1	0
University	0	1	. 1	0	0
FM Developers	2	3	4	0	0
Totals	11	20	21	1	0

- 10. Are you personally inclined to apply formal methods on a design project in the near future?

 - a. Strongly inclined b. Moderately inclined
- c. Indifferent

- d. Not inclined
- e. Would quit first

Question 10					
·	a	Ь	c	d	е
Industry	13	9	1	5	0
Government	8	6	0	0	0
University	2	0	0	0	0
FM Developers	6	3	0	0	0
Totals	29	18	1	5	0

- 11. How well prepared are the professionals in your organization through education and previous training to absorb the technology of formal methods?
 - a. Minimally
- b. Somewhat
- c. Adequately

- d. Receptive
- e. Well prepared

Question 11					
•	a	b	С	d	е
Industry	15	8	3	0	2
Government	7	7	0	0	0
University	0	1	1	0	0
FM Developers	1	0	0	1	7
Totals	23	16	4	1	9

- 12. In your organization, which of the following obstacles exist that inhibit or prevent the use of formal methods? (check all that apply)
 - ___ Management believes it is impractical (Mgmt) ___ Engineering staff believes it is impractical (Eng) ___ Lack of sufficient knowledge about formal methods (Know) (Skill) ___ Lack of required skills (Cost) ___ Up-front cost too high (Neg) ___ Have had negative experiences in the past ___ Do not believe it is useful (Not) (None) ___ No obstacles exist

Question 12								
-	Mgmt	Eng	Know	Skill	Cost	Neg	Not	None
Industry	10	13	24	20	10	4	6	2
Government	5	4	13	11	6	1	4	0
University	0	0	1	0	0	2	0	0
FM Developers	1	2	1	1	3	0	0	4
Totals	16	19	39	32	19	7	10	6

Note: An industry representative checked so obstacles exist, but added the comment "except funding."

13. How would you rate the potential benefits of using formal methods?

- a. Wegligible
- b. Somewhat useful
- c. Moderately useful

d. Helpful

e. Significant

Question 13					
·	a	Ъ	c	d	e
Industry	0	5	1	4	18
Government	0	0	1	4	9
University	0	0	0	1	1
FM Developers	0	0	1	3	5
Totals	0	5	3	12	33

Note: A person from industry circled e, but added the caveat, "if it does all that is advertised."

- 14. How would you rate the costs of formal methods technology relative to the costs of current practice?
 - a. Excessively higher
- b. Somewhat higher
- c. Equivalent

- d. Somewhat lower
- e. Much lower

Question 14					
	a	ь	c	d	e
Industry	4	13	5	4	2
Government	2	8	0	0.5	1.5
University	0	2	0	0	0
FM Developers	0	2	5	0	0
Totals	6	25	10	4.5	3.5

- Note 1: A government representative circled e and added "over system life cycle."

 Note 2: An industry person circled a, with the additional comment "don't see FM replacing anything

 --- it only adds confidence and cost to date."
- 15. How aggressively would you recommend your management pursue the use of formal methods technology?
 - a. Forget it
 - b. Keep up with developments
 - c. Attempt small pilot projects
 - d. Attempt larger applications
 - e. Full speed ahead

Question 15					
	a	b	c	d	e
Industry	0	6	20	2	0
Government	0	0.5	10.5	2	1
University	0	0	2	0	0
FM Developers	0	0.5	2	4.5	1
Totals	0	7	34.5	8.5	2

Note: One industry representative answered c and added the comment "to completion!"

- 16. How much empirical evidence on the benefits of formal methods do you feel is available for managers to make informed decisions regarding its use?
 - a. Insufficient
- b. Hearly sufficient
- c. Adequate

- d. More than adequate
- e. Plentiful

Question 16					
	a	b	c	ď	e
Industry	22	2	3	0	1
Government	8	2	3	0	0
University	1	0	1	0	0
FM Developers	4	3	0	0	2
Totals	35	7	7	0	3

- 17. Rate the importance of reusable formal verifications such as verified clock synchronization circuits and verified software modules.
 - a. None at all
- b. Somewhat
- c. Moderately

d. Very

e. Extremely

Question 17					-
•	a	b	C	d	e
Industry	2	2	7	6	10
Government	0	5	4	3	0
University	0	0	0	1	1
FM Developers	0	0	0	4	4
Totals	2	7	11	14	15

- 18. Rate the importance of generic tools (such as, semi-automatic theorem provers, specification language typecheckers) that can be applied to software/hardware development.
 - a. Wone at all
- b. Somewhat
- c. Moderately

d. Very

e. Extremely

Question 18					
-	a	b	c	d	е
Industry	0	2	5	11	10
Government	0	1	4	6	3
University	0	0	0	0	2
FM Developers	0	0	2	2	5
Totals	0	3	11	19	20

- 19. Rate the importance of the capability of formal methods to produce trustworthy solutions of difficult problems in computer science.
 - a. None at all
- b. Somewhat
- c. Moderately

d. Very

e. Extremely

Question 19					
-	a	b	c	ď	е
Industry	1	3	5	12	7
Government	0	1	4	4	5
University	0	1	0	1	0
FM Developers	0	0	1	2	6
Totals	1	5	10	19	18

Note: An industry person wrote: "(a) who cares (practically) about CS? (c) for real problems. We need trustworthy solutions to real problems!"

- 20. Where in the life-cycle do you feel formal methods can be applied most costeffectively?
 - a. Requirements
- b. High-level design
- c. Detailed design

- d. Implementation
- e. Maintenance

Question 20		,	•		
	8.	b	c	d	e
Industry	15.5	8	3.5	0.5	0.5
Government	9.33	2.83	1.33	0.5	0
University	0.45	0.45	0.45	0.45	0.20
FM Developers	1.67	5.67	0.33	0	0.33
Totals	26.95	16.95	5.61	1.45	1.03

- 21. Where in the life-cycle do you feel formal methods can yield the most significant benefits, irrespective of cost?
 - a. Requirements
- b. High-level design
- c. Detailed design

- d. Implementation
- e. Maintenance

Question 21					
	a	b	c	d	е
Industry	20.33	2.83	3.33	0	0.5
Government	9.33	1.83	0.83	0	0
University	1.33	0.33	0.33	0	0
FM Developers	1.5	1.5	3	1	1
Totals	32.5	6.5	4.5	1	1.5

- 22. How long does it take to become proficient in formal methods?

 - a. Less than 2 weeks b. 2 weeks to 1 month
- c. 1 to 6 months
- d. 6 months to 1 year e. 1 to 5 years

Question 22					
	a	b	c	d	e
Industry	0	0	2	16	9
Government	0	0	1	5	6
University	0	0	0	0	2
FM Developers	0	0	1	7	0
Totals	0	0	4	28	17

- Note 1: Two people, one from government and one from industry, said that the answer to this question was "dependent on background."
 - Note 2: A person from a university circled e, and annotated the answer with "or more."
- 23. What is your opinion of the following statement: "Proficiency in formal methods requires a high degree of mathematical sophistication. ''?
 - a. Agree strongly
- b. Agree

c. No opinion

- d. Disagree
- e. Disagree strongly

Question 23					
•	a	ь	c	d	е
Industry	9	14	1	2	2
Government	5	6	1	1	0
University	0	1	0	1	0
FM Developers	0	6	0	2	0
Totals	14	27	2	6	2

Note: An industry representative circled a, but added, "but it shouldn't be the case!"

- 24. To each of the following areas assign a number from 1 to 5 to denote the importance of the area. Use 1 to denote that the area is extremely important, and 5 to denote that the area is not important at all. Please assign a 0 to any area about which you have no opinion.
 - ___ Basic modeling techniques
 - ___ Code verification (especially for Ada)
 - ___ Education and training
 - ___ Integrated verification systems
 - ___ Mechanical theorem provers
 - ___ Reusable deductive theories (libraries of definitions and theories)
 - ___ Reusable, verified software libraries
 - ___ Special purpose verification tools (such as Spectool, DDD, & Penelope)
 - ___ Specification languages
 - ___ Worked examples

Question 24: I	ndu	stry					
•	0	1	2	3	4	5	Avg.
Model. Tech.	3	11	8	4	2	0	1.9
Code Verif.	4	10	5	6	3	0	2.1
Education	2	15	10	0	0	1	1.5
Int. Ver. Sys.	4	10	6	5	3	0	2.0
Mech. T. Prov.	4	2	11	7	4	0	2.5
R. Ded. Theo.	5	5	11	3	4	0	2.3
R. Soft. Lib.	2	7	11	3	5	0	2.2
Sp. Purp. Tool	5	0	7	14	2	0	2.8
Spec. Langs.	1	14	8	3	1	1	1.8
Examples	2	11	9	4	2	0	1.9

Question 24: C	Fov	erni	mer	ıt			
•	0	1	2	3	4	5	Avg.
Model. Tech.	2	5	4	0	0	2	2.1
Code Verif.	2	4	2	5	0	1	2.3
Education	0	6	0	5	0	2	2.4
Int. Ver. Sys.	3	0	2	4	2	1	3.2
Mech. T. Prov.	1	3	2	3	1	2	2.7
R. Ded. Theo.	2	1	2	4	3	1	3.1
R. Soft. Lib.	1	2	2	4	3	1	2.9
Sp. Purp. Tool	4	1	2	4	1	1	2.9
Spec. Langs.	1	4	3	2	1	2	2.5
Examples	1	6	2	2	0	2	2.2

Question 24: U	Jniv	ers	ity				
	0	1	2	3	4	5	Avg.
Model. Tech.	1	1	0	0	0	0	1.0
Code Verif.	0	0	0	0	0	0	_
Education	0	0	0	0	0	0	_
Int. Ver. Sys.	0	0	0	0	0	0	_
Mech. T. Prov.	0	0	0	0	0	0	
R. Ded. Theo.	0	0	0	0	0	0	_
R. Soft. Lib.	0	0	0	0	0	0	-
Sp. Purp. Tool	0	0	0	0	0	0	-
Spec. Langs.	0	0	0.	0	0	0	-
Examples	0	0	0	0	.0	0	

Question 24: F	'M	Dev	relo	per	8		
	0	1	2	3	4	5	Avg.
Model. Tech.	0	6	2	1	0	0	1.4
Code Verif.	0	3	2	2	1	1	2.4
Education	0	6	2	1	0	0	1.4
Int. Ver. Sys.	0	5	1	2	1	0	1.9
Mech. T. Prov.	0	3	3	2	1	0	2.1
R. Ded. Theo.	0	3	6	0	0	0	1.7
R. Soft. Lib.	0	4	2	4	0	0	2.0
Sp. Purp. Tool	0	3	2	1	3	0	2.4
Spec. Langs.	0	3	6	0	0	0	1.7
Examples	0	5	2	1	1	0	1.8

Note 1: Answers of 0 were ignored in calculating the averages.

Note 2: For a few respondents, the answers to this question seemed inconsistent with answers to other questions. We suspect that some people may have failed to read the question carefully, and as a result reversed the ordering (that is, used 5 to denote extreme importance and 1 to denote no importance); however, we recorded their responses as given.

25. To each of the following tools and techniques assign a number from 1 to 5 to denote your perception of the usefulness of the tool/technique. Use 1 to denote that you believe the tool/technique may be extremely useful, and 5 to denote that you believe the tool/technique is useless. Please assign a 0 to any tool/technique about which you have no opinion.

____ Boyer-Moore ____ DDD ____ EVES
___ HOL ___ Modelisation ____ Muprl
___ Penelope ____ PVS/Ehdm ____ Safety analysis
____ Spectool

Question 25: I	ndus	try					
•	0	1	2	3	4	5	Avg.
Boyer-Moore	9	1	4	10	3	1	2.9
HOL	8	1	7	6	5	1	2.9
Penelope	12	0	9	4	3	0	2.6
Spectool	16	0	6	4	2	0	2.7
DDD	19	0	2	4	3	0	3.1
Modelisation	14	5	2	3	2	2	2.6
PVS/Ehdm	5	6	10	5	1	1	2.2
EVES	20	Ō	3	3	1	1	3.0
Nuprl	23	Õ	3	0	1	1	3.0
Safety Analysis	8	14	3	2	1	0	1.5

Question 25: G	ove	rnn	ent	;			
V	0	1	2	3	4	5	Avg.
Boyer-Moore	7	1	3	2	0	0	2.2
HOL	8	2	0	3	0	0	2.2
Penelope	11	1	1	0	0	0	1.5
Spectool	13	0	0	0	0	0	_
DDD	12	0	1	0	0	0	2.0
Modelisation	8	1	2	0	0	0	1.7
PVS/Ehdm	7	3	1	2	0	0	1.8
EVES	12	0	0	1	0	0	3.0
Nuprl	12	0	0	1	0	0	3.0
Safety Analysis	5	5	1	1	0	1	1.9

Question 25:	Univ	ers	ity				
•	0	1	2	3	4	5	Avg.
Boyer-Moore	0	1	1	0	0	0	1.7
HOL	0	0	2	0	0	0	2.0
Penelope	1	0	1	0	0	0	2.0
Spectool	1	0	1	0	0	0	2.0
DDD	1	0	1	0	0	0	2.0
Modelisation	2	0	0	0	0	0	_
PVS/Ehdm	0	2	0	0	0	0	1.0
EVES	0	0	1	1	0	0	2.5
Nuprl	0	0	2	0	0	0	2.0
Safety Analysis	1	0	0	0	1	0	4.0

Question 25: F	'M	De	velo	per	8	_	
•	0	1	2	3	4	5	Avg.
Boyer-Moore	0	0	5	1	0	0	2.2
HOL	0	0	3	2	2	0	2.9
Penelope	0	3	0	2	2	0	2.4
Spectool	1	3	0	3	0	0	2.0
DDD	2	0	1	3	0	1	3.2
Modelisation	3	1	1	1	1	0	2.5
PVS/Ehdm	0	1	5	1	0	0	2.0
EVES	1	1	3	2	0	0	2.2
Nuprl	0	0	0	1	4	2	4.1
Safety Analysis	2	1	2	1	1	0	2.4

Note: See the notes for Question 24.

- 26. How expressive should a formal language be?
 - a. Very expressive (such as Z and VDM)
- b. To the level of higher-order logic
- c. To the level of 1st order logic
- d. To the level of Prolog
- e. To the level of propositional calculus

Question 26					
	a	Ъ	c	d	е
Industry	14	6	2	1	0
Government	2	4	0	0	1
University	1	0.5	0.5	0	0
FM Developers	3	4	2	0	0
Totals	20	14.5	4.5	1	1

Note: Four people, one from industry and three from government, did not answer this question, but wrote the following comments instead: "depends on application," "to understanding of user," "this needs to be decided on the basis of the domain of application requirements," and "depends on when it is used."

- 27. How important is it to have a specification language that can mimic the notation typically employed in the problem domain?
 - a. None at all
- b. Somewhat
- c. Moderately

d. Very

e. Extremely

Question 27					
L	a	b	c	d	e
Industry	0	3	5	12	6
Government	0	2	3	2	5
University	0	0	0	1	1
FM Developers	0	0	3	4	2
Totals	0	5	11	19	14

- Note 1: A member of the government answered e, and included the comment: "to be accepted by the engineers and program managers."
- Note 2: Another government representative did not circle an answer, but wrote "It must not necessarily mimic but must be readable by experts in the problem domain."
- 28. How important is the availability of powerful decision procedures in a theorem prover (for example, decision procedures for linear arithmetic and propositional calculus)?
 - a. None at all
- b. Somewhat
- c. Moderately

d. Very

e. Extremely

Question 28		·			
	a	Ь	c	d	e
Industry	0	3	8	7	5
Government	0	1	3	3	2
University	0	0	1	1	0
FM Developers	0	0	1	2	6
Totals	0	4	13	13	13

- 29. To each of the following areas assign a number from 1 to 5 to denote your opinion as to the importance of NASA sponsoring work in the area. Use 1 to denote that you believe it is extremely important for NASA to sponsor work in the area, and 5 to denote that you believe NASA should not sponsor any work in the area.
 - ___ Theoretical research (for example, developing theorem provers)
 - ___ Applied research (for example, pilot projects applying formal methods)
 - ___ Joint projects between traditional engineering groups and formal methods experts
 - ___ Workshops such as this one

Question 29: Indus	try						
	0	1	2	3	4	5	Avg.
Theoretical Research	0	- 8	5	7	3	5	2.7
Applied Research	0	19	6	0	0	3	1.6
Joint Projects	0	23	2	2	I	0	1.3
Workshops	0	17	7	2	2	0	1.6

Question 29: Gover	11111	ent					
	0	1	2	3	4	5	Avg.
Theoretical Research	0	3	5	1	4	0	2.5
Applied Research	0	10	1	1	0	1	1.5
Joint Projects	0	9	3	0	1	0	1.5
Workshops	0	11	I	0	0	1	1.4

Question 29: Unive	rsit	y					
•	0	1	2	3	4	5	Avg.
Theoretical Research	0	0	1	1	0	0	2.5
Applied Research	0	2	0	0	0	0	1.0
Joint Projects	0	1	1	0	0	0	1.5
Workshops	0	1	1	0	0	0	1.5

Question 29: FM Developers							
	0	1	2	3	4	5	Avg.
Theoretical Research	0	4	2	2	1	0	2.0
Applied Research	0	5	4	0	0	0	1.4
Joint Projects	0	5	4	0	0	0	1.4
Workshops	0	2	4	2	1	0	2.2

Note: See the notes for Question 24.

Questions 30-32 were not multiple choice. Only a few representative comments from each organizational category are included below. These comments are presented exactly as given; no editing has been done. For these questions, Government and University participants have been grouped together.

What formal methods have you used?

Industry: Boyer-Moore, cleanroom, Clio, EHDM, HOL, Spectool, temporal logic, VDM, Z

Gov & Univ: Boyer-Moore, cleanroom, DDD, EHDM, HOL, VDM

FM Developers: Boyer-Moore, Clio, EHDM, EVES, HOL, PVS, Penelope, SDVS, Spectool, temporal logic, Z

31. In what applications and parts of the life-cycle have you used formal methods?

Industry: requirements modeling, design, and testing, conceptual study, detailed design, verification of algorithms, implementation

Gov & Univ: software requirements, high level requirements, avionics software, missile systems, electronic message systems, design, implementation, academic research projects

FM Developers: hardware designs, microcode, detailed design, algorithms, high-level HW design

32. Any additional comments?

Industry:

- ''Workshops of this type where interested industries can attend and participate are excellent opportunities for technology transfer. I would encourage WASA to continue this type of interaction.''
- ''I would very much like to see a survey of (1) methods (2) languages & (3) tools presenting PROs & COMs of each. As a novice wanting to enter the field, where do I start?''
- e ''Tools are very important to this effort. Paper and pencil will not spread to industry.''
- ''It would have been nice to actually solve some simple problems using a formal technique rather than seeing lots of talks about proofs.''
- 'Suitable applications of FMs was not elaborated on. I still cannot say 'where' one should apply 'what' FM.''
- ''Need to separate HW FM's from SW FM's.''
- ''This is one of the only forums I have attended that has had equal representation from the software and hardware community sharing roughly equal concerns and a common interest in a technology of equal value and benefit to each community.''
- ''You are overcautious about overselling. ...''

Gov & Univ:

- ''We must find a way to better find errors in Reqm'ts''
- ''It is important for WASA to take a leadership position in Formal Methods for civilian aerospace applications.''
- "FN appears to be currently the most feasible means of adding rigor and consistency to the software development process."
- ''Keep holding this workshop!''
- ''I really wish copies of slides had been available at the conference. It would greatly simplify notetaking.''

FM Developers:

- ''There is no 'royal road' to FM for industry.''
- . "FM is powerful for educating designers."
- · ''Formal methods are no panacea''

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